

# Assessing the impacts of integrating snowpack error distribution in the management of a hydropower reservoir using Bayesian Stochastic Dynamic Programming (BSDP)



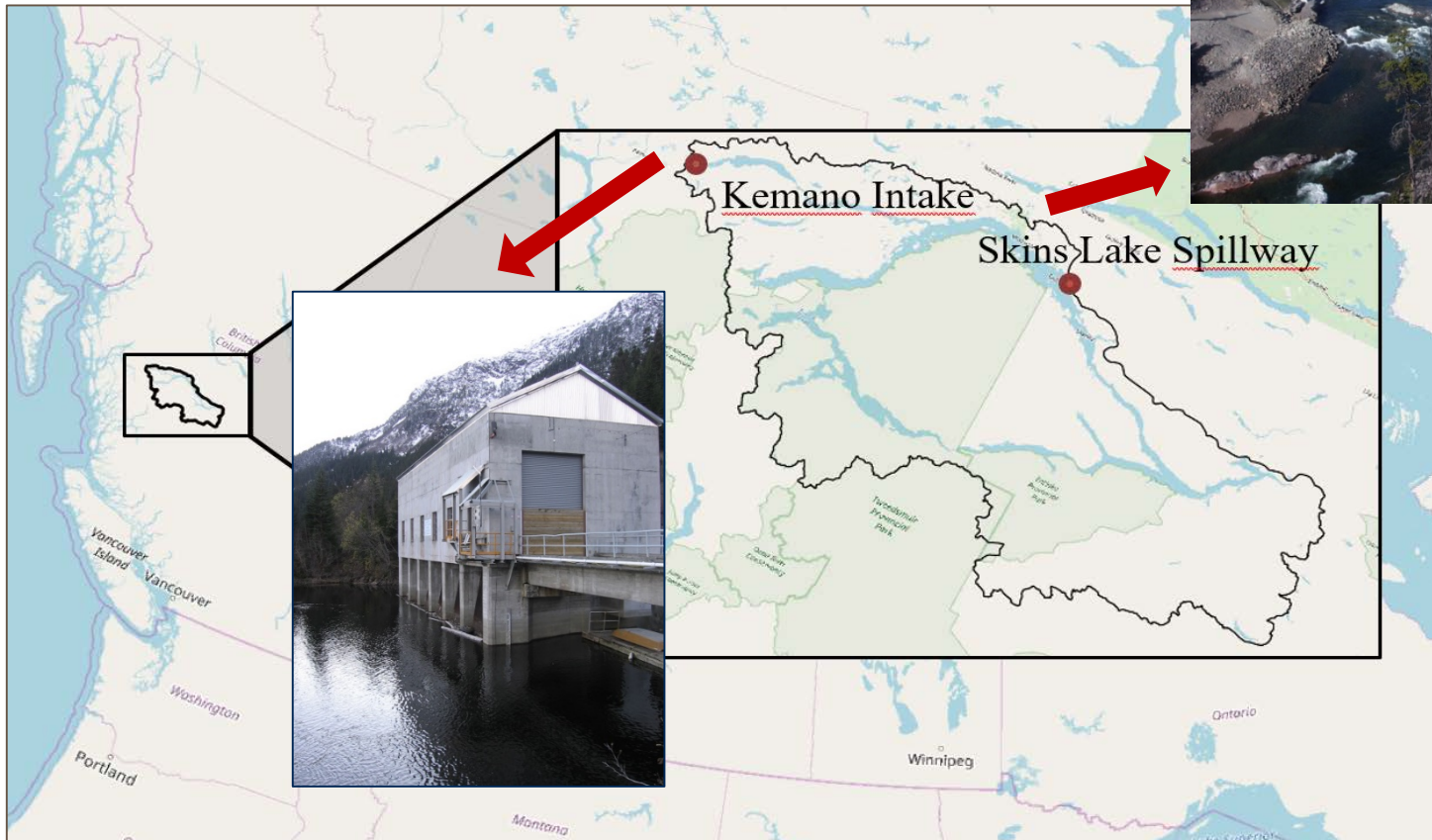
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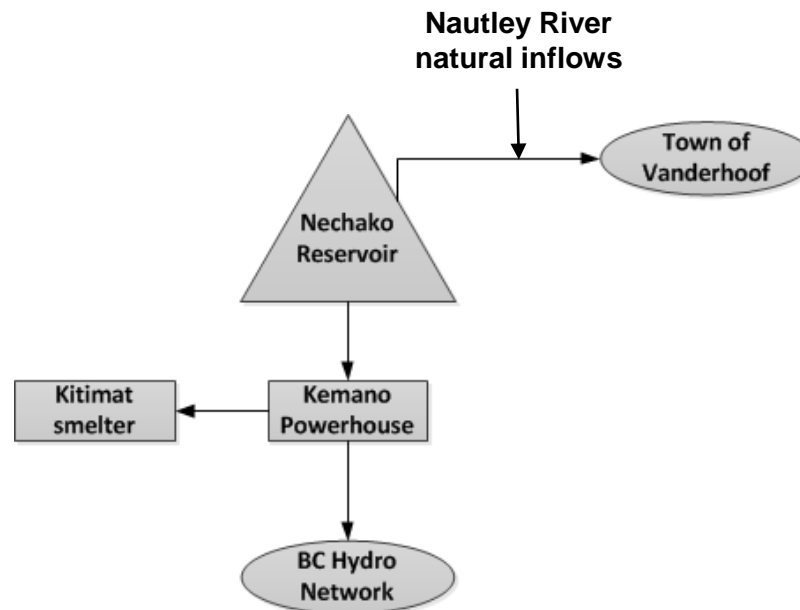
# ÉTS Hydropower System

