

Data-efficient optimisation of wind farms providing secondary frequency regulation with Bayesian optimisation

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Motivation

- Advanced model predictive controllers for wind farm control can be beneficial as it allows for constraints and multi-objective control objectives.
 - However, tuning the resulting predictive controller is hard in practice as the closed-loop solution is usually not known or cannot be analytically derived [1].
 - Recent advances in Bayesian optimisation show promise as an efficient black-box optimisation tool for even high-dimensional optimisation problems [2].
- Given these premises we propose a controller auto-tuning strategy based on
1. Data-efficient Bayesian optimisation for single- and multi-objective optimisation of closed-loop controllers.
 2. Leveraging high-dimensional Bayesian optimisation for handling many tuning parameters in wind farm controllers that provide secondary frequency regulation.

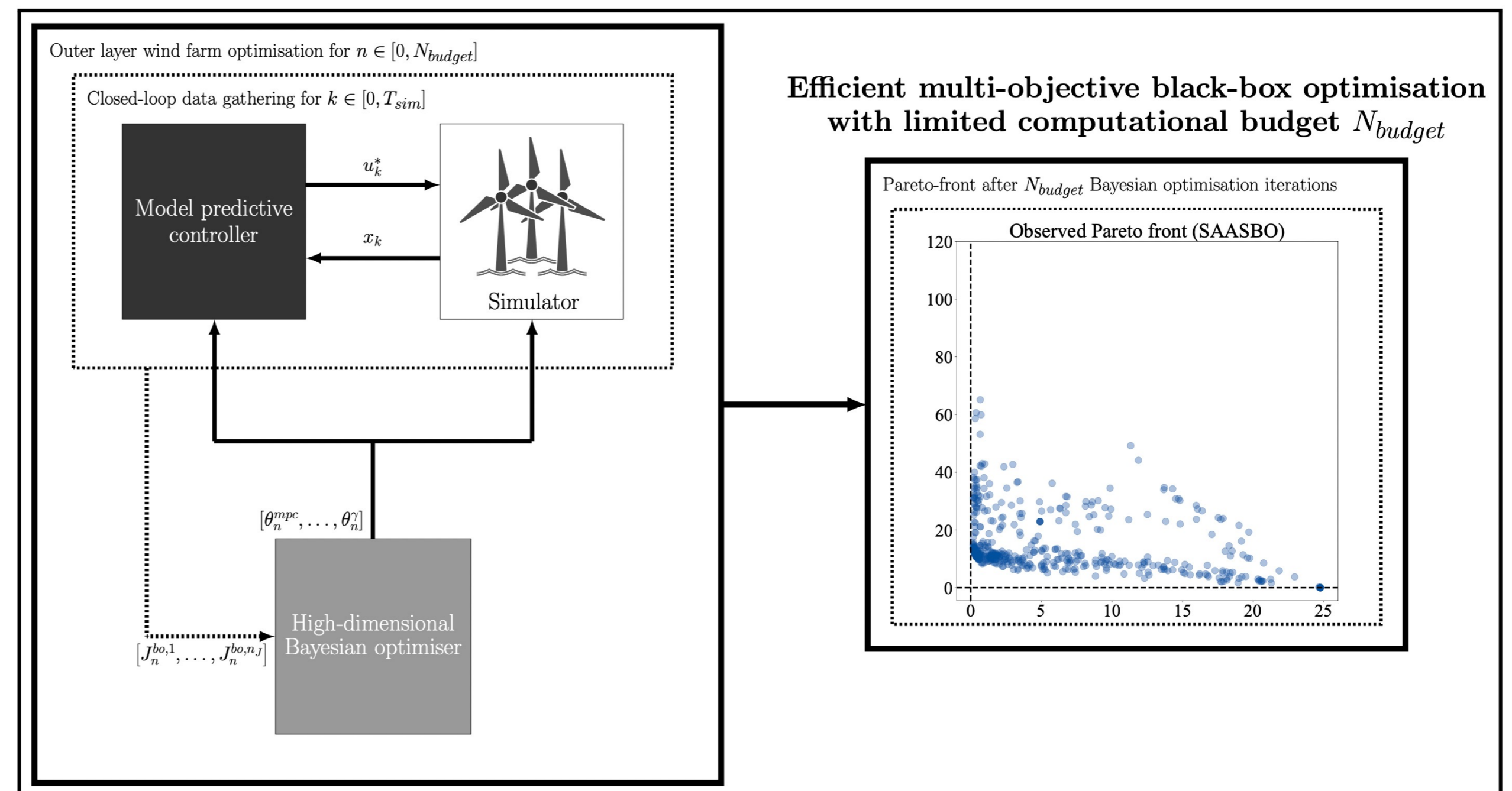


Fig. 1: A schematic of the proposed method for optimising constrained closed-loop wind farm systems providing secondary frequency regulation with model predictive control. By collecting limited samples of the closed-loop costs J for the current choice of closed-loop system specific parameters θ , Pareto-optimal θ can be approximated despite limited computational budget.

Idea: Bayesian optimisation for data-efficient auto-tuning of controllers

