

# Modelling start/stop in short-term multimarket hydropower scheduling

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# Background

- Mainly day-ahead trading
  - Increasing share of wind production
  - Increasing integration with rest of Europe
    - Cables
    - Market coupling
  - Expects increasing variability and volumes in short-term markets
    - Intra day
    - Reserves
    - Balancing
- Business opportunities for hydropower producers
  - Changed operating patterns

## Start/stop properties

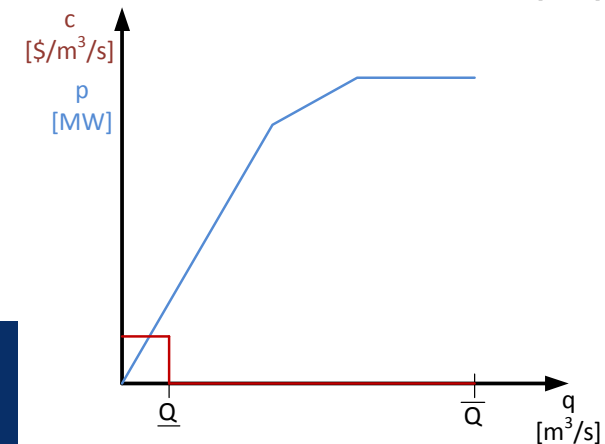
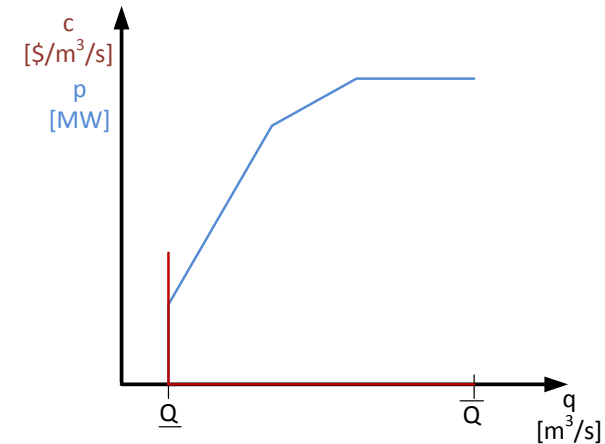
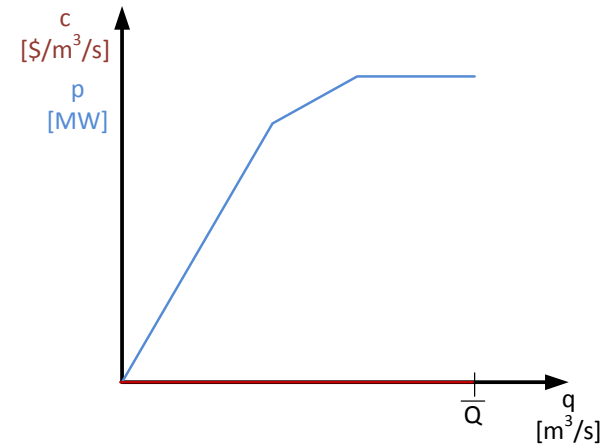
- **Binary – spinning state**
- **Minimum production rate**
- **Start-up cost**
  
- Ramping rate
- Minimum up/down-time
- Shut-down cost
- Down-time dependent start-up cost
- Logical dependencies between generators/pumps

