



NTNU  
Norwegian University of  
Science and Technology

## **Membrane Transport of *n*-butane by a Temperature Gradient**

Isabella Inzoli, Jean-Marc Simon, Sondre. S. Kvalvåg,  
Signe Kjelstrup

Department of Chemistry

22.10.2009

# Outline

Motivation

Method

System

Results

Conclusion

## Acknowledgment

Project financially supported by The Center of Gas Technology NTNU/SINTEF and NFR.



NTNU  
Norwegian University of  
Science and Technology

# Motivation

- Study thermal influence on transport
- Transport properties in micro porous materials
- Transport properties across surfaces
- Coupling of heat and mass transport (NET)



# Model method

- Molecular dynamics simulations
  - Adsorption – Langmuir
  - Sampling in equilibrium
  - Deterministic
- Non-equilibrium Molecular dynamics simulations
  - Gradients in temperature and concentration
  - Steady-state transport

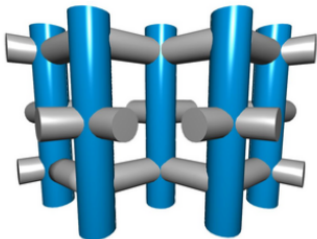
## Newton's equations of motion

$$\mathbf{F}_i = -\frac{\partial V}{\partial \mathbf{r}_i}$$



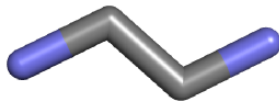
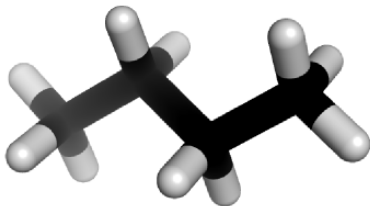
# System

- Perfect zeolite: silicalite-1 ( $[\text{SiO}_2]_{96}$ )
- Zig-zag and straight channels (5.5 Å diam.)
- Channels interconnected
- All-Atom model – flexible grid



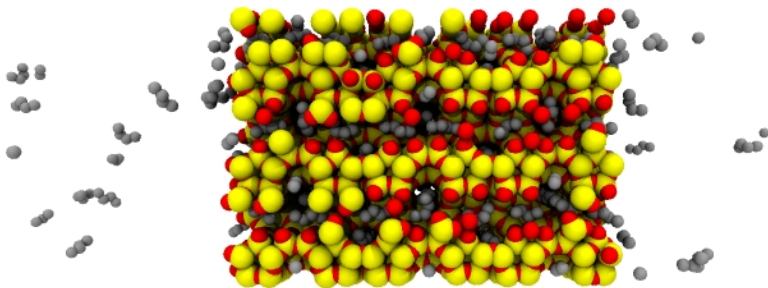
## System cont'd

- *n*-butane
- United atoms model
- Stretching – Bending – Torsion

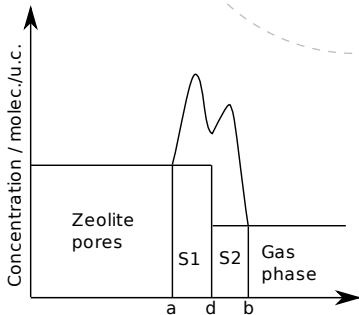
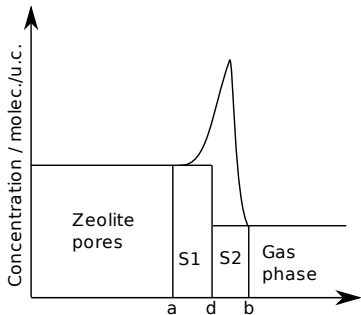


# System cont'd

- Semi-infinite membrane (least image convention)
- Gas phases on both sides
- Different surface structures, and temperatures



# Surface





# Interface transport equations

Describing the transport across the surface:

$$\Delta_{z,g}T = -\frac{1}{\lambda^s} (J_q^{g'} - q_b^{*s,r} J_b) \quad (1)$$

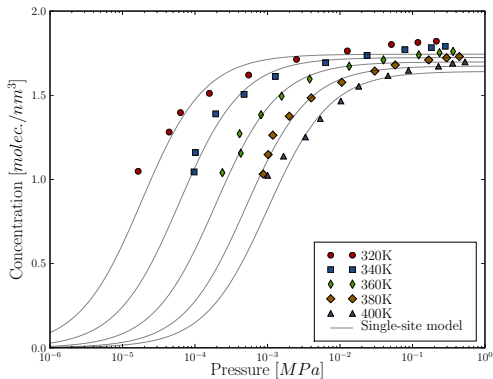
$$\frac{1}{T^z} \Delta_{z,g} \mu_{b,T} (T^z) = -\frac{q_b^{*s,r}}{T^z T^g} \Delta_{z,g} T - R_{bb}^{s,r} J_b \quad (2)$$

Derived from the entropy production at the interface.

