



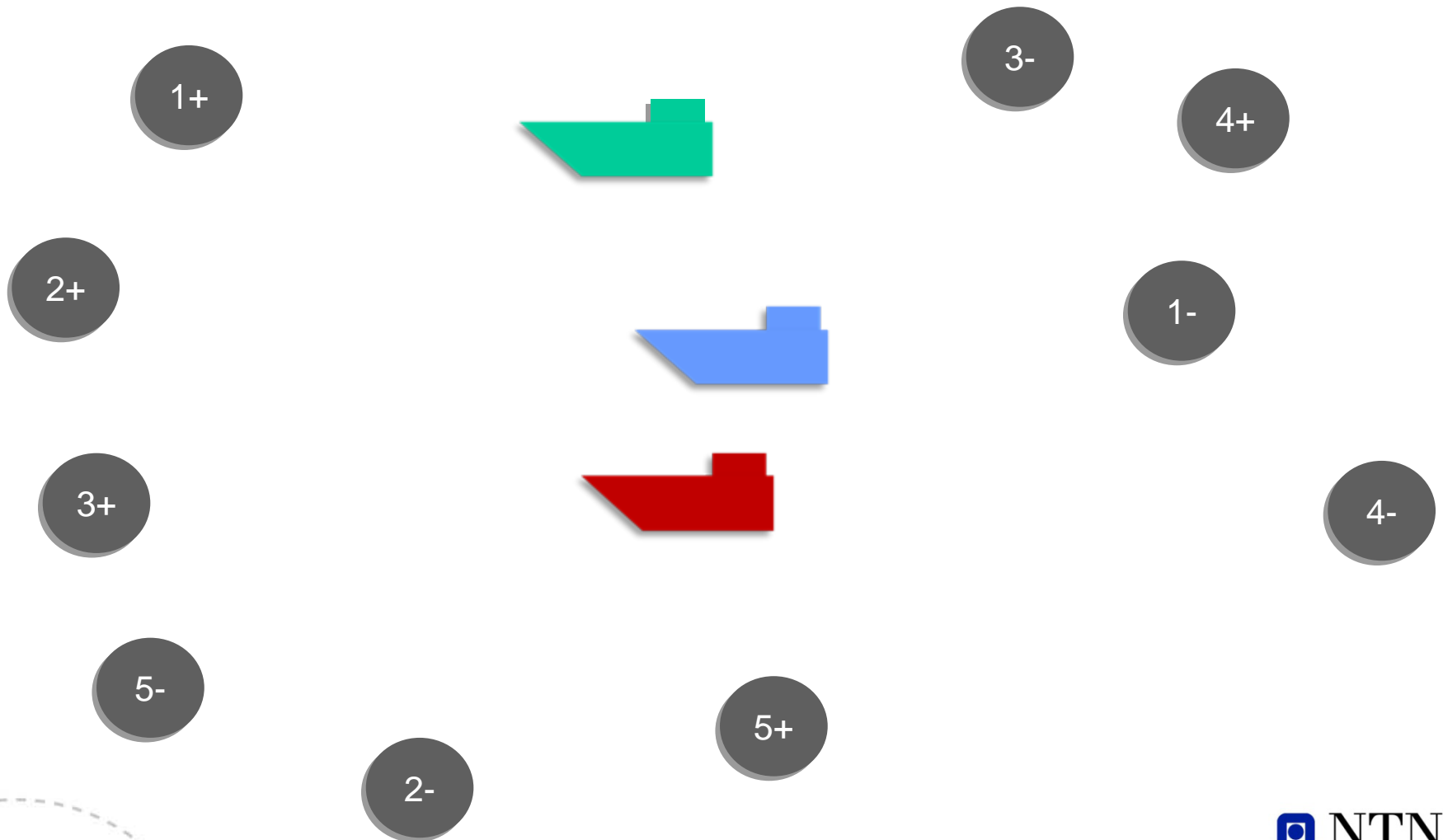
# When Feasibility of Routes is Difficult to Determine: an Example from Maritime Bulk Shipping