# Start/stop modelling

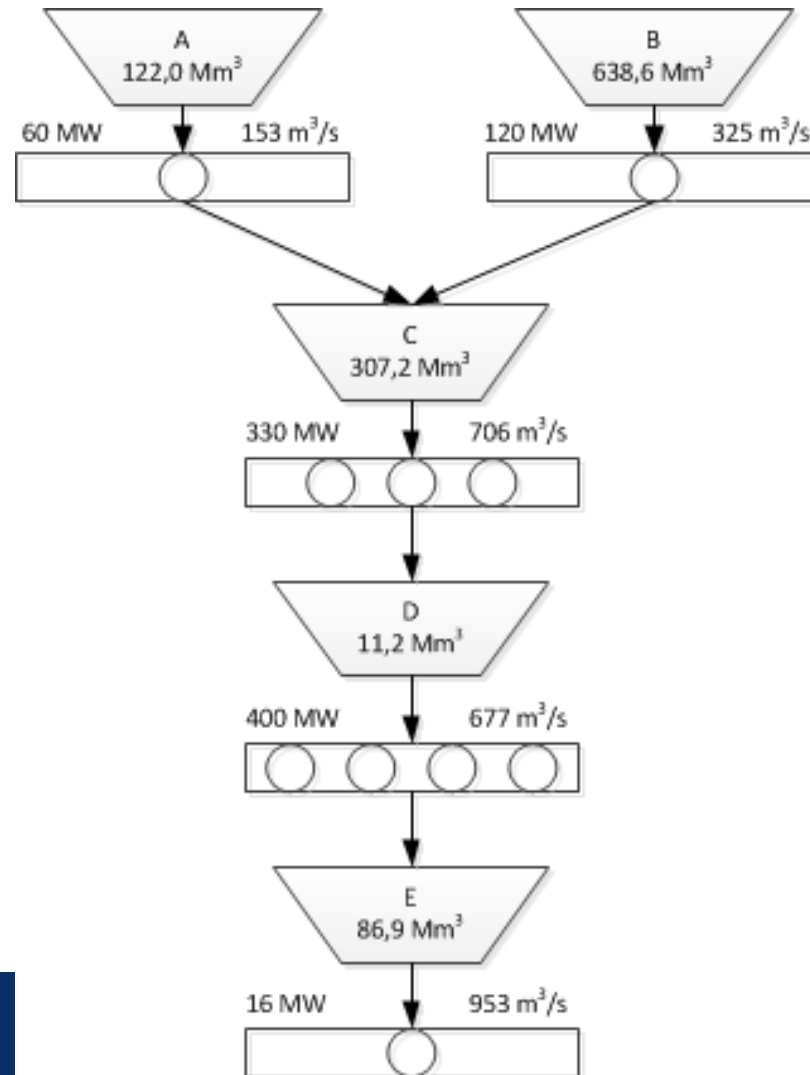
1. No start/stop ("noSS")
  - No minimum production
  - No start-up cost
2. Binary start/stop ("0/1")
3. Linear approximation ("linearSS")
  - Incentive to stay above  $\underline{Q}$

$$\begin{aligned}
 c_t &\geq C(u_t^L - u_{t-1}^L) \\
 Qu_t^L + (\bar{Q} - \underline{Q})u_t^H &= q_t \\
 u_t^L &\geq u_t^H \\
 0 &\leq u_t^L, u_t^H \leq 1
 \end{aligned}$$

Warland&Huuse, 2008

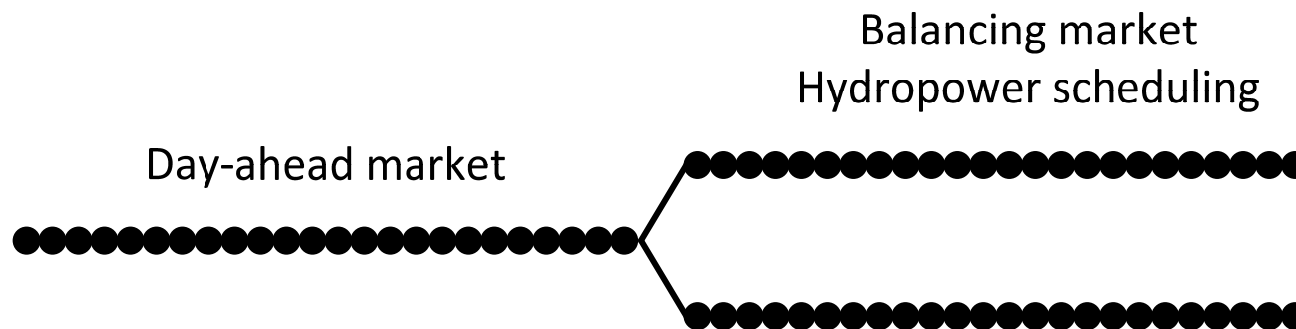


# Test case – a Norwegian water course



# Trade and market modelling

- Day-ahead (DA) and balancing market (BM) by price
- Balancing market
  - Activation given by price difference
    - Day-ahead price > balancing market price => down regulation
    - Day-ahead price < balancing market price => up regulation
- Allocation, no bidding
  - Increasing allocation with increasing price