RioTinto

- > **Kemano Hydropower System in B.C., Canada**
- > 14040 km<sup>2</sup> drainage area
- > Snowmelt-dominated hydrograph



- > **Rio Tinto Kemano System in B.C. Canada**
- > Water release decisions aided by an SDP implementation
- > A hydrological variable representing the water content of the catchment, including Snow-Water Equivalent (SWE), is used as a predictive variable of future inflows in SDP



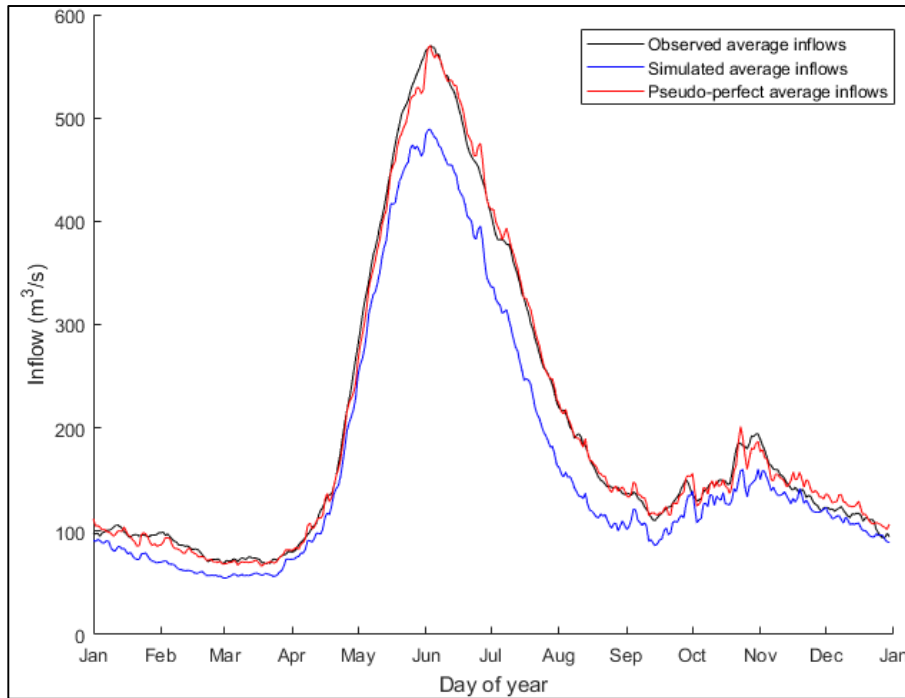
- > Impact of snowmelt is paramount in the management of the hydropower system.
- > High uncertainty around SWE measurements (4 snow pillows, 7 core-sampling sites)
- > Spatial variability of SWE is very high (2000mm precip. in the mountains, 400mm in the plains)

## Objective:

- > Evaluate uncertainty around hydrologic variables (including SWE) and use this information to improve the water release policy in a Stochastic Dynamic Programming Framework

## > Distributed hydrological model (CEQUEAU) – 2 simulations

- (1) Ordinary simulation, using actual measured Precip. and Temp.
- (2) « Pseudo-Perfect » simulation, using fitted Precip. and Temp. time-series to perfectly reproduce inflows;