Lars Magnus Hvattum<sup>1</sup>, Kjetil Fagerholt<sup>1</sup>,  
and Vinícius A. Armentano<sup>2</sup>

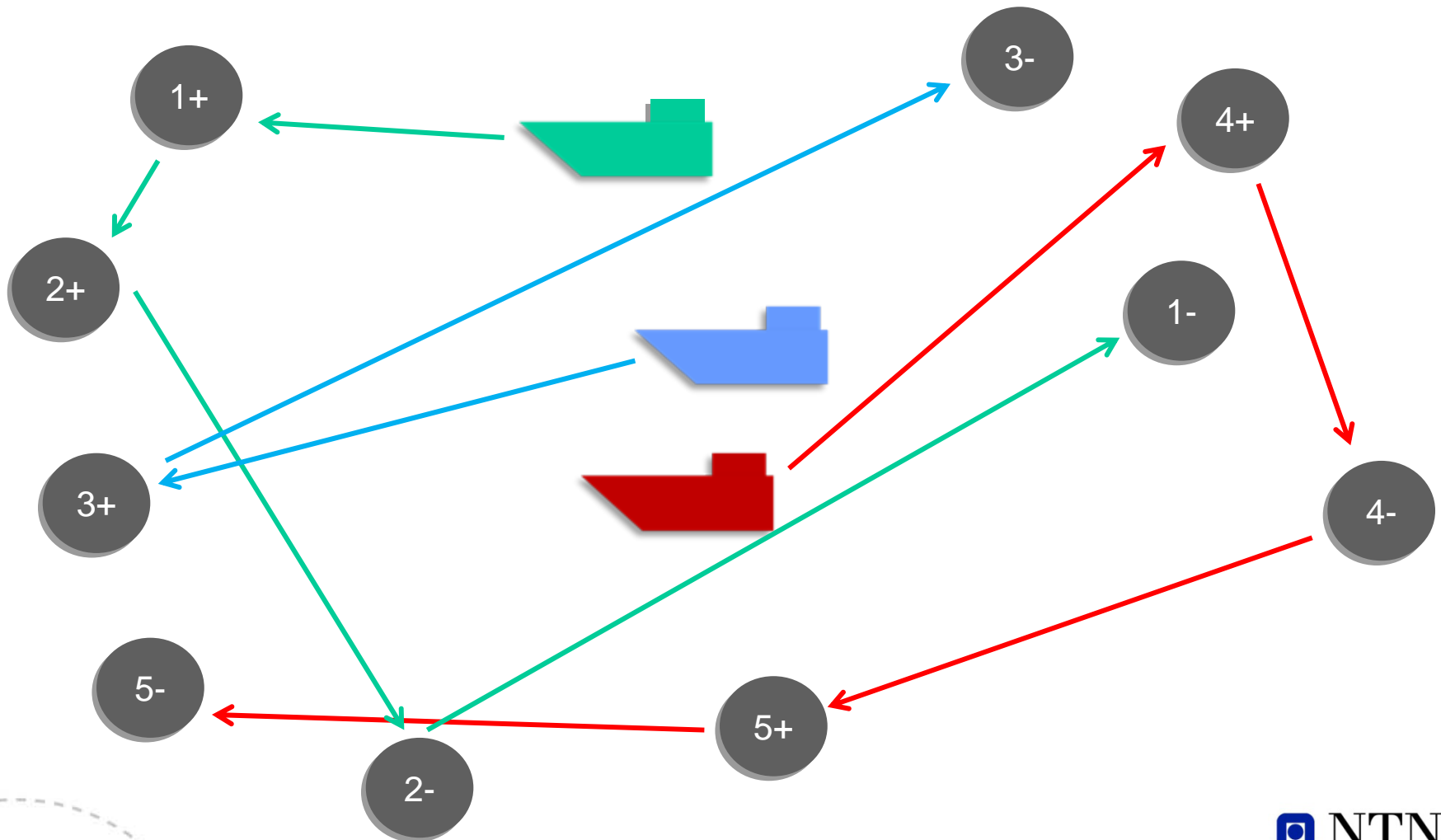
<sup>1</sup> Norwegian University of Science and Technology (NTNU), Norway