1. Run closed-loop experiments with a given controller design/configuration θ to gather closed-loop performance measures y , for example tracking or dynamic loading.
2. Based on previous data, train a Gaussian process for each performance measure to model the closed-loop interactions between current controller and system.
3. Iteratively, based on the trained Gaussian process, compute the posterior to derive the next search space based on an acquisition function.

1 $\dot{x}(t) = f(x(t), u^*(x(t), P^{\text{ref}}, \theta^{\text{MPC}}), p(t), w(t), \theta^{\text{WF}}) dt$

2 $y = J^{\text{cl}}(z^{\text{cl}}(\theta, \mathcal{W})) + \epsilon \sim \text{GP}(m(\theta), k(\theta, \theta'), \psi)$

3 $\theta^{*,\text{pareto}} = \arg \min_{\theta} J^{\text{cl}}(z^{\text{cl}}(\theta, \mathcal{W}))$

1. Based on a simulator or real-life setup, apply the controller with some current design parameters θ .
 - θ can encompass both controller tuning constants but also binary decisions such as whether to use a model predictive controller or PID.
2. Collect closed-loop performance measure y .
 - When using model predictive controller, plant/model mismatch is common. The resulting input is thus sub-optimal and the closed-loop consequence of applying the controller is different from the open-loop calculations.

- Based on each performance measure y , train a probabilistic surrogate model (commonly a Gaussian process).

- Leverage the posterior of the probabilistic surrogate model to estimate the next θ until the optimal θ is estimated with an acquisition function for balancing exploitation vs exploration.

