



# Flow Observations using Nacelle Lidars: A Study on the University of Stavanger Campus

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Session 2B: Metocean conditions

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# Instruments on campus

2 ZXTM horizontally scanning nacelle lidars



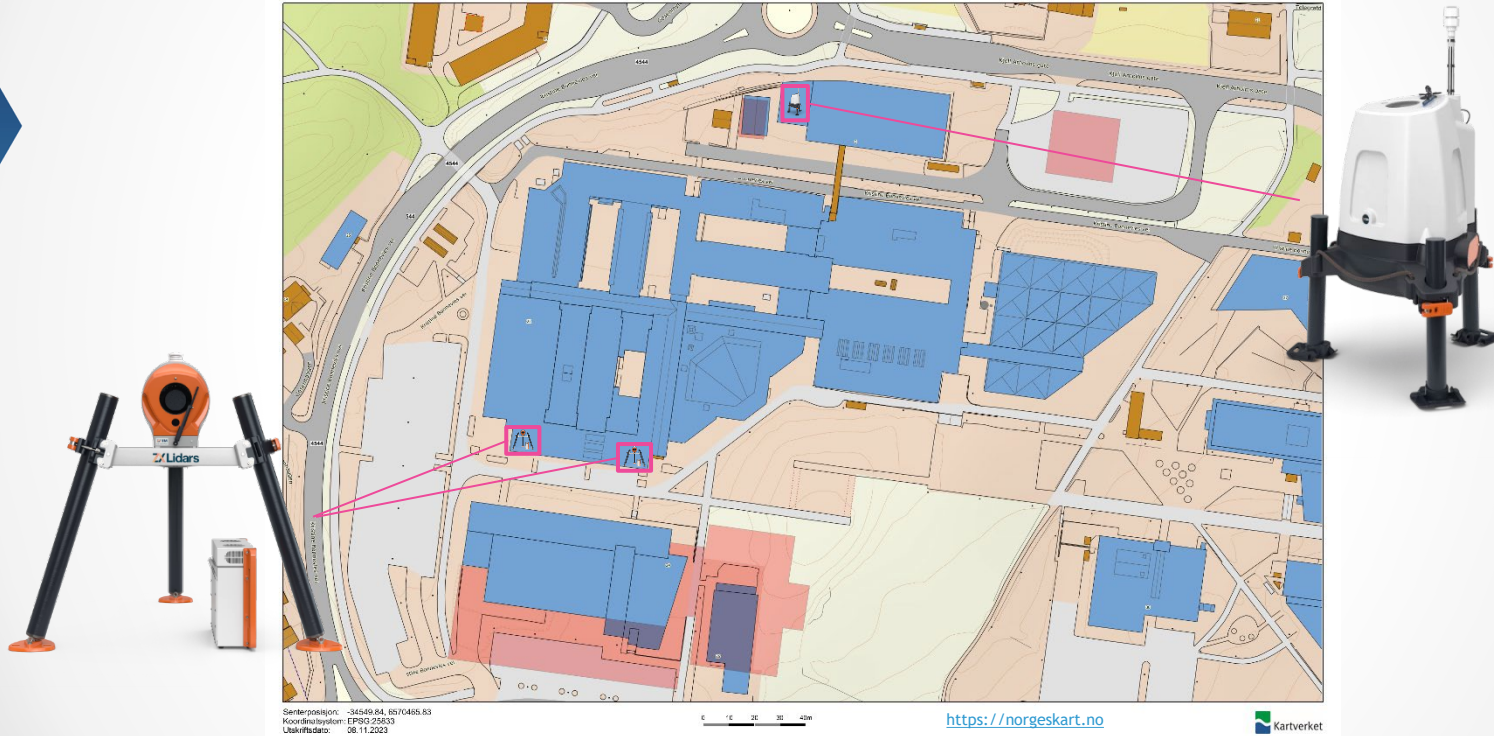
<https://www.zxlidars.com/wind-lidars/>

1 ZX300 vertically profiling lidar



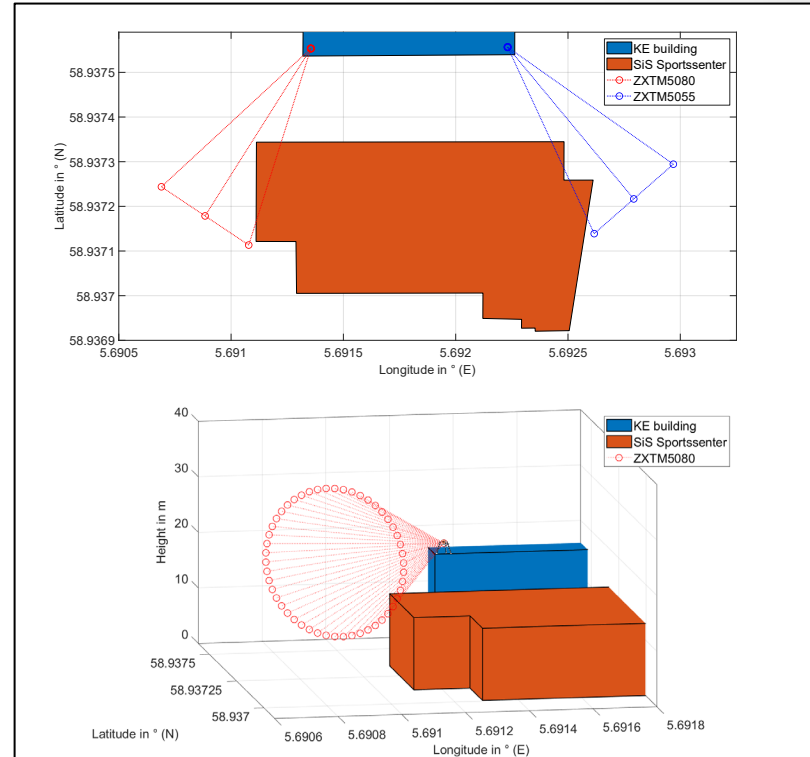
<https://www.zxlidars.com/wind-lidars/>

# Instruments on campus



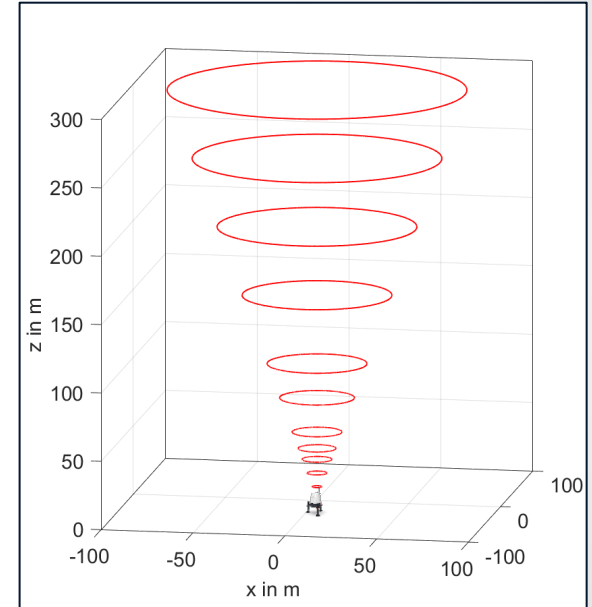
# ZXTM nacelle lidar specifications

- Half cone opening angle 15°
- Scanning distance 50 m
- Scanning circle radius 13.4 m
- Number of scanning points 50
- Sampling rate 50 Hz
- Lidar inclination 5.3°



# ZX300 profiling lidar specifications

- Half cone opening angle  $15^\circ$
- Scanning heights 10 m, 20 m, 30 m, 38 m, 50 m, 75 m, 100 m, 150 m, 200 m, 250 m, 300 m
- Sampling rate at each height 0.06 Hz