# Scenario tree generation

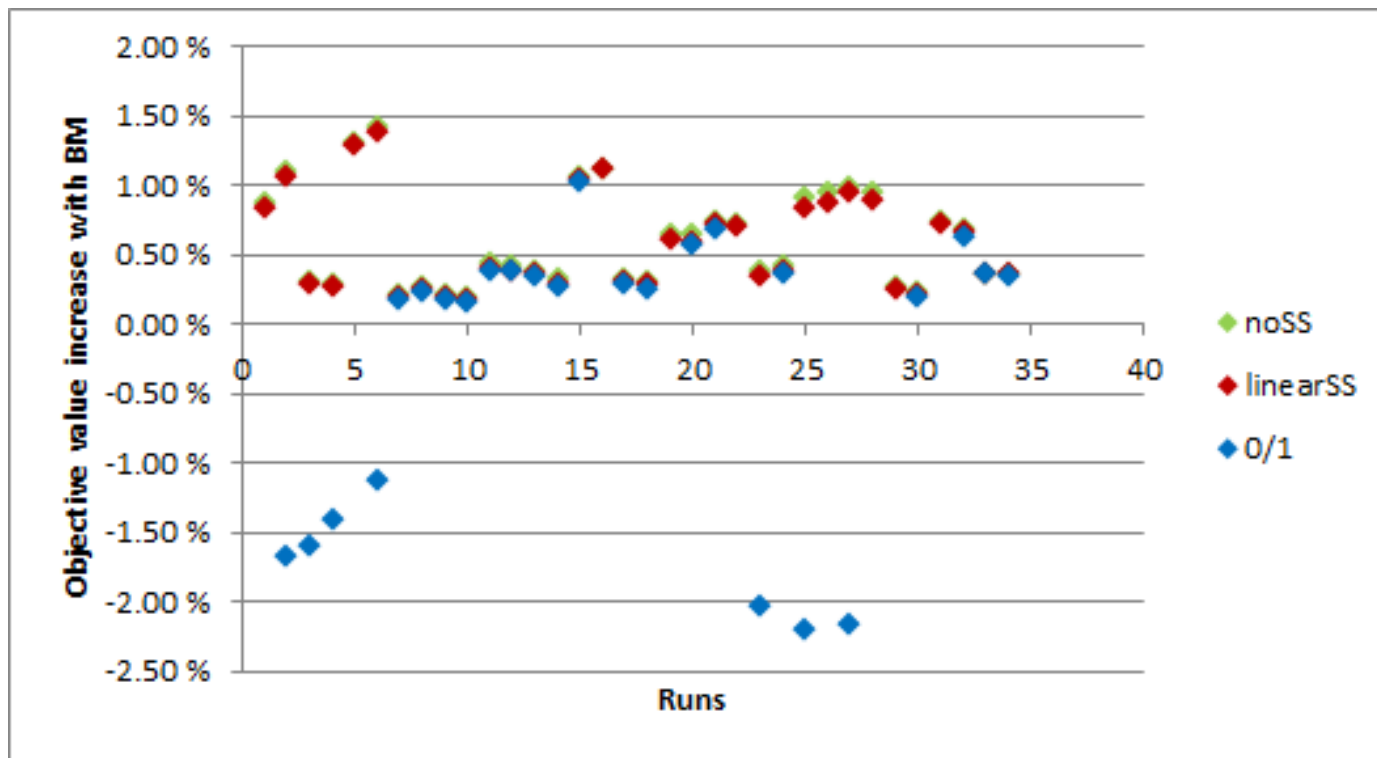
- Highly inspired by Boomsma, Juul & Fleten (2014) in EJOR
- Prices from Nord Pool Spot, 2013-2014, Southern Norway (NO2)
- Time series model
  - Day-ahead price: SARIMA
  - Balancing price: SARIMAX
  - Joint trend and seasonality correction
- Procedure:
  - Sample day-ahead
  - Scenario reduction day-ahead
  - Sample balancing market
  - Scenario reduction balancing market
  - Remove arbitrage possibilities