- > Each simulation also returns state variables, such as SWE
- > We can estimate the bias and uncertainty in the hydrologic variable by comparing both simulations

- > Current Policy given by SDP:

$$\pi_t(s_t, h_t) = \operatorname{argmax}_{u_t} \left\{ \mathbb{E}_{q_t|h_t} \left[ B_t(s_t, u_t, q_t) + \mathbb{E}_{h_{t+1}|h_t} [F_{t+1}(s_{t+1}, h_{t+1})] \right] \right\}$$

- > With the water value function computed as:

$$F_t(s_t, h_t) = \max_{u_t} \left\{ \mathbb{E}_{q_t|h_t} \left[ B_t(s_t, u_t, q_t) + \mathbb{E}_{h_{t+1}|h_t} [F_{t+1}(s_{t+1}, h_{t+1})] \right] \right\}$$

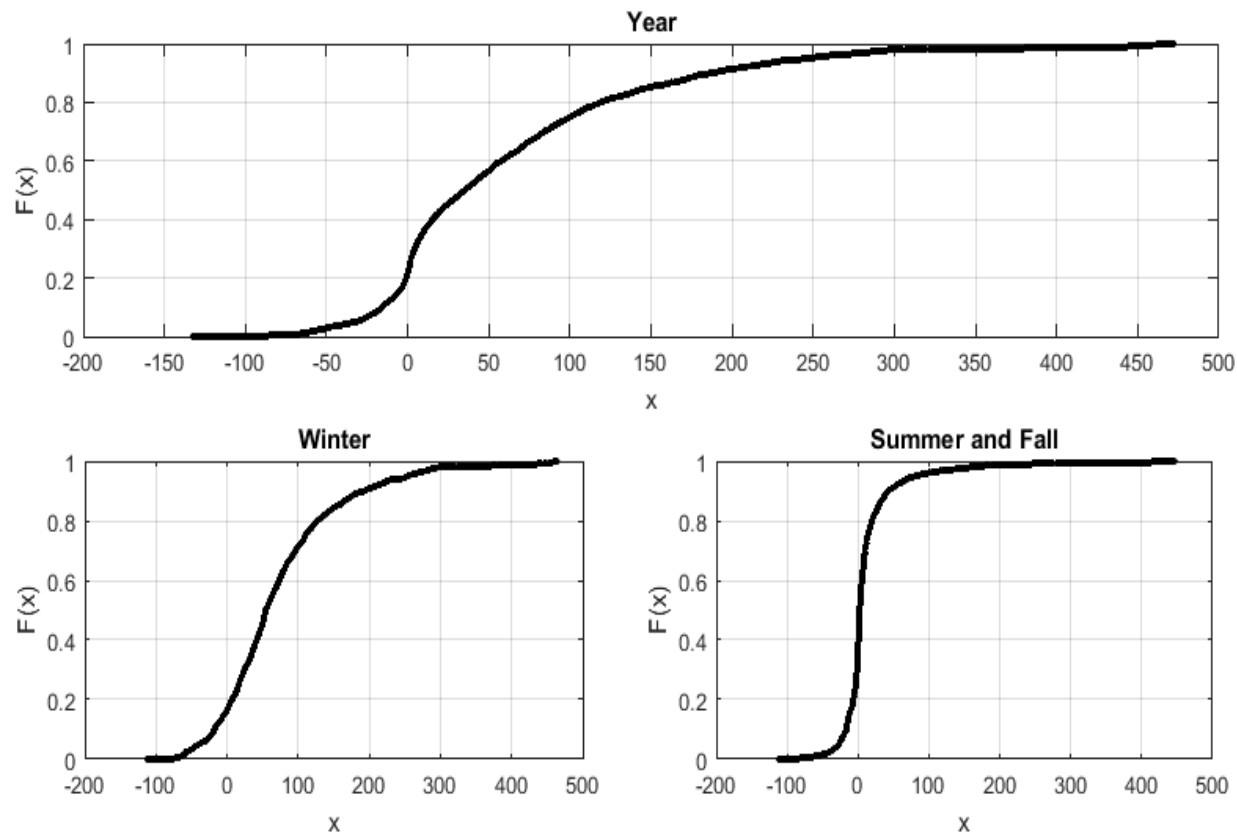
- > However, operationally we do not have perfect values.
- > In operations, we add the error distribution of  $h_t$  in the SDP policy:

$$\pi_t(s_t, h_t) = \operatorname{argmax}_{u_t} \left\{ \mathbb{E}_{h_t|\hat{h}_t} \left[ \mathbb{E}_{q_t|h_t} \left[ B_t(s_t, u_t, q_t) + \mathbb{E}_{h_{t+1}|h_t} [F_{t+1}(s_{t+1}, h_{t+1})] \right] \right] \right\}$$

- > Where the error distribution of  $h_t$  is computed and updated at the end of each season when the pseudo-perfect weather timeseries can be generated.