# Objectives of the study

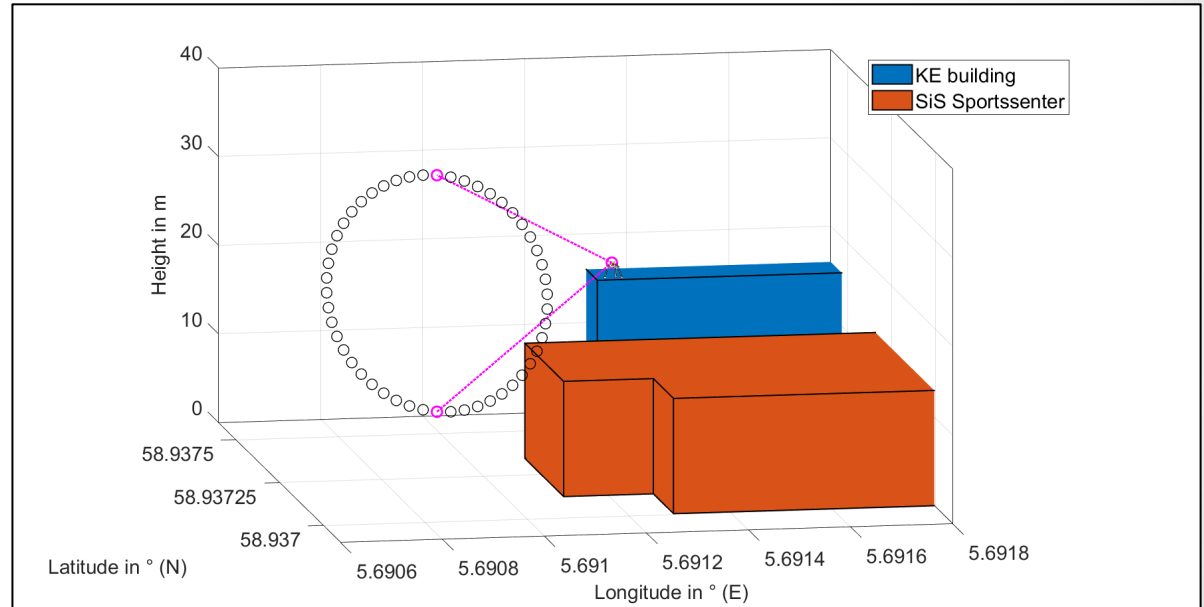
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- Experience in instrument use and data processing
- Evaluation of instruments' potential for:
  - flow characterization in urban environment
  - turbulence characterization
- Investigation of flow conditions on campus

# Time series from radial velocity observations

Estimate:

- $u$  and  $v$   
from horizontal  
beams
- $u$  and  $w$   
from vertical  
beams



# Time series from radial velocity observations

- Estimation of 10-min wind direction

$$\bar{v}_{r,1} = \bar{u} \cos(\omega + \bar{\phi})$$

$$\bar{v}_{r,2} = \bar{u} \cos(\omega - \bar{\phi})$$

- Calculation of instantaneous wind speed and direction

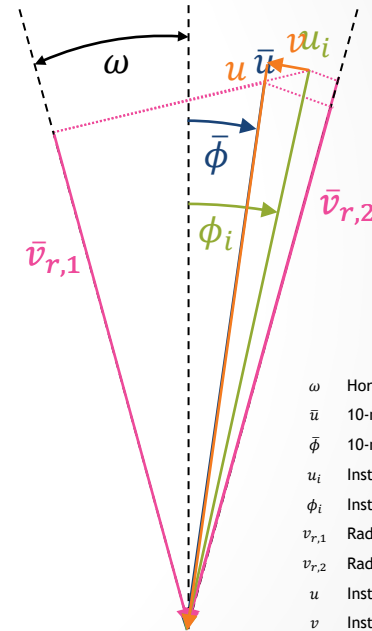
$$v_{r,1} = u_i \cos(\omega + \phi_i)$$

$$v_{r,2} = u_i \cos(\omega - \phi_i)$$

- Decomposition into instantaneous along- and cross-wind components

$$u = u_i \cos(\bar{\phi} - \phi_i)$$

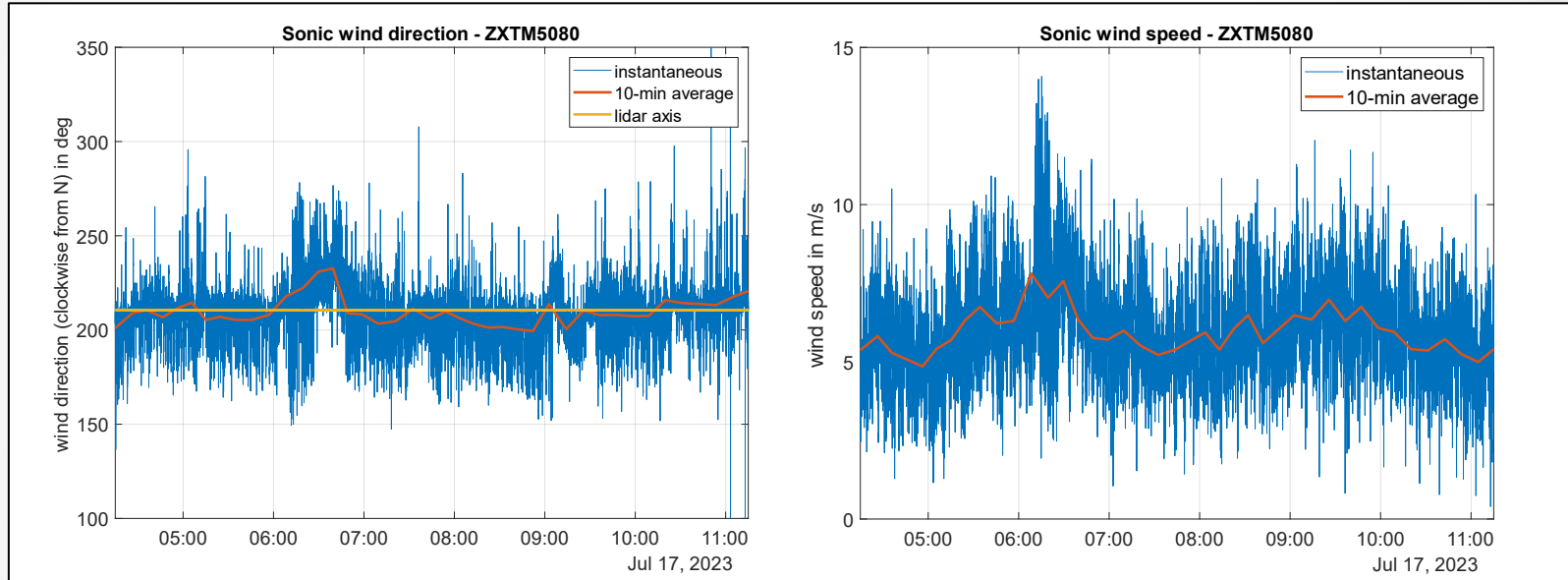
$$v = u_i \sin(\bar{\phi} - \phi_i)$$



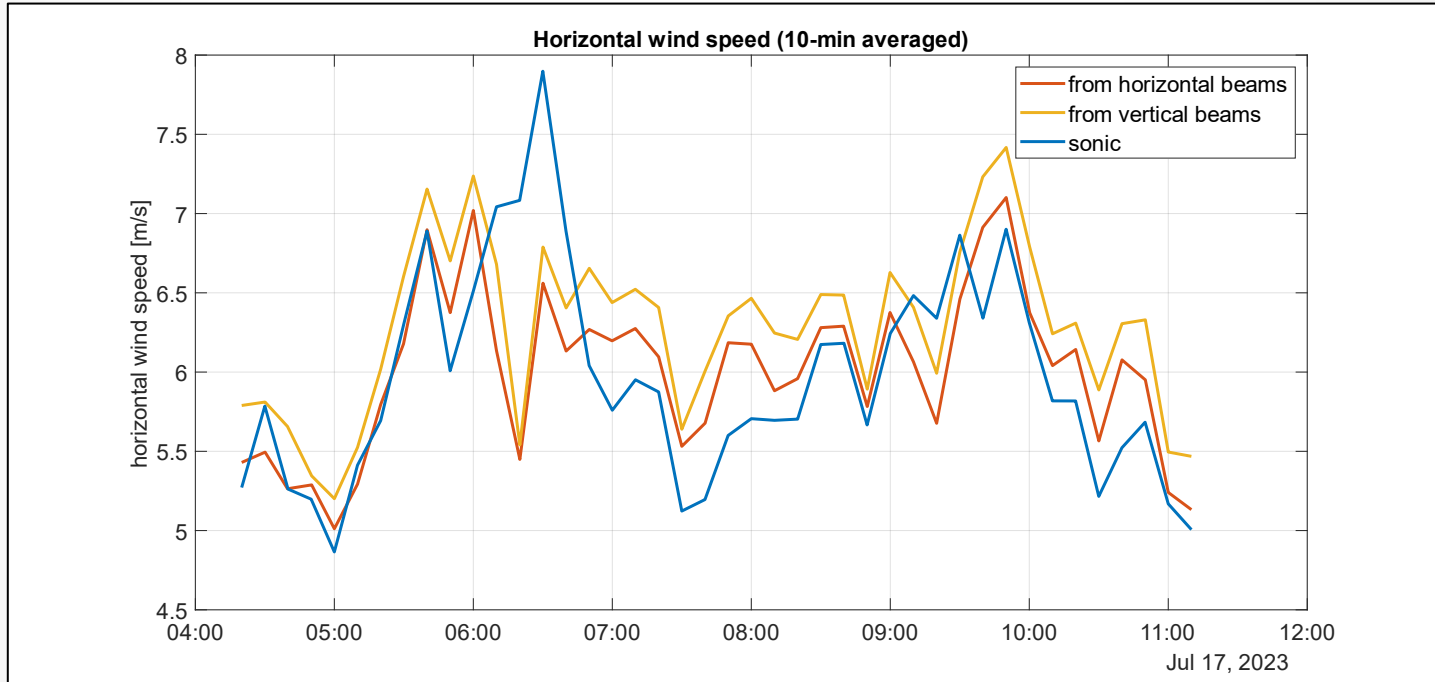
- $\omega$  Horizontal beam angle
- $\bar{u}$  10-min wind speed
- $\bar{\phi}$  10-min offset from lidar axis
- $u_i$  Instantaneous wind speed
- $\phi_i$  Instantaneous offset from lidar axis
- $v_{r,1}$  Radial velocity beam 1
- $v_{r,2}$  Radial velocity beam 2
- $u$  Instantaneous along-wind
- $v$  Instantaneous cross-wind