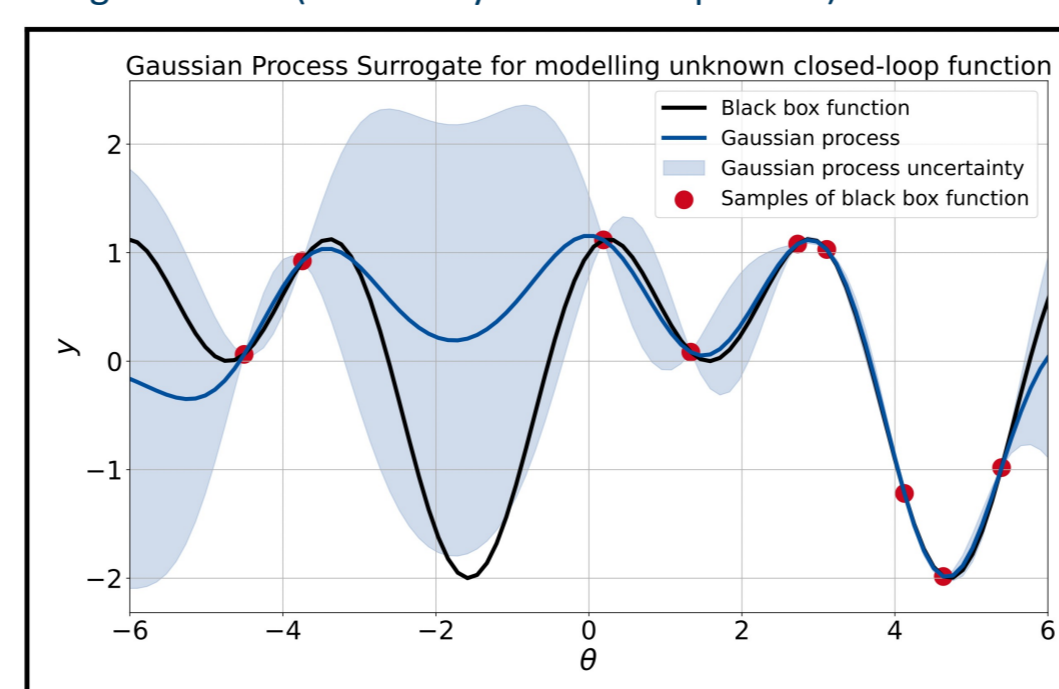


Fig. 2: Example 1d Gaussian model of y given some samples of θ .

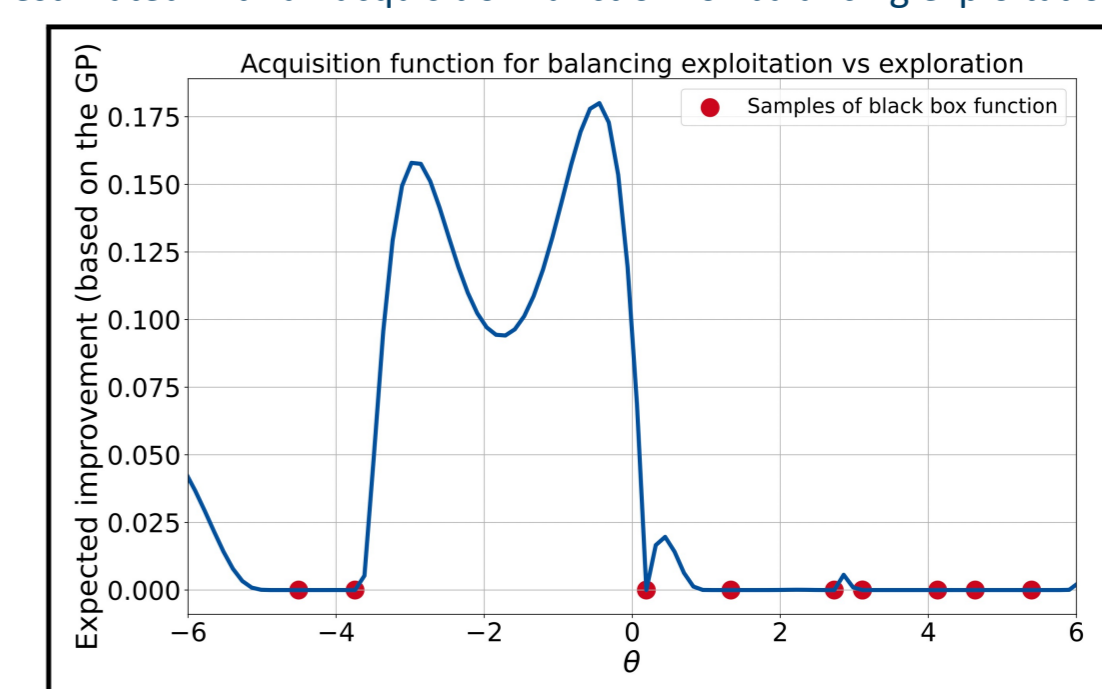


Fig. 3: Example plot of 1d acquisition function (given the GP from Fig. 2.)

High-dimensional Multi-objective case study – tracking and dynamic loading

- Based on a model predictive controller from [3] with 28 tuneable parameters, the proposed method is validated in simulations using WFSim [4].
- The performance measures that is considered is **tracking** and **dynamic loading** with a computational budget for Bayesian optimisation of 100 with 5 replicates.
- From closed-loop experiments, Pareto fronts can be estimated to help some operator to decide on the optimal controller parameterisation with no prior knowledge.
- Utilising sparse-axis aligned subspaces (SAAS) priors improve the results with the notion of **automatic relevance** (deciding the importance on the go from data).
- Higher relevance results in lower values in the lengthscales ψ in the Gaussian process.
- Results in an improved Pareto front.