# Test setup

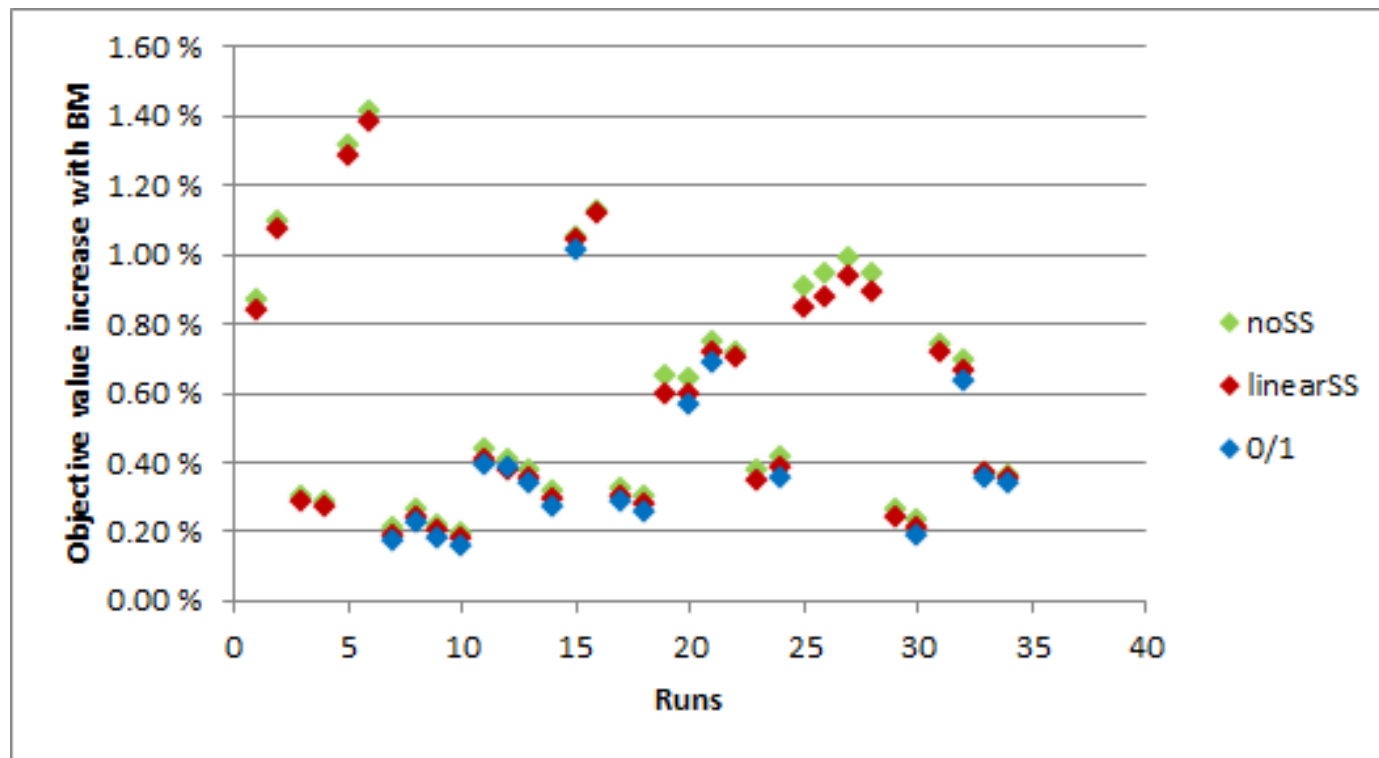
- 34 one-day scenario trees generated
  - 225 scenarios (15 day-ahead x 15 balancing market)
- September/October
- Initial reservoir level: 90%
  