# Exemplary case

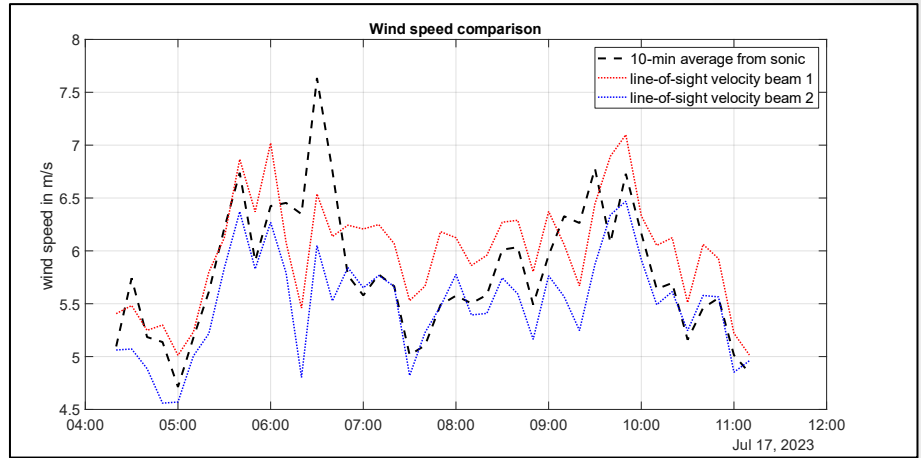
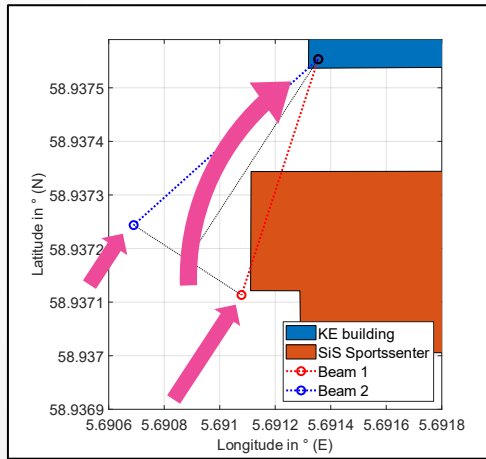


# Wind speed comparison



# Wind speed comparison

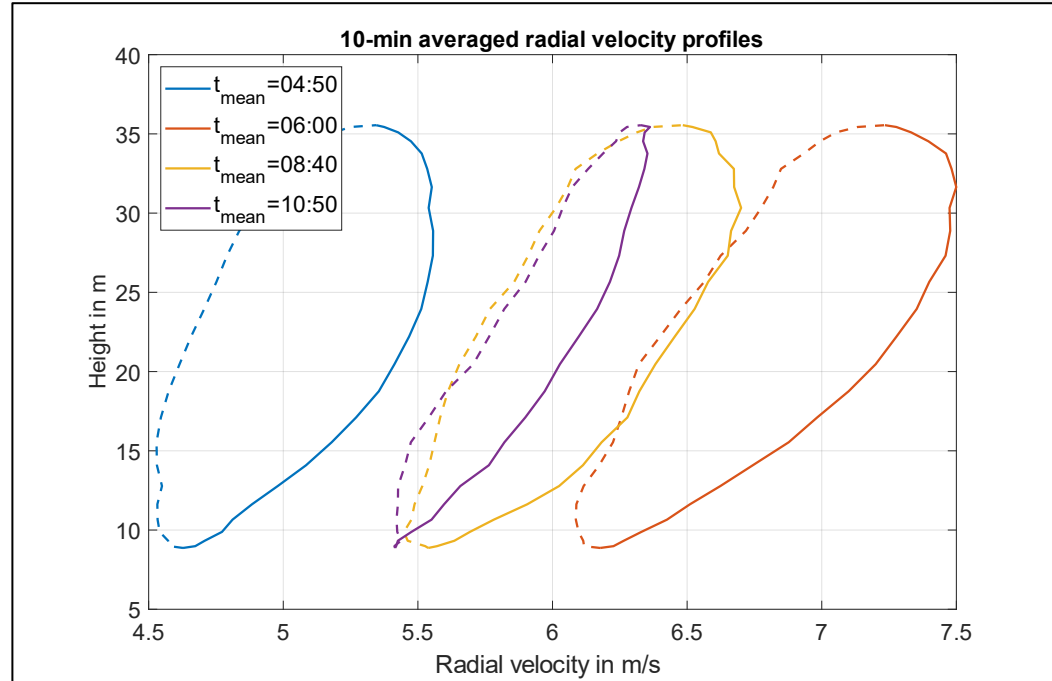
- Systematic difference between radial velocities of horizontal beams



- Likely caused by interference with sports centre
  - A. Local speed-up
  - B. Directional change
  - C. Combination of both

# Wind profiles from nacelle lidar

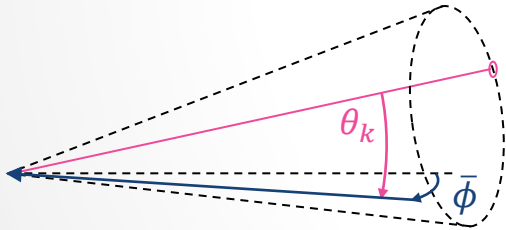
- Solid lines: left side of the scanning circle
- Dashed lines: right side of the scanning circle