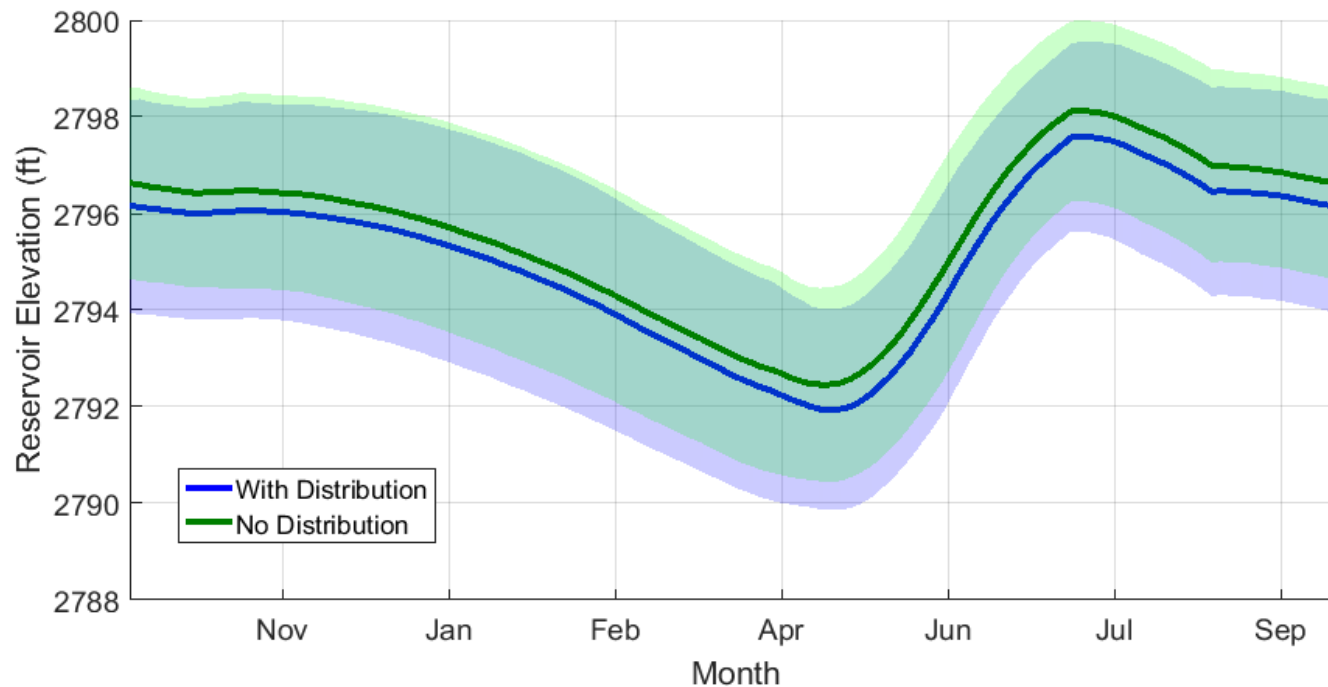
## > Error distribution relative to the season

The hydrological variable also includes soil humidity, which is negligible in winter but becomes important in summer. Units in mm of water.



## > Impact on water management

Hydrological Variable	Avg. Annual Export and Aluminum	Daily Probability of Shortage	Daily Probability of Flooding
Pseudo-perfect Corrected	106.1	6,5%	0,1%
Real, No Distribution	100.0	6,0%	0,5%
Real, With Distribution	103.1	6,0%	0,2%



## Analysis and conclusions

- > BSDP naturally corrects the Hydrologic Variable bias
  - > Lower reservoir level on average: probably due to correction of precipitation undercatch
  - > More efficient generation due to better uncertainty representation
  - > Less flooding, more energy for same shortage risk.
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- > Bayesian SDP has shown to be a promising water resources management tool
  - > Pseudo-perfect simulations can be very valuable to estimate the error distributions (rather than embarking on measurement field trips)

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