<sup>2</sup> Universidade Estadual de Campinas, Brazil

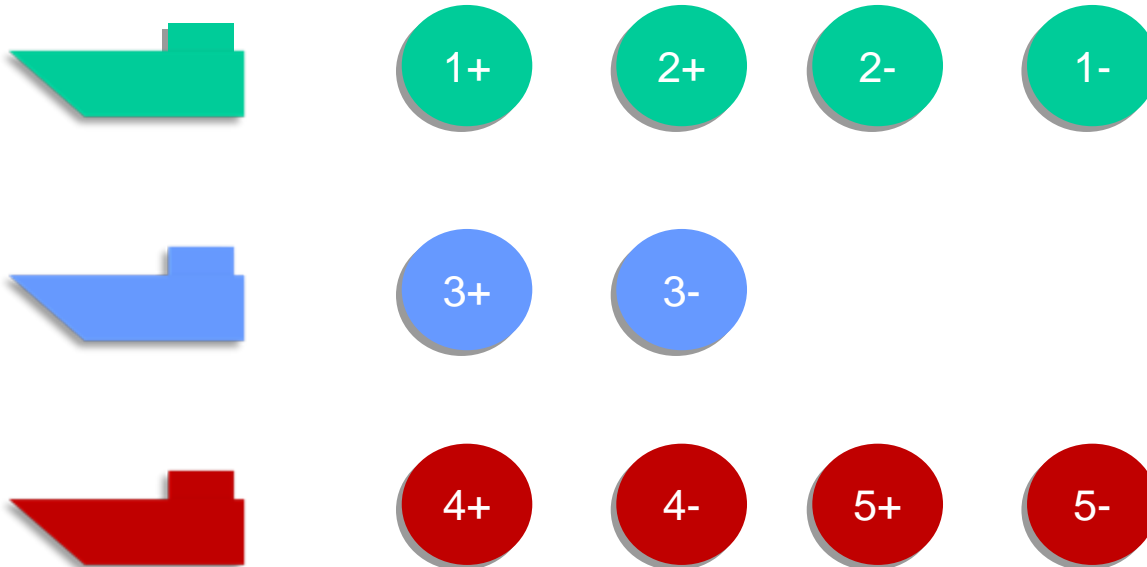
# Main Problem



# Vessel Routes

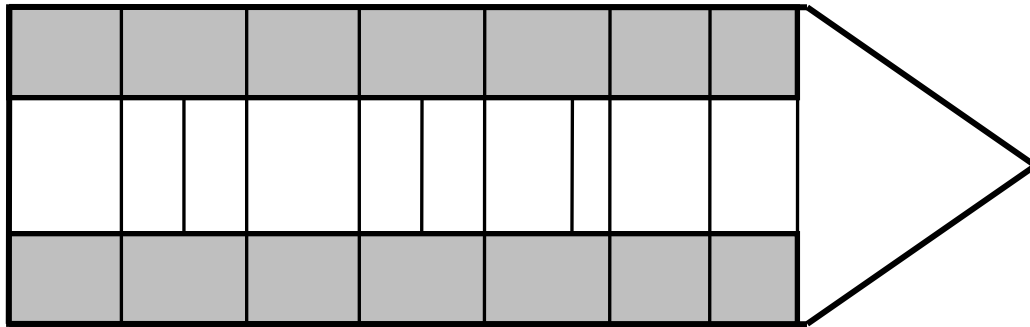


# Possible Solution



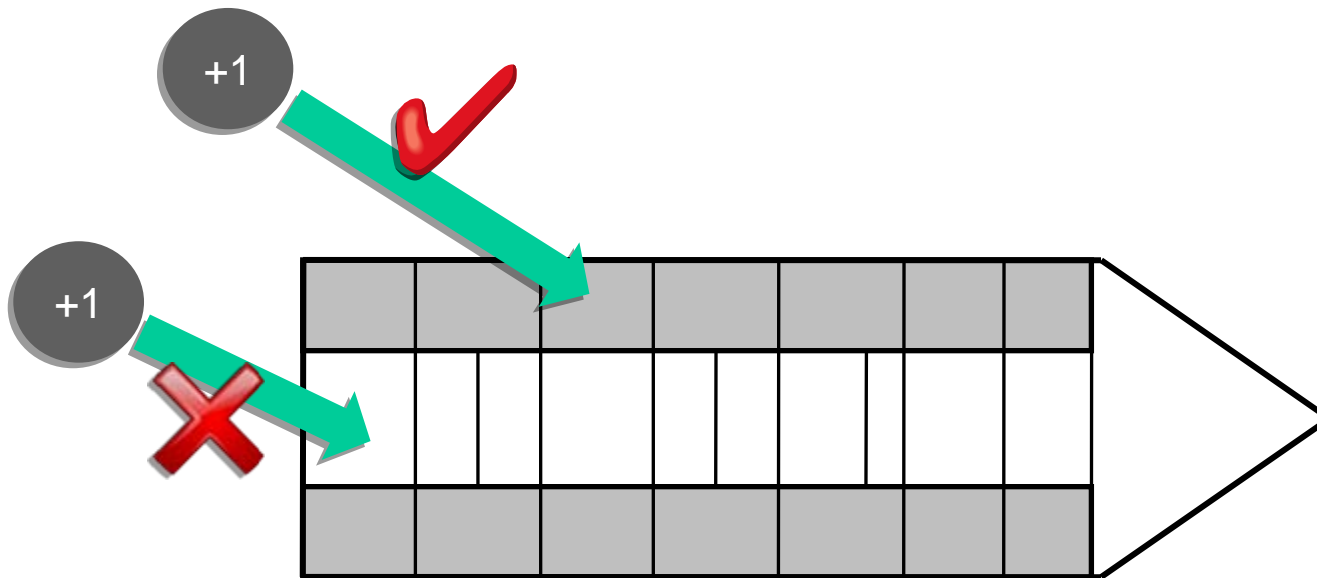
# Constraints (1)

- Each cargo must be allocated to one or several tanks
- Cargo quantity must not exceed the total capacity of these tanks
  - Volume
  - Weight



# Constraints (2)

- Tanks have different coatings, and cargos can only be allocated to tanks with compatible coatings