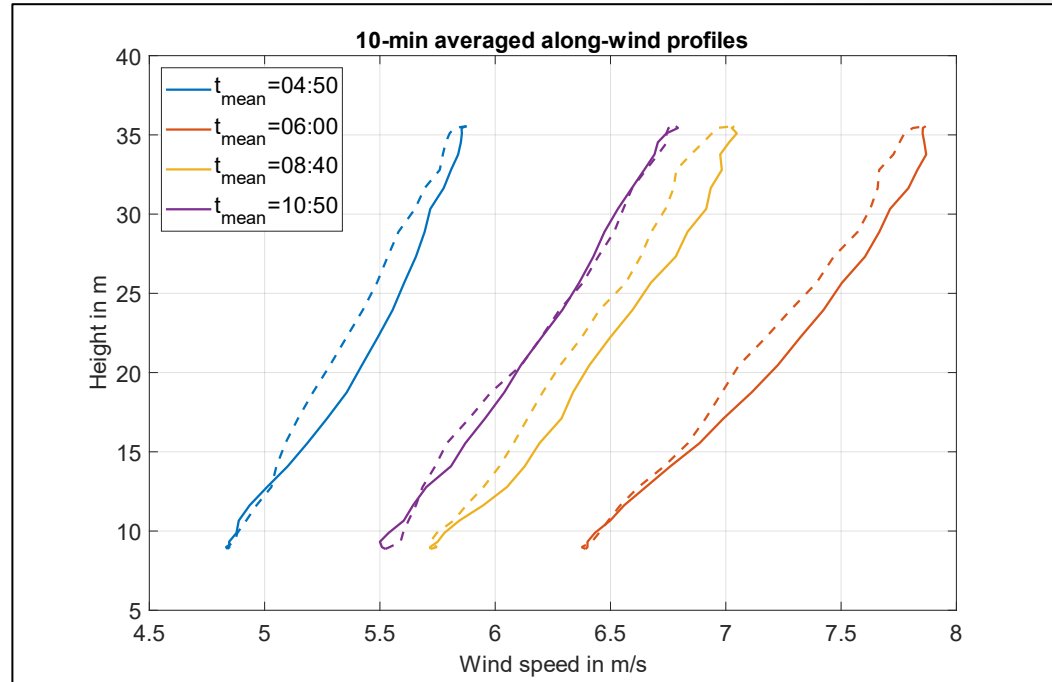
# Wind profiles from nacelle lidar

- Yaw and tilt corrected profiles

$$u_k = \frac{v_{r,k}}{\cos \theta_k}$$

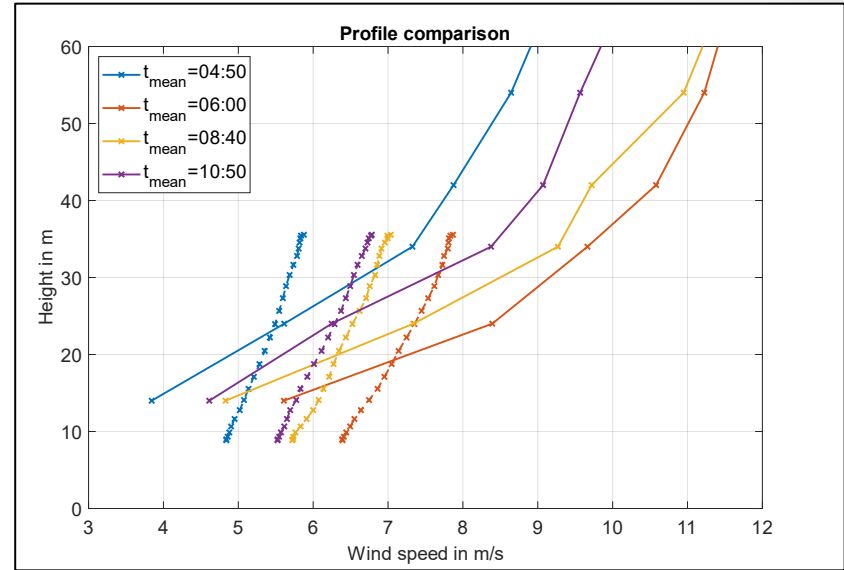
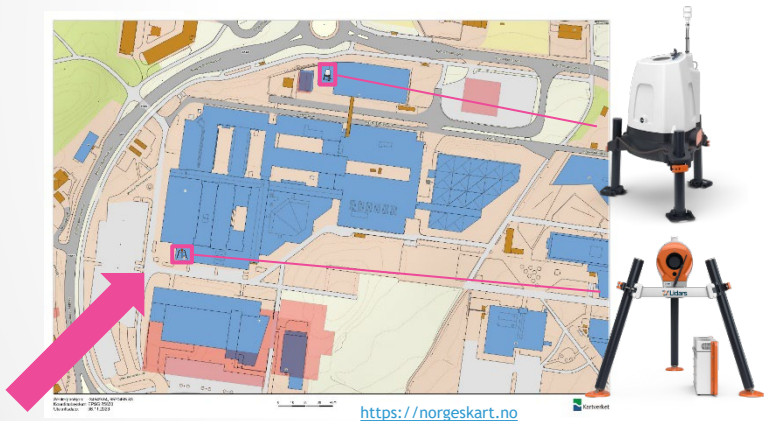


- $\bar{\phi}$  10-min offset from lidar axis
- $v_{r,k}$  Radial velocity of beam k
- $\theta_k$  Along-wind angle of beam k



# Wind profile comparison

- Wind reaches profiler after passing KE building
- boundary layer with steep gradients



- solid lines: profiling lidar
- dashed lines: nacelle lidar

# Fitting of standard wind profiles

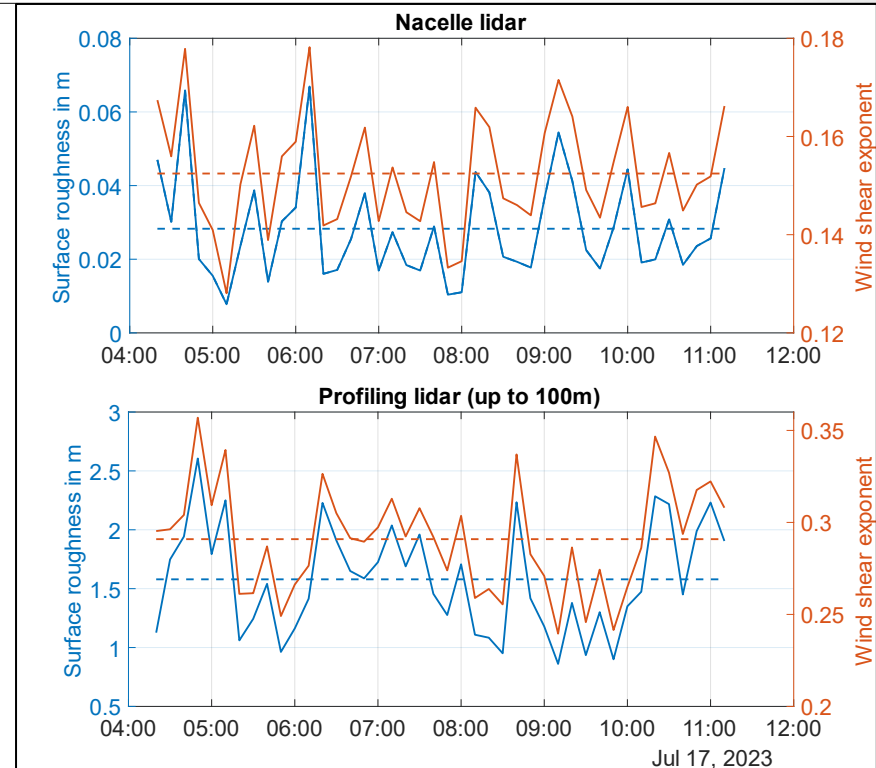
- Power law

$$\bar{u}(z) = \bar{u}_{ref} \cdot \left( \frac{z}{z_{ref}} \right)^\alpha$$

- Logarithmic profile

$$\bar{u}(z) = \bar{u}_{ref} \cdot \left( \frac{\ln \frac{z}{z_0}}{\ln \frac{z_{ref}}{z_0}} \right)$$

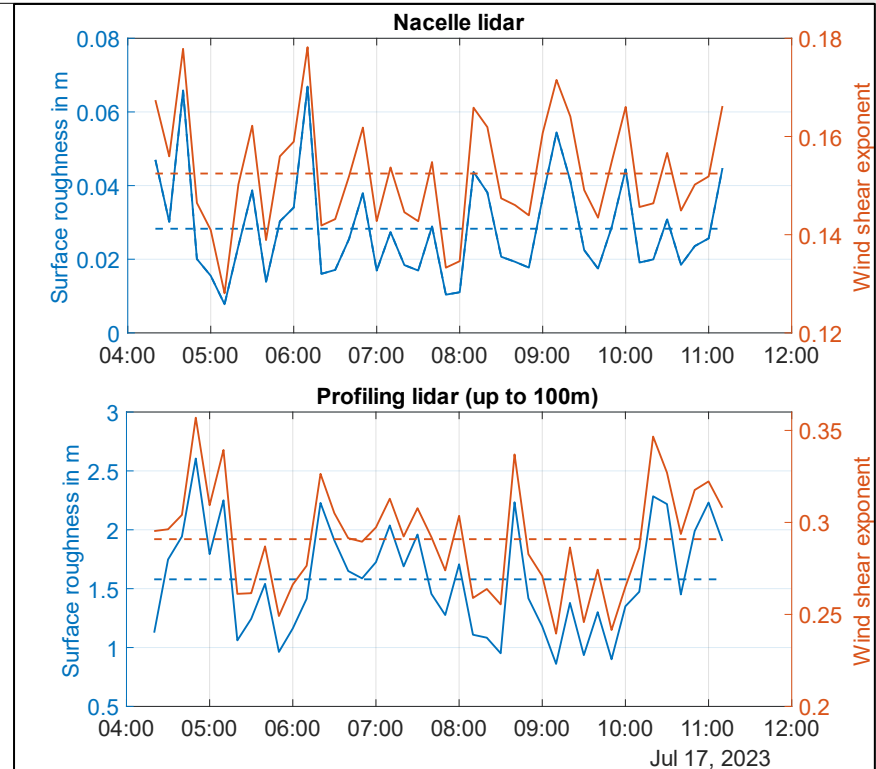
$\bar{u}(z)$  Wind speed at height  $z$   
 $\bar{u}_{ref}(z)$  Wind speed at reference height  $z_{ref}$   
 $\alpha$  Wind shear exponent  
 $z_0$  Surface roughness