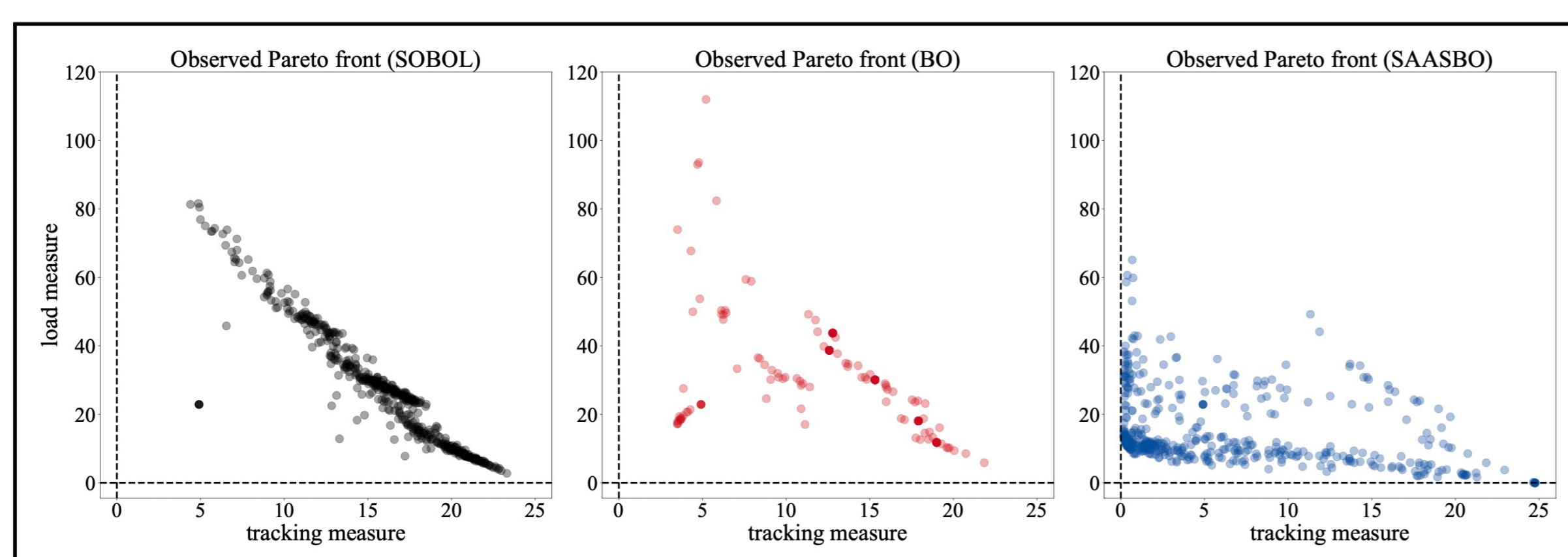


Fig. 4: Scatterplots of the resulting Pareto-front for optimising cumulative tracking and dynamic load.