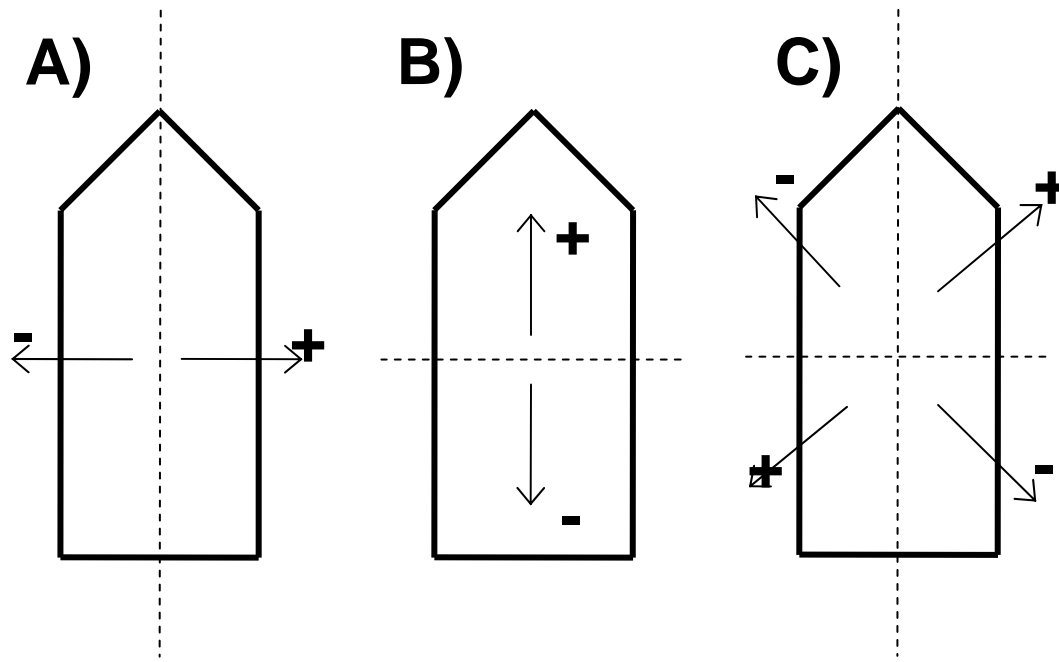


# Constraints (3)

- It is not allowed to move a cargo between tanks after it has been loaded
- It is not allowed to mix cargos, even if it is the same product, in the same tank
- At the beginning of the planning horizon, some tanks may be already occupied by some cargos that have not yet been unloaded
- It may be prohibited to have tanks that are only half-full, in order to avoid sloshing cargos

# Constraints (4)

- There are requirements with respect to the stability (A, B) and strength (C) of the ship





# Constraints (5)

- Due to hazmat rules, certain products cannot be allocated to neighboring tanks
- Due to hazmat rules, certain products cannot be onboard the same vessel at the same time
- Due to hazmat rules, certain products cannot be allocated in sequence to the same tank, except if the tank has been cleaned or the tank has been used by a number of other cargos in between

# Model for the Single Instant TAP

$$b_t x_{lt} \leq y_{lt} \leq c_t x_{lt} \quad (l \in \mathbf{L}, t \in \mathbf{T}_1)$$

$$\sum_{t \in \mathbf{T}_1} y_{lt} = v_l \quad (l \in \mathbf{L})$$

$$\sum_{l \in \mathbf{L}_t} x_{lt} \leq 1 \quad (t \in \mathbf{T})$$

$$\sum_{k \in \mathbf{L}_1} \sum_{u \in \mathbf{T}_{1kt}} x_{ku} \leq M_{lt}(1 - x_{lt}) \quad (l \in \mathbf{L}, t \in \mathbf{T}_1)$$

$$m^{s-} \leq \sum_{l \in \mathbf{L}} \sum_{t \in \mathbf{T}_1} m_t^s (w_l / v_l) y_{lt} \leq m^{s+} \quad (s \in \mathbf{S})$$

$$x_{lt} \in \{0, 1\} \quad (l \in \mathbf{L}, t \in \mathbf{T}_1)$$

$$y_{lt} \geq 0 \quad (l \in \mathbf{L}, t \in \mathbf{T}_1)$$

# Model for the Tank Allocation Problem

$$b_t x_{lt} \leq y_{lt} \leq c_t x_{lt} \quad (l \in \mathbf{L}, t \in \mathbf{T}_1)$$

$$\sum_{t \in \mathbf{T}_1} y_{lt} = v_l \quad (l \in \mathbf{L})$$

$$\sum_{k \in \mathbf{L}_t \cap \mathbf{N}_1} x_{kt} \leq 1 \quad (l \in \mathbf{L}, t \in \mathbf{T})$$

$$\sum_{k \in \mathbf{L}_1 \cap \mathbf{N}_1} \sum_{u \in \mathbf{T}_{1kt}} x_{ku} \leq M_{lt}(1 - x_{lt}) \quad (l \in \mathbf{L}, t \in \mathbf{T}_1)$$

$$m^{s-} \leq \sum_{l \in \mathbf{R}} \sum_{t \in \mathbf{T}_1} m_t^s (w_l / v_l) y_{lt} \leq m^{s+} \quad (\mathbf{R} \in \mathbf{Q}, s \in \mathbf{S})$$

$$h_{lkt}(x_{lt} - z_{lt}) - \sum_{j \in \mathbf{R}} (x_{jt} + h_{lkt} z_{jt}) \leq h_{lkt}(1 - x_{kt}) \quad \begin{array}{l} (l \in \mathbf{L}, t \in \mathbf{T}_1, \\ k \in \mathbf{P}_1 \cap \mathbf{L}_1, \\ \mathbf{R} = \mathbf{P}_1 \setminus \mathbf{P}_k \setminus \{k\}) \end{array}$$