# Fitting of standard wind profiles

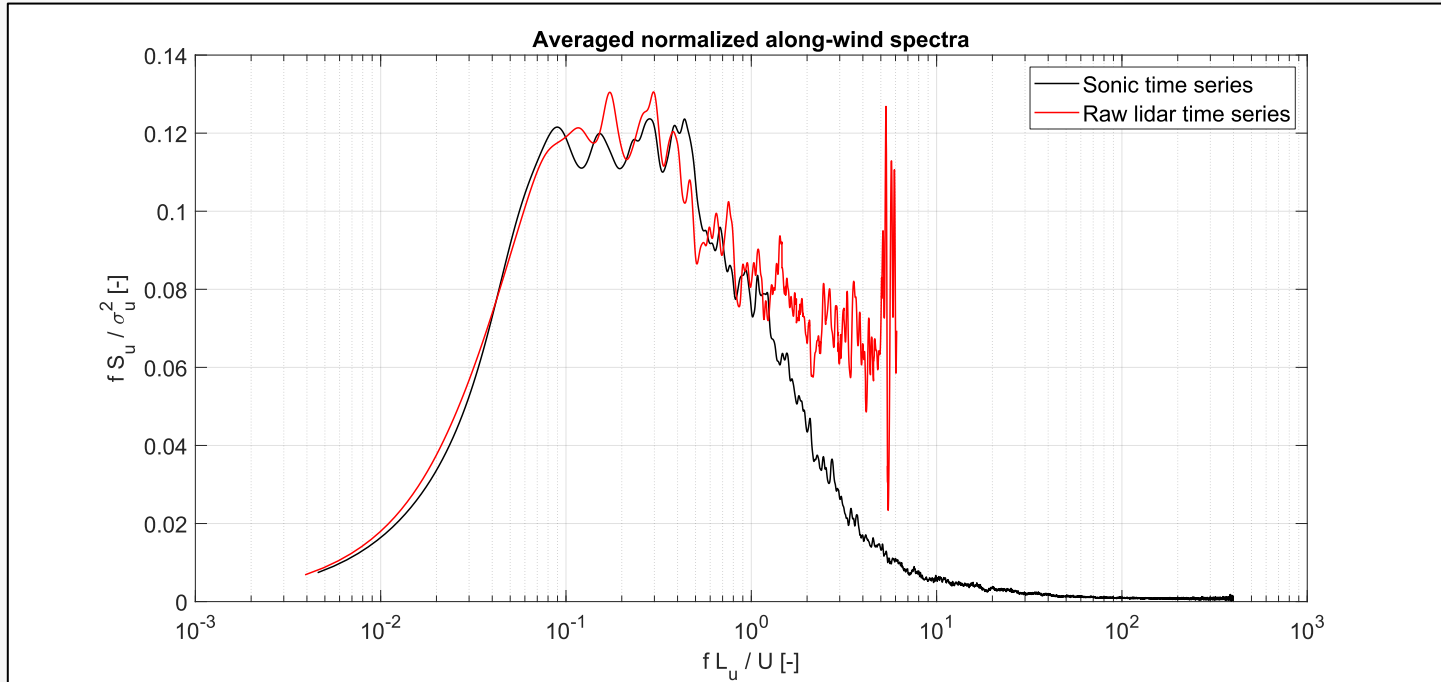
- Nacelle lidar:
  - $z_0 = 0.01 \dots 0.07$  m
  - $\alpha = 0.13 \dots 0.18$
- Profiler:
  - $z_0 = 1 \dots 2.5$  m
  - $\alpha = 0.24 \dots 0.36$
- Literature values:

Type of terrain	Surface roughness in m	Wind shear exponent
Mown grass	0.001 ... 0.01	
Nacelle lidar	Low grass	0.01 ... 0.04
	High grass	0.04 ... 0.1
Forest and woodland	0.1 ... 1	0.13
Profiler	Built up area, suburb	0.19
	City	1 ... 2
		0.32



