

Calculation of zeros in Vector Fitting

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In Vector Fitting, the new poles are calculated as the zeros of $\sigma(s)$ where $\sigma(s)$ is a rational, scalar function

$$\sigma(s) = \frac{y(s)}{u(s)} = \sum_m \frac{c_m}{s - a_m} + 1 = \frac{\Pi(s - z_m)}{\Pi(s - a_m)} \quad (1)$$

From (1) we see that the zeros of $\sigma(s)$ is equal to the poles of $1/\sigma(s)$. The inverse of $\sigma(s)$ we can obtain by interchanging the input (u) with output (y). To do this, we look at (1) in the time domain:

$$\dot{x} = Ax + bu \quad (2a)$$

$$y = cx + du \quad (2b)$$

where A is a diagonal matrix holding the elements $\{a_m\}$, c is a row-vector holding the elements $\{c_m\}$, d is unity, and b is a column of one's.

From (2b) we get:

$$u = d^{-1}(y - cx) \quad (3)$$

Inserting (3) into (2a) we get

$$\dot{x} = Ax + bd^{-1}(y - cx) = (A - bd^{-1}c)x \quad (4)$$

In σ , $d=1$ and so we get:

$$\dot{x} = (A - bc)x = \tilde{A}x \quad (5)$$

The poles are equal to the eigenvalues of \tilde{A} and so we have that the zeros of σ are equal to $\text{eig}(A - bc)$.