

# Kalman estimation of position and velocity for ReaTHM testing applications

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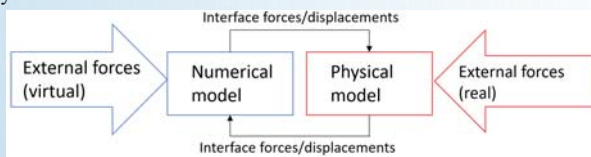
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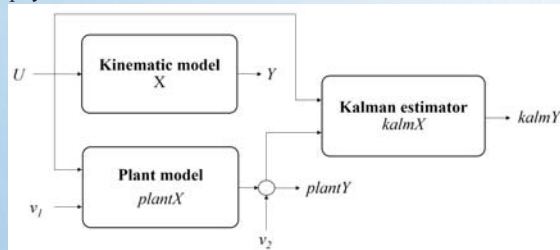
## Introduction

- Model testing can reduce the costs of offshore wind turbines (OWTs).
- Real-time hybrid model (ReaTHM) testing provides solution to challenges related to such tests.
- The system is divided into physical and numerical substructure.
- State estimator is designed to estimate and filter the positions and velocities of the physical substructure.

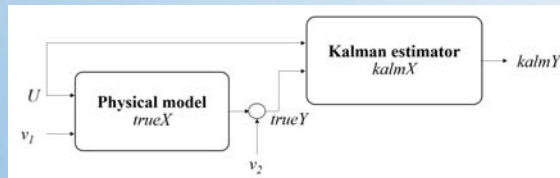


## Numerical Model

Two different versions of the system are designed for tests using virtual and physical data:



Virtual data



Physical data

### Kinematic model

- Can represent the motion of any floating structure in 6-DOF.
- Plant model intended to simulate the physical system is implemented using the same state-space matrices.
- State vector consists of the variables to be estimated.
- Output vector consists of the variables which can be measured.
- System matrices are defined according to Fossen [1].
- Simplified model for tests with SIMA: linear and time-invariant.

### Estimator design

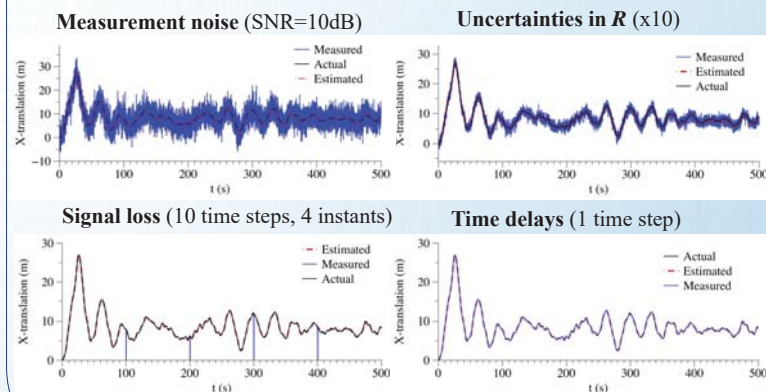
- Kalman estimator chosen since it provides optimal estimates, minimizing the estimation error in the statistical sense.
- Both steady-state and time-varying versions are designed, implemented in MATLAB and tested.

## References

- [1] Fossen T I 2011 *Handbook of Marine Craft Hydrodynamics and Motion Control* (Chichester, UK: John Wiley & Sons, Ltd.)  
 [2] Vilsen S A, Sauder T and Sørensen A J 2017 *Dyn. Coupl. Struct.* **4** 79-92

## Sensitivity analyses using virtual data

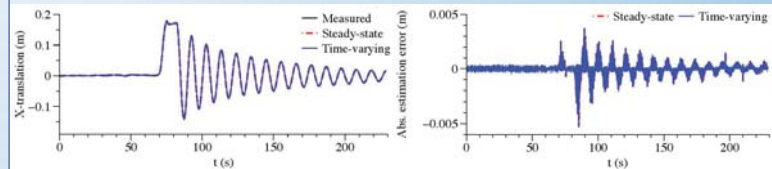
Sensitivity analyses addressing the robustness towards different types of disturbances are performed to identify the limits of the estimator. Time-varying Kalman estimator used for signal loss, otherwise steady-state version is used.



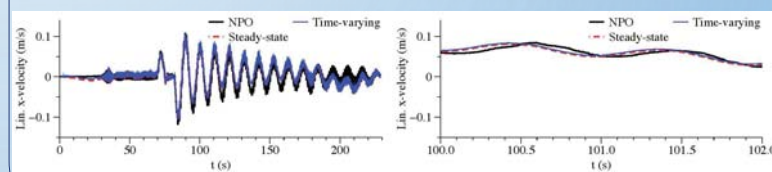
The estimator is robust towards noise, uncertainties, time delays and signal loss.

## Validation of estimator using physical data

Both versions of the Kalman estimator are further tested against the laboratory experiments by Vilsen et al. [2]. Knowledge about delays and inaccuracies in the sensors used is taken into account.



## Comparison of steady-state and time-varying Kalman estimates with physical data



## Comparison of steady-state and time-varying Kalman estimates with NPO

Good results are obtained for both versions of the Kalman estimator.

## Conclusions

- The generic kinematic model developed can recreate the SIMA simulated motions with reasonable accuracy.
- A Kalman estimator providing smooth and accurate position and velocity estimates in 6-DOF is designed, implemented and tested.
- The estimator is proven to be robust towards different types of disturbances.
- The estimator is able to estimate the states with a good accuracy, when compared with physical measurements.
- An improvement from the previously implemented estimators is demonstrated.