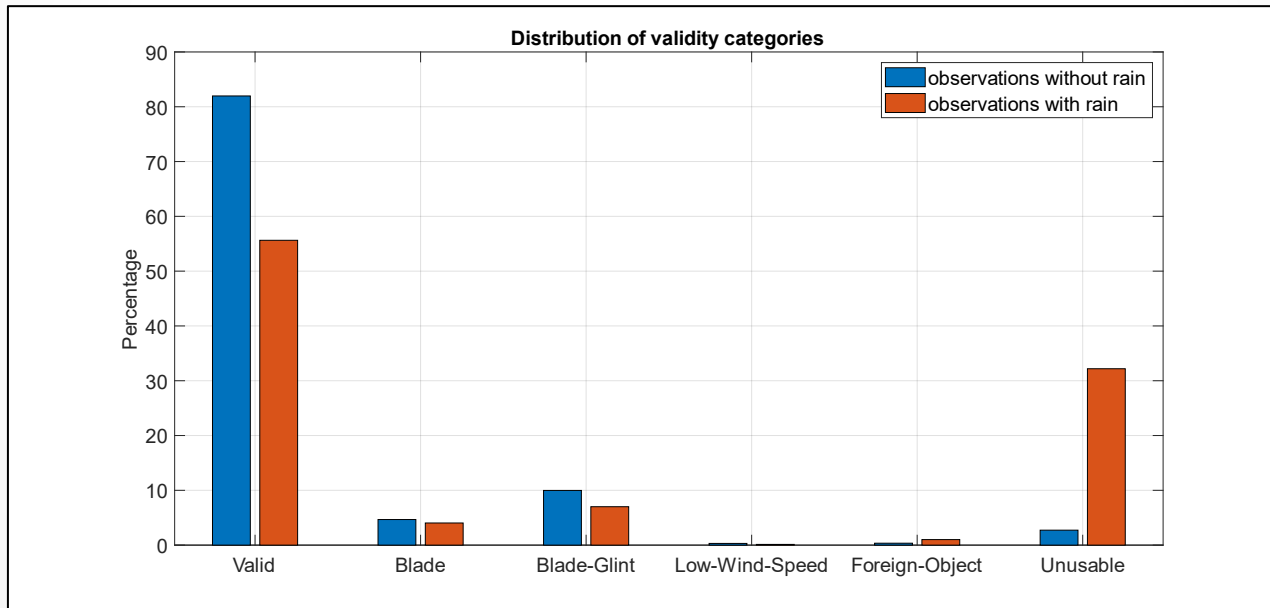


# Spectral estimates

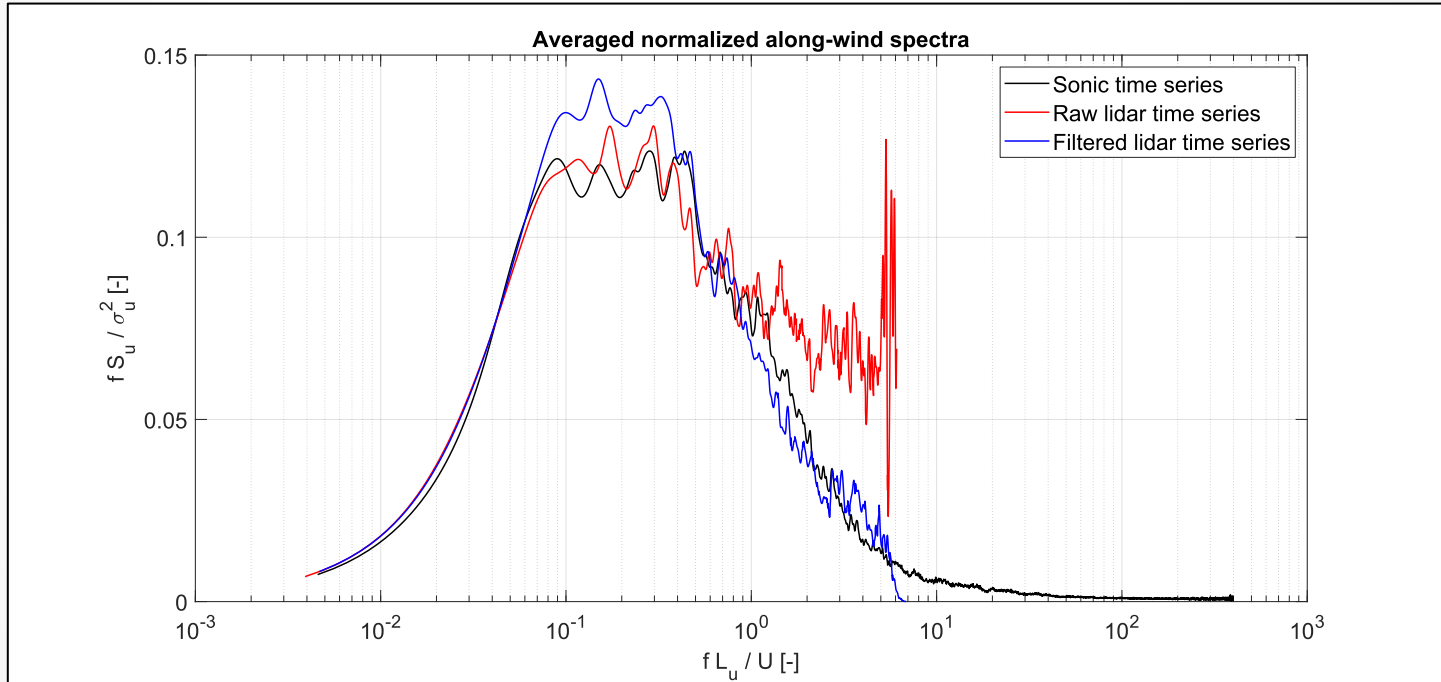


# Spectral estimates

- Large share of data flagged as “unusable”



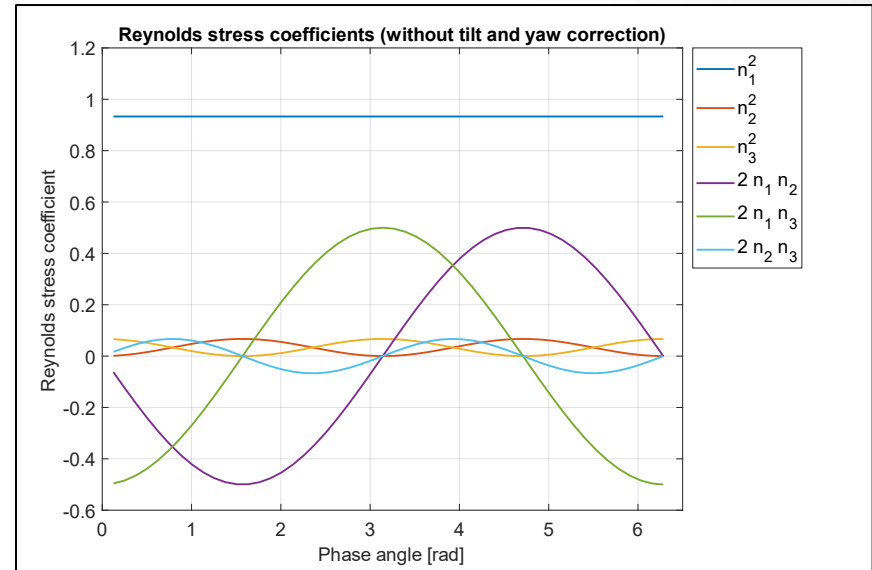
# Spectral estimates



# Estimation of Reynolds stresses

$$\sigma_{v_r}^2 = \sigma_u^2 n_1^2 + \sigma_v^2 n_2^2 + \sigma_w^2 n_3^2 - \langle u'v' \rangle 2 n_1 n_2 - \langle u'w' \rangle 2 n_1 n_3 + \langle v'w' \rangle 2 n_2 n_3$$

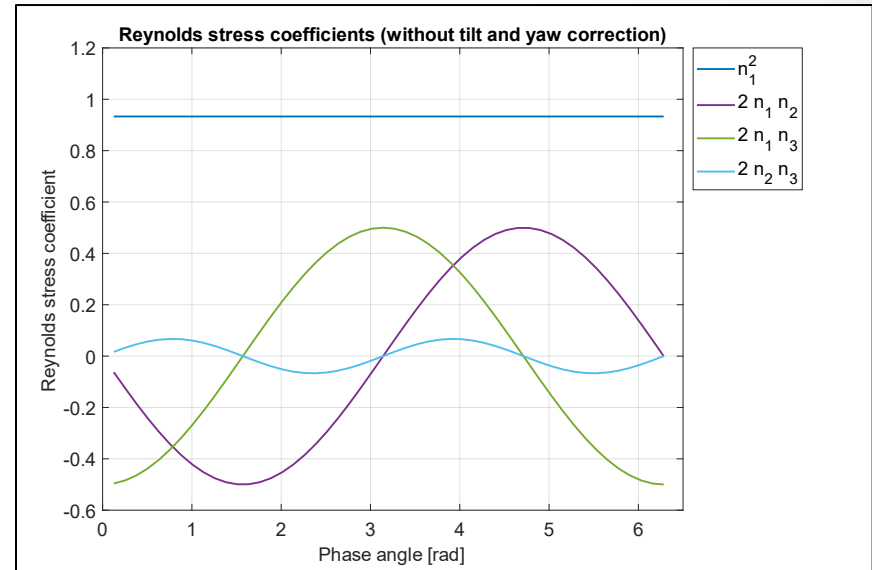
- fitting procedure is poorly conditioned in case of lidars with a single opening angle



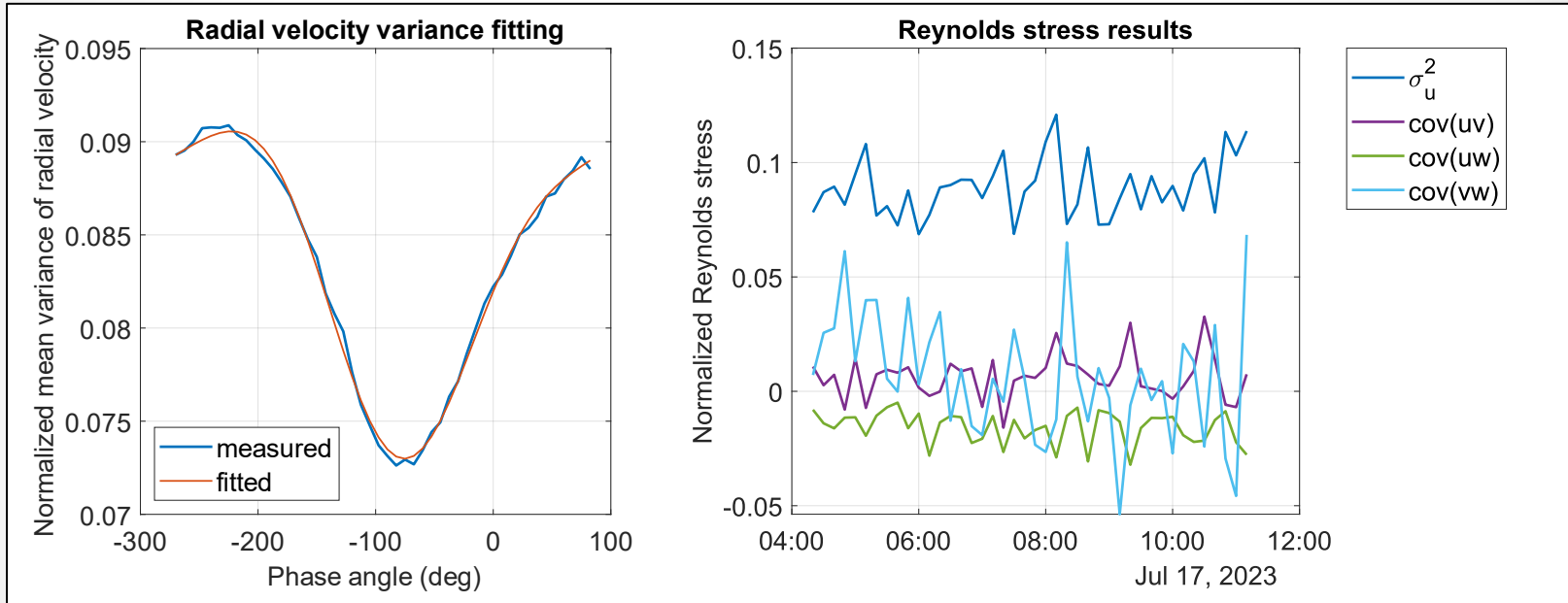
# Estimation of Reynolds stresses

$$\sigma_{v_r}^2 = \sigma_u^2 n_1^2 - \langle u'v' \rangle 2 n_1 n_2 - \langle u'w' \rangle 2 n_1 n_3 + \langle v'w' \rangle 2 n_2 n_3$$