$$x_{lt} \in \{0, 1\} \quad (l \in \mathbf{L}, t \in \mathbf{T}_1)$$

$$y_{lt} \geq 0 \quad (l \in \mathbf{L}, t \in \mathbf{T}_1)$$

$$z_{lt} \in \{0, 1\} \quad (l \in \mathbf{L}, t \in \mathbf{T}_1)$$

# Objective functions

- Minimize the number of cleaned tanks

$$\min z = \sum_{l \in L} \sum_{t \in T_1} z_{lt}$$

- Maximize capacity of vacant tanks during the vessel route?
  - increasing flexibility for future changes in the route
- Maximize the probability of being able to accept future transportation requests?
  - must take all vessel routes into consideration
- Anyway, feasibility is more important!

# Computational Complexity

- Finding a feasible solution is NP-complete
  - even when considering a single instant of the vessel route
    - i.e., can a given set of cargos be present on the ship simultaneously, disregarding the sequence of loading/unloading?
  - even if disregarding
    - all hazmat regulations
    - all stability/strength restrictions
    - anti-sloshing constraints
  - even if allowing loads to be mixed in tanks
    - proofs of NP-completeness then use either hazmat constraints or stability/strength constraints

# Test Instances

- First, how much time is required to solve realistically sized instances?
- Instances generated by varying
  - Ship configuration (24 tanks or 38 tanks)
  - Number of loads (10, 20, or 30)
  - Load categories (0%, 10%, 20%, or 30% of loads are hazardous)
  - Min/max levels of ship utilization (65%, 75%, or 85% full)
  - Size of loads (1-5, 3-9, or 8-16 thousand tons)
- All instances include a history of 10 loads (some of which may still be present on the ship)
- Stability w.r.t. roll is enforced

# Results using CPLEX

- Two different objective functions
  - obj1: minimize the number of tank cleanings
    - potential problem: little guidance when branching
  - obj2: maximize average free capacity during the voyage

	obj1	obj2
	not feasible	not feasible
> 600 seconds	4	3
> 100 seconds	13	9
> 10 seconds	43	48
> 1 second	165	174
in total	720	720

# Which Dimensions Matter?

subset	instances	obj1			obj2		
		feasible	seconds	open	feasible	seconds	open
TAP	720	716	4.13	561	717	5.12	40
L20	240	240	1.11	231	240	0.57	38
L30	240	239	2.21	189	239	2.41	9
L40	240	237	9.14	189	237	9.14	9
C1	180	177	0.35	177	180	0.97	15
C2	180	179	2.23	165	180	5.40	7
C3	180	180	4.00	180	180	4.00	12
C4	180	180	9.88	95	179	10.75	12
F1	240	239	2.81	190	238	3.88	20
F2	240	240	5.14	187	239	8.65	9
F3	240	237	4.45	187	237	4.45	9
T24/S3	180	180	1.21	130	178	1.54	14
T24/S6	180	180	0.23	130	178	0.23	14
T38/S6	180	176	12.79	131	176	11.81	9
T38/S12	180	180	2.50	145	180	3.84	10