- Compares model run
  - with and without balancing market (+BM vs -BM)
  - with different start/stop modelling



# Value of Balancing Market (BM)



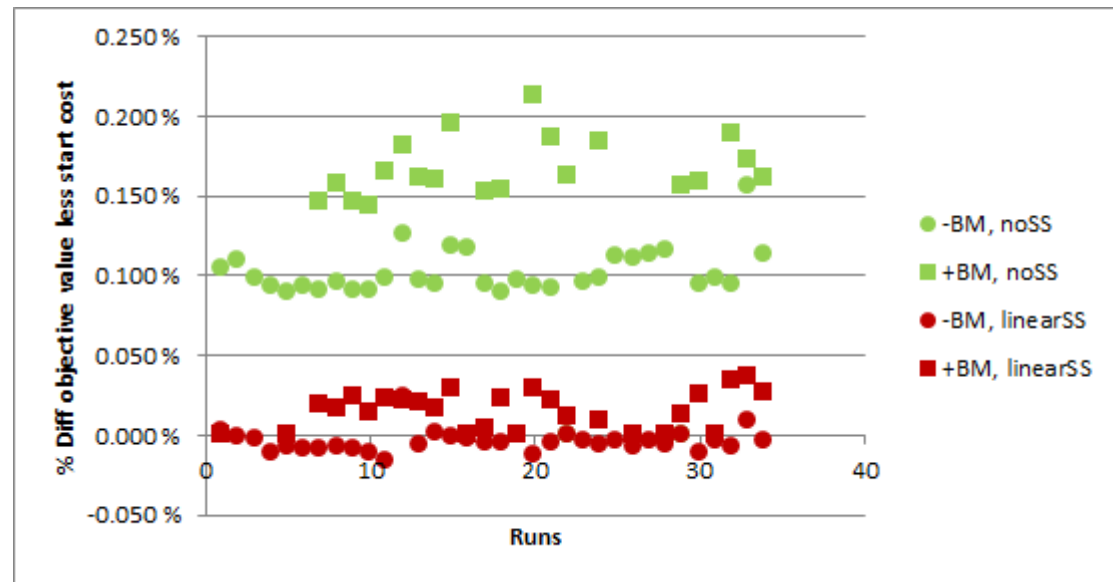
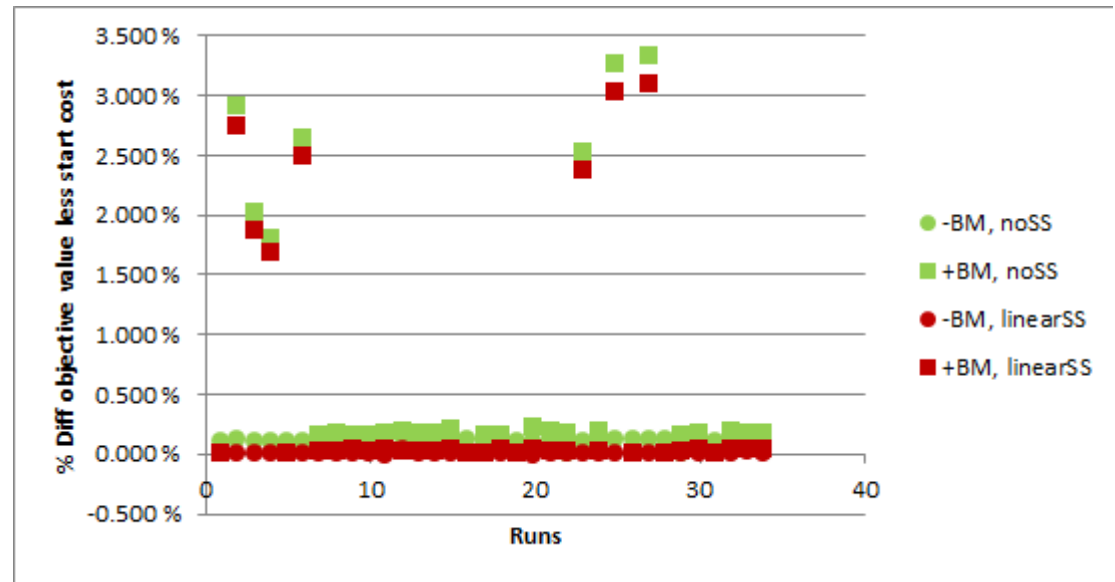
## Value of Balancing Market (BM)