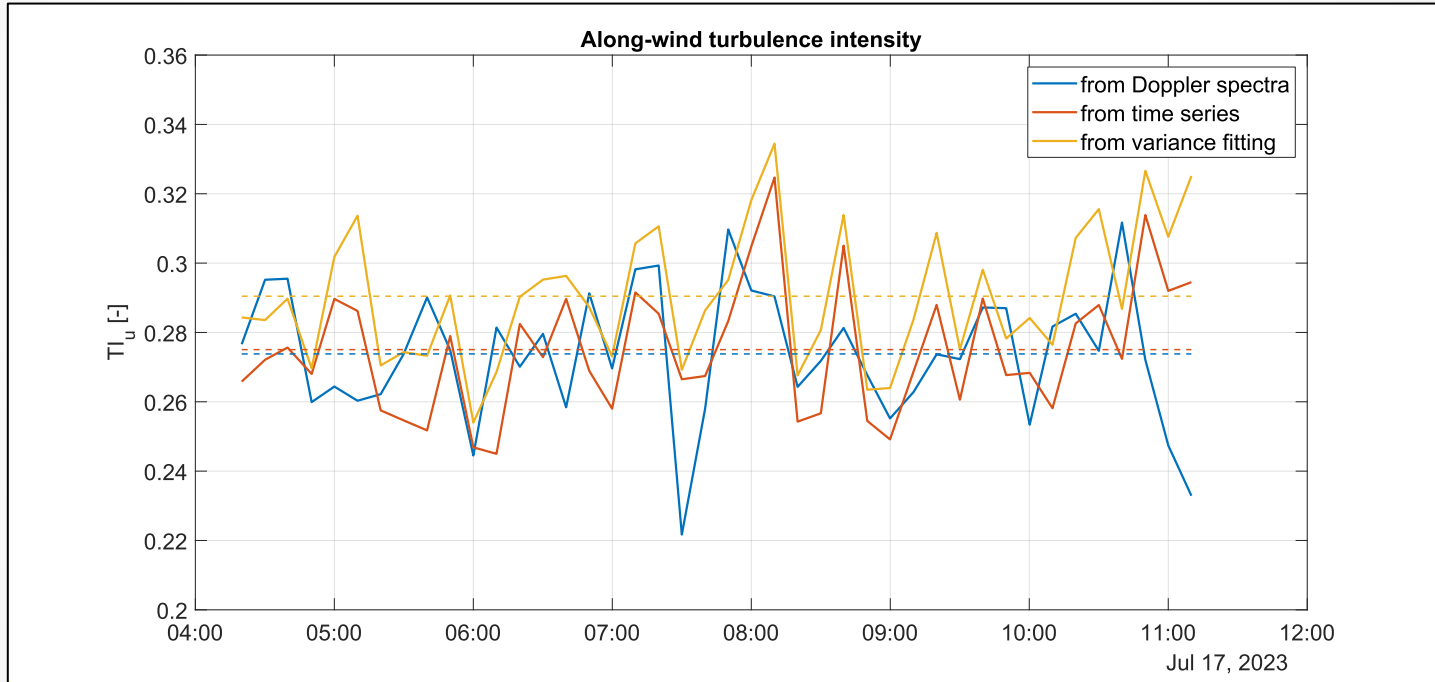
- simplified estimate of  $\sigma_u^2$  (as well as  $\langle u'v' \rangle$ ,  $\langle u'w' \rangle$  and  $\langle v'w' \rangle$ ) by neglecting the terms  $\sigma_v^2 n_2^2$  &  $\sigma_w^2 n_3^2$



# Estimation of Reynolds stresses



# Turbulence intensity estimates



# Conclusion

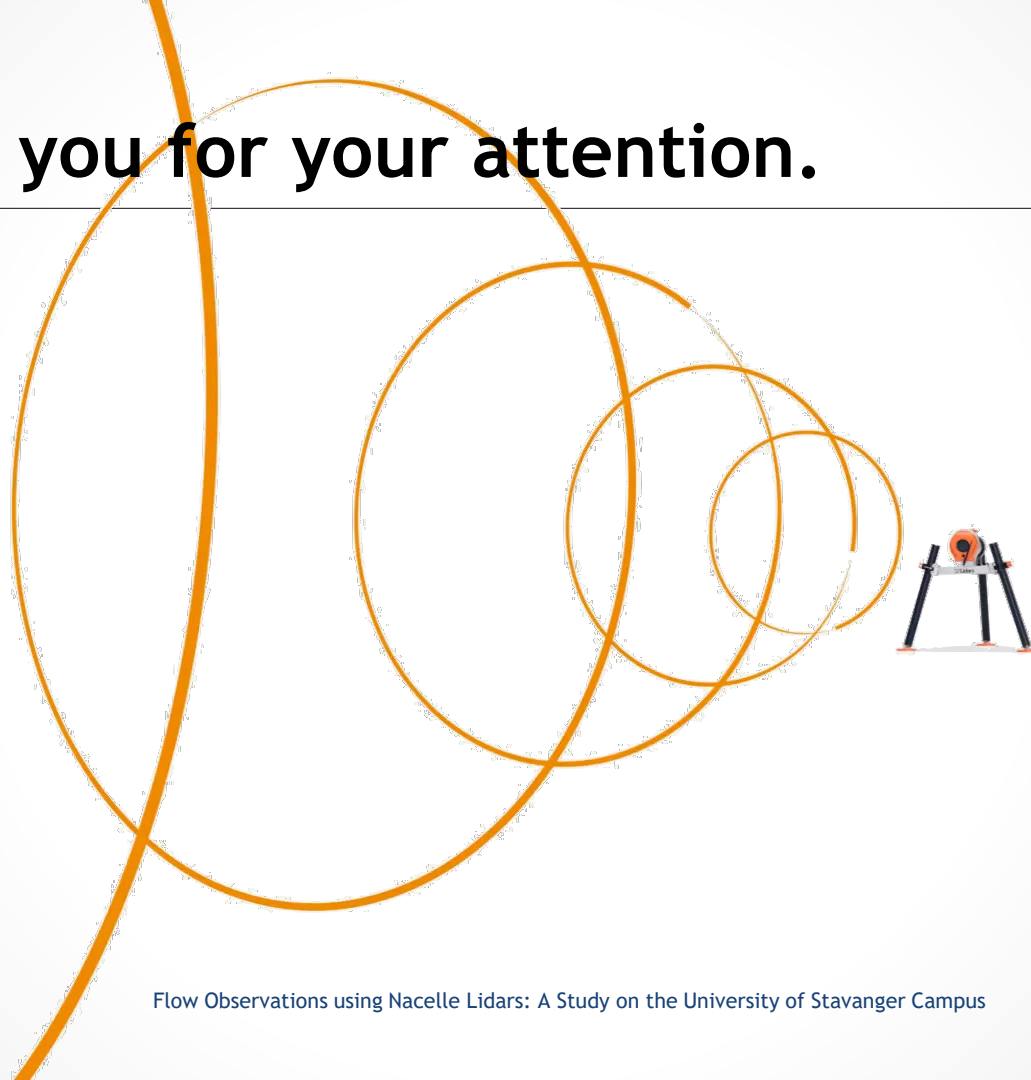
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- 2 horizontal lidars (ZXTM) and 1 profiler (ZX300) deployed on the UiS campus, in an urban environment
- The 3 lidars give insights on:
  - Flow interference with buildings
  - Wind profile
  - Surface roughness estimates
- The horizontal lidars provide:
  - Line of sight time-series in 50 points on the scanning circle, at 1 Hz in each point
  - Time-series of the along-wind turbulence from the data in the horizontal plane
  - Turbulence characteristics in terms of:
    - Reduced Reynolds stress tensor including turbulence intensity
    - Radial and along-wind turbulence spectra
  - Influence of rain on the data quality identified and accounted for