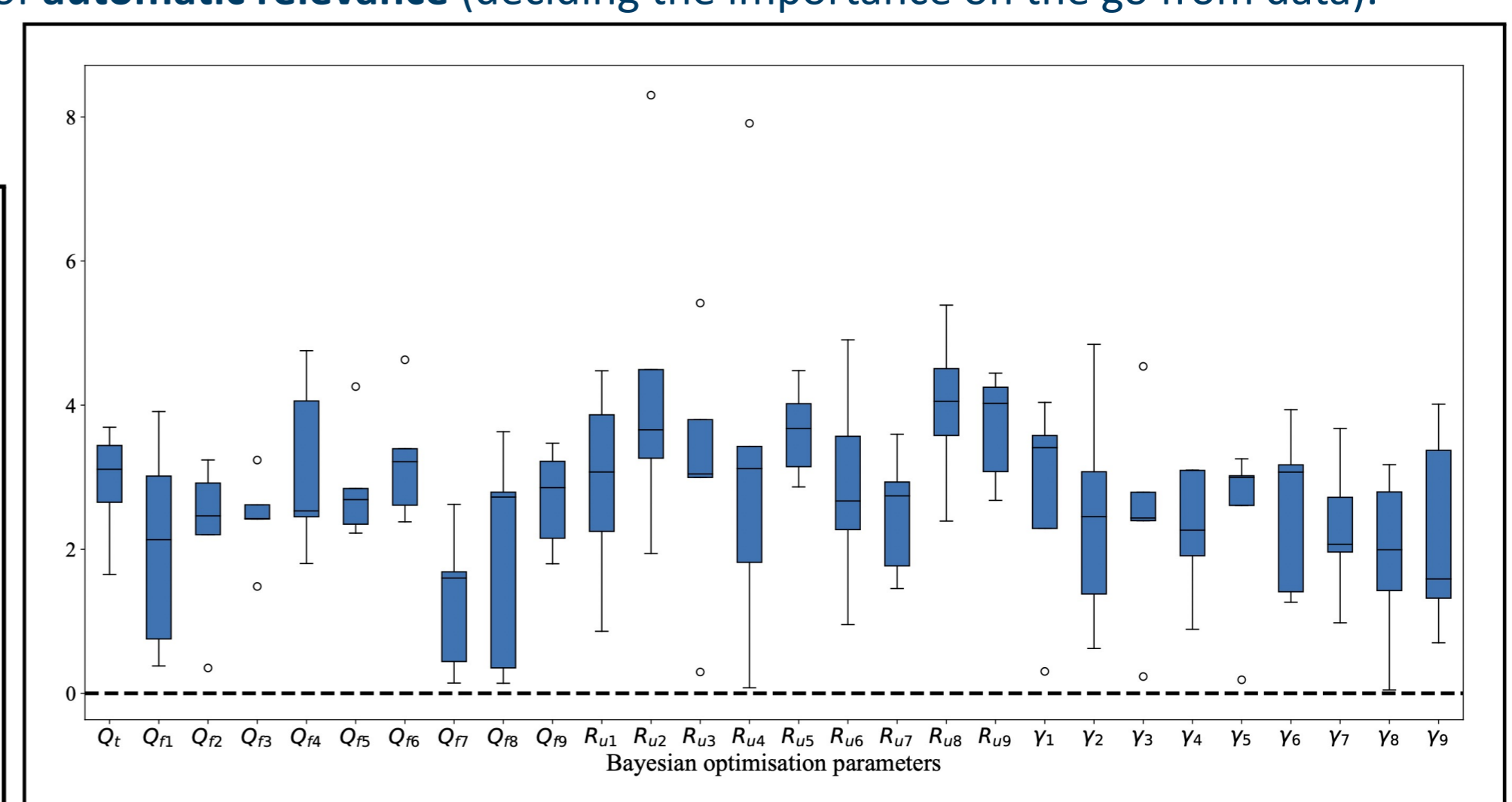


Fig. 5: Boxplots of the resulting lengthscales in the SAAS priors for deriving automatic relevance.

References

- [1] J.A. Paulson et al, **A Tutorial on Derivative-Free Policy Learning Methods for Interpretable Controller Representations**, in American Control Conference, 2023
- [2] D. Eriksson et al, **High-Dimensional Bayesian Optimization with Sparse Axis-Aligned Subspaces**, in Proceedings of the Thirty-Seventh Conference on Uncertainty in Artificial Intelligence, 2021.
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Acknowledgement

This research is being conducted with support from the LowEmission Research Centre (www.lowemission.no) through PETROSENTER LowEmission (project code 296207), the American-Scandinavian Foundation and the Norway-America Association.

Special acknowledgement goes to Kimberly Chan from UC Berkeley for helping with implementation of the different methods.