**more loads = more difficult**

**more hazmat = more difficult**

**higher ship utilization = unclear**

**smaller loads = more difficult**

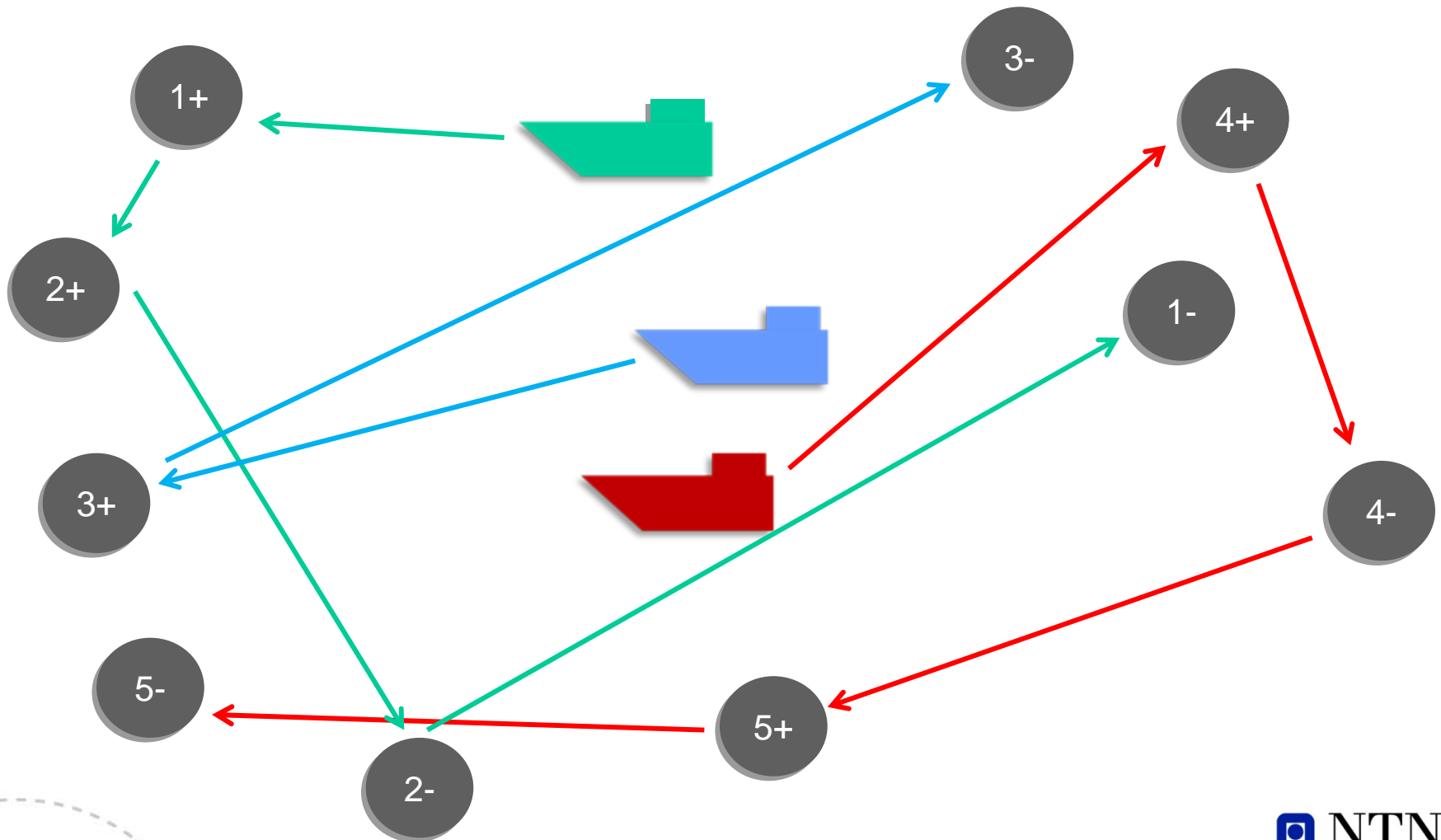
**more tanks = more difficult**



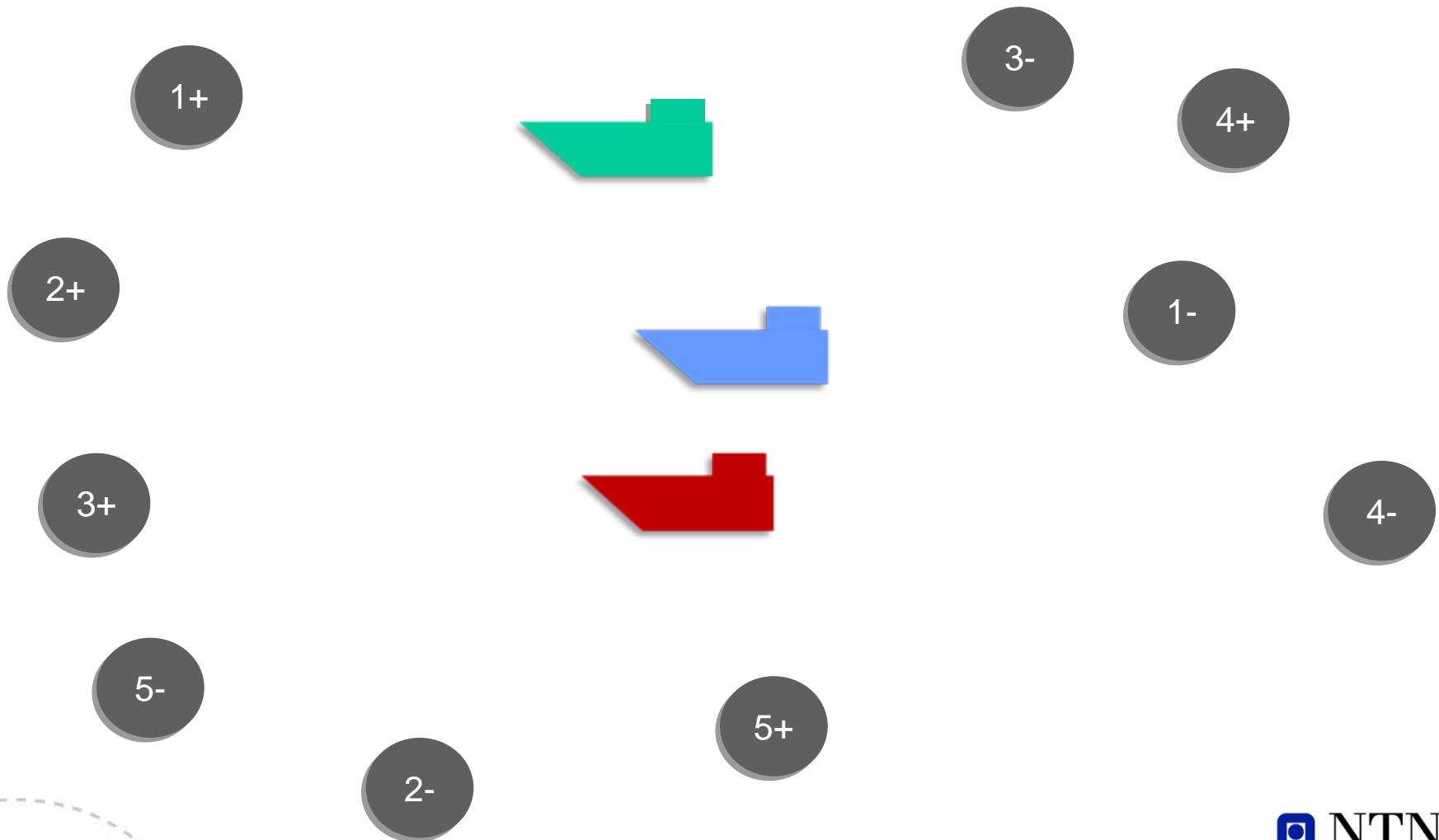
# Solving TAPs and Future Work

- Most realistically sized instances solved by CPLEX within 1 second
  - OK if the goal is to find a feasible stowage plan
- Some instances cannot be solved within 10 minutes
  - CPLEX is not robust
- We can try to modify branching priorities to see if this can guide CPLEX in the difficult cases?
- We can try Constraint Programming solvers?
- We can develop special heuristics that might be better suited to find feasible solutions?

# 1) Finding Stowage for a Route



## 2) Finding Routes and Stowage Together?



# Solving the Main Problem

- For now we focus on the subproblem, TAP
- Eventually, the goal is to solve the main problem: finding the best vessel routes with a feasible stowage plan
- We know that metaheuristic search, such as Tabu Search, works well for routing problems
  - Efficient neighborhood exploration
- What is the best strategy when evaluating a neighbor is NP-complete?

# Future Research

- Improved neighborhood exploration
  - First Improvement
  - Neighborhood reductions
    - Granular Tabu Search
  - Surrogate Evaluation
    - Delay evaluation of stowage plan
    - How to handle infeasible stowage problems?
- Improved solution methods for the stowage problem
  - Use the stowage plan of current solution as a starting point for finding a stowage plan when evaluating a neighboring solution
- Other?



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