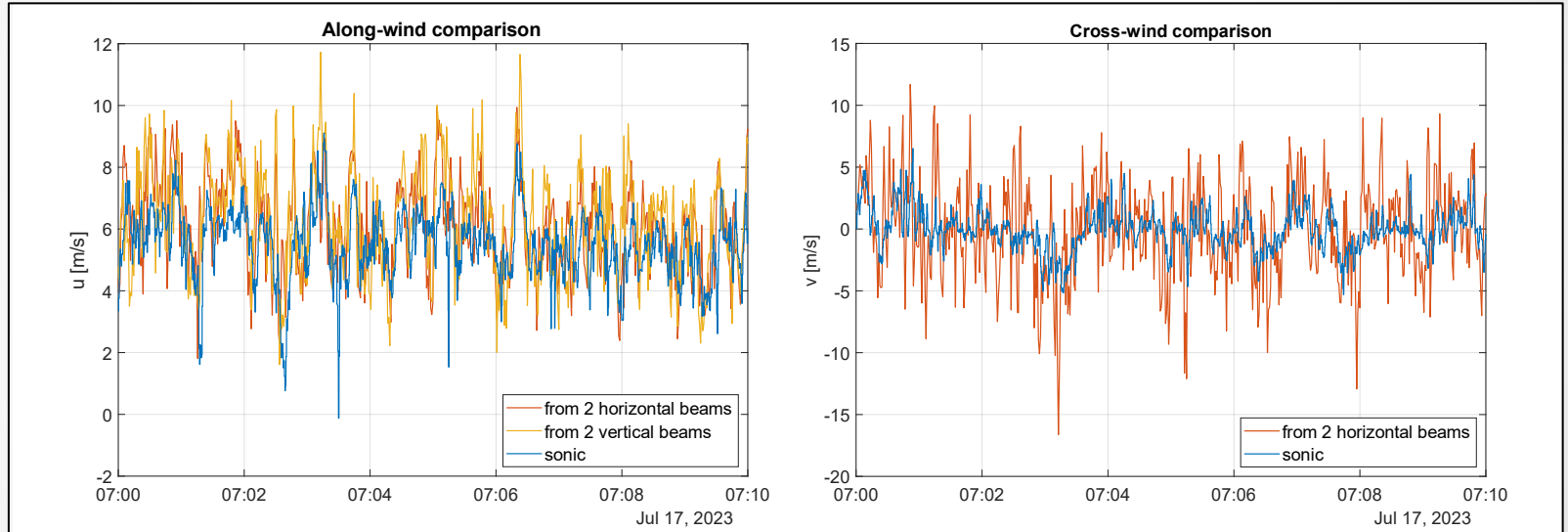
# Thank you for your attention.

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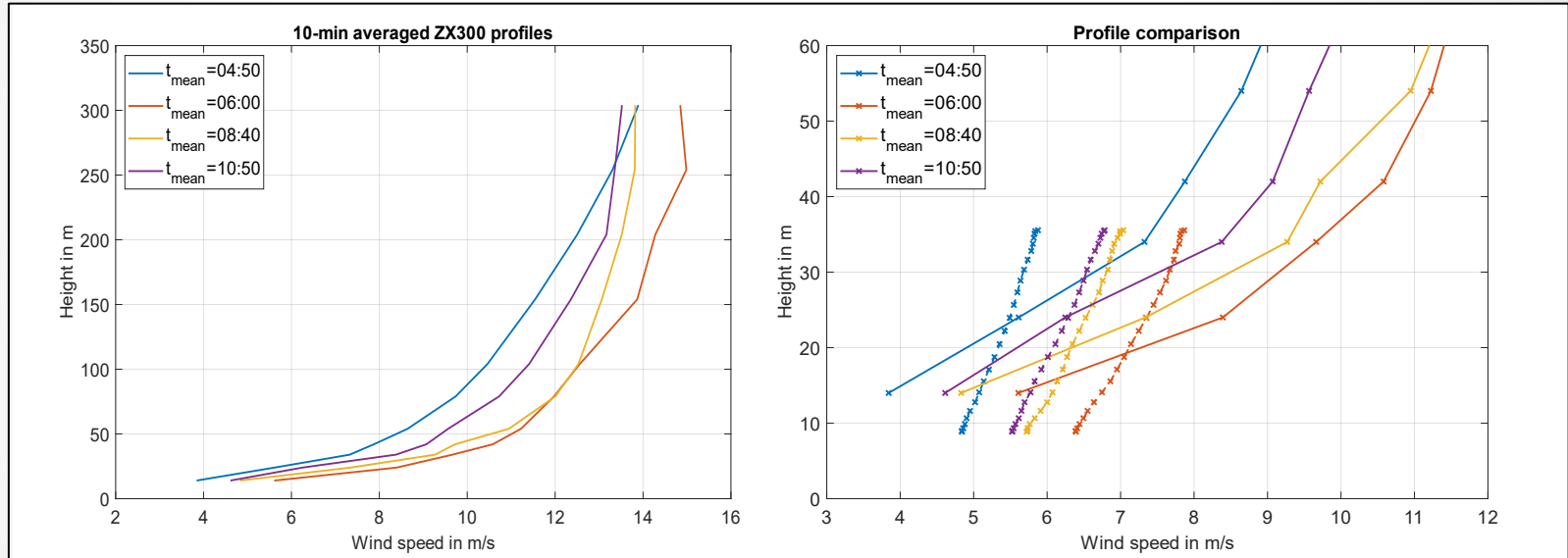




# Wind speed comparison



# Wind profiles from profiling lidar

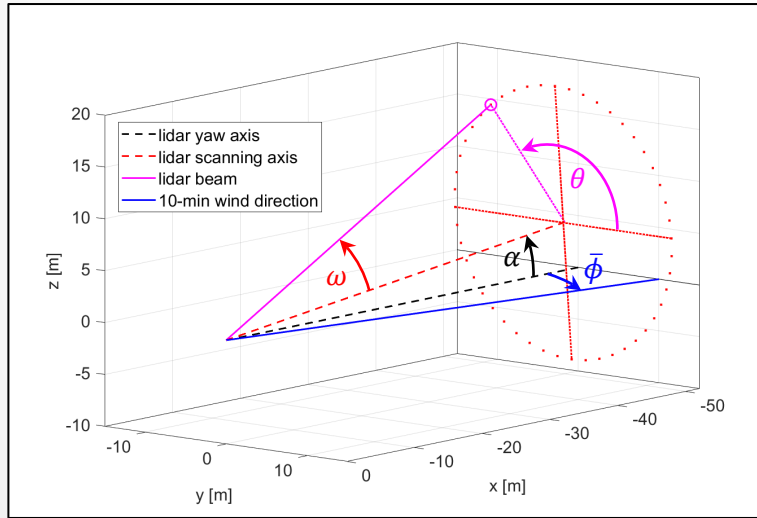


- solid lines: profiling lidar
- dashed lines: nacelle lidar

# Estimation of Reynolds stresses

- Unit vector:

$$n(\theta) = [-\cos \omega \quad \cos \theta \sin \omega \quad \sin \theta \sin \omega] \cdot \underbrace{\begin{bmatrix} \cos \alpha & 0 & -\sin \alpha \\ 0 & 1 & 0 \\ \sin \alpha & 0 & \cos \alpha \end{bmatrix}}_{\text{tilt correction}} \cdot \underbrace{\begin{bmatrix} \cos \phi & \sin \phi & 0 \\ -\sin \phi & \cos \phi & 0 \\ 0 & 0 & 1 \end{bmatrix}}_{\text{yaw correction}}$$



$\omega$  half cone opening angle  
 $\alpha$  tilt angle  
 $\phi$  yaw error  
 $\theta$  scanning point phase angle

# Estimation of Reynolds stresses

- Radial velocity:

$$v_r = u n_1 + v n_2 + w n_3$$

- Radial velocity variance:

$$\sigma_{v_r}^2 = \sigma_u^2 n_1^2 + \sigma_v^2 n_2^2 + \sigma_w^2 n_3^2 - 2\langle u'v' \rangle n_1 n_2 - 2\langle u'w' \rangle n_1 n_3 + 2\langle v'w' \rangle n_2 n_3$$

- Reynolds stress tensor:

$$\mathbf{R} = \begin{bmatrix} \sigma_u^2 & \langle u'v' \rangle & \langle u'w' \rangle \\ \langle v'u' \rangle & \sigma_v^2 & \langle v'w' \rangle \\ \langle w'u' \rangle & \langle w'v' \rangle & \sigma_w^2 \end{bmatrix}$$