[Inzoli, I., Kjelstrup, S., Bedeaux, D. and Simon, J.-M. *Microporous and Mesoporous Materials*, 125 (2009) 112–125.]



# Equilibrium results



Langmuir adsorption

$$c_{pores} = \frac{c_{sat} \cdot K \cdot p}{1 + K \cdot p}$$

$$\Delta H_{ads}^0 = -54 \pm 1 \text{ kJ/mol}$$

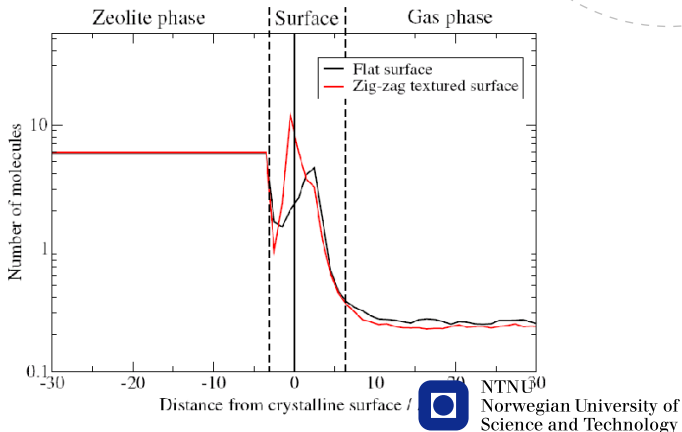
$$c_{sat} \approx 1.75 \text{ molec./nm}^3$$



NTNU  
Norwegian University of  
Science and Technology

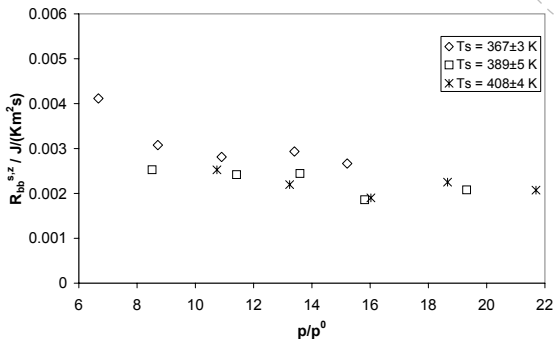
# Surface excess

- Surface is rate-limiting for both heat and mass transfer (negative surface excess)



# Surface resistance to mass transport

— Not very dependent on gas pressure.

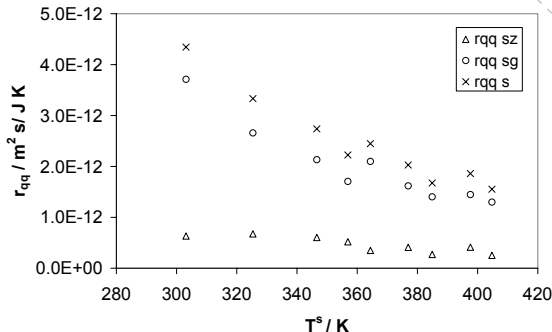


$$\frac{1}{T^z} \Delta_{z,g} \mu_{b,T} (T^z) = -\frac{q_b^{*s,r}}{T^z T g} \Delta_{z,g} T - R_{bb}^{s,r} J_b$$



# Surface resistance to heat transport

— Gas side dominates the resistance.

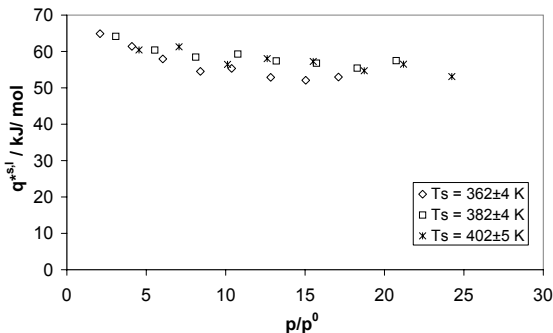


$$\Delta_{z,g}T = -\frac{1}{\lambda^s} (J_q^{l,g} - q_b^{*s,r} J_b)$$



# Coupling

- Large values for Heat of transfer,  $q_b^{*s,r}$
- Significantly larger than for  $\Delta H_{ads}^0$



$$\frac{1}{T^z} \Delta_{z,g} \mu_{b,T} (T^z) = -\frac{q_b^{*s,r}}{T^z T^g} \Delta_{z,g} T - R_{bb}^{s,r} J_b$$

$$\Delta_{z,g} T = -\frac{1}{\lambda^s} (J_q^g - q_b^{*s,r} J_b)$$



# Conclusion

- A membrane surface can well be rate-limiting to transport of heat and mass.
- Proper descriptions of heat and mass transport must take into account the coupling between the two.



# Thank you for your attention!

## Questions?



NTNU  
Norwegian University of  
Science and Technology