# Comparison of start/stop models

## Observations

- Linear better than noSS (red vs green)
- Without BM better than with (circles vs squares)
- Introduction of BM reduces approximation quality



# Spinning states

0/1 SS

linearSS

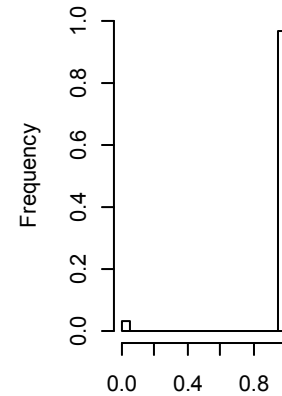
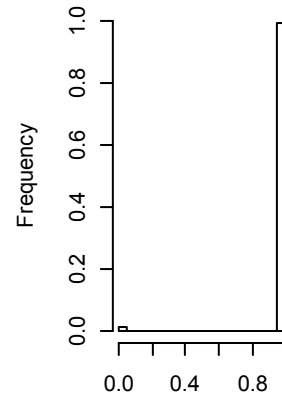
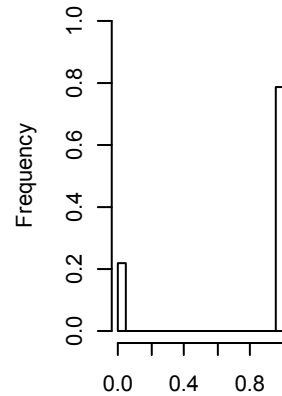
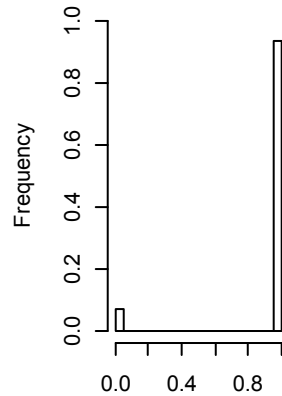
-BM

+BM

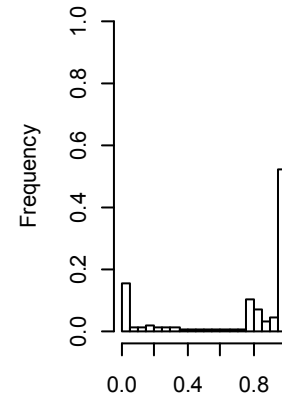
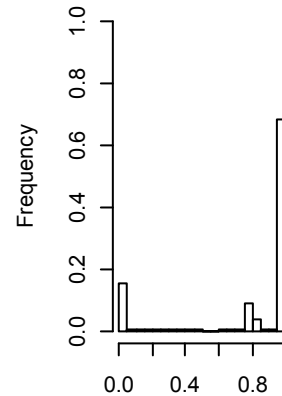
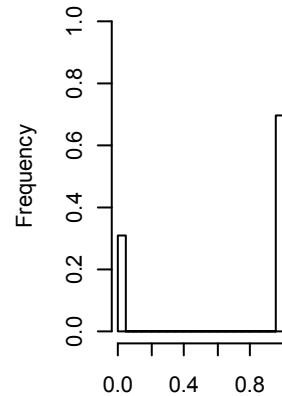
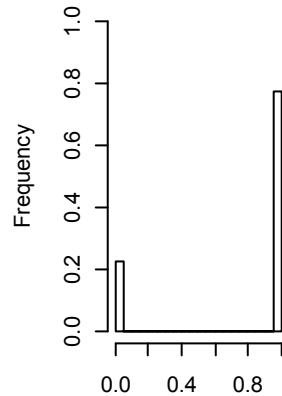
-BM

+BM

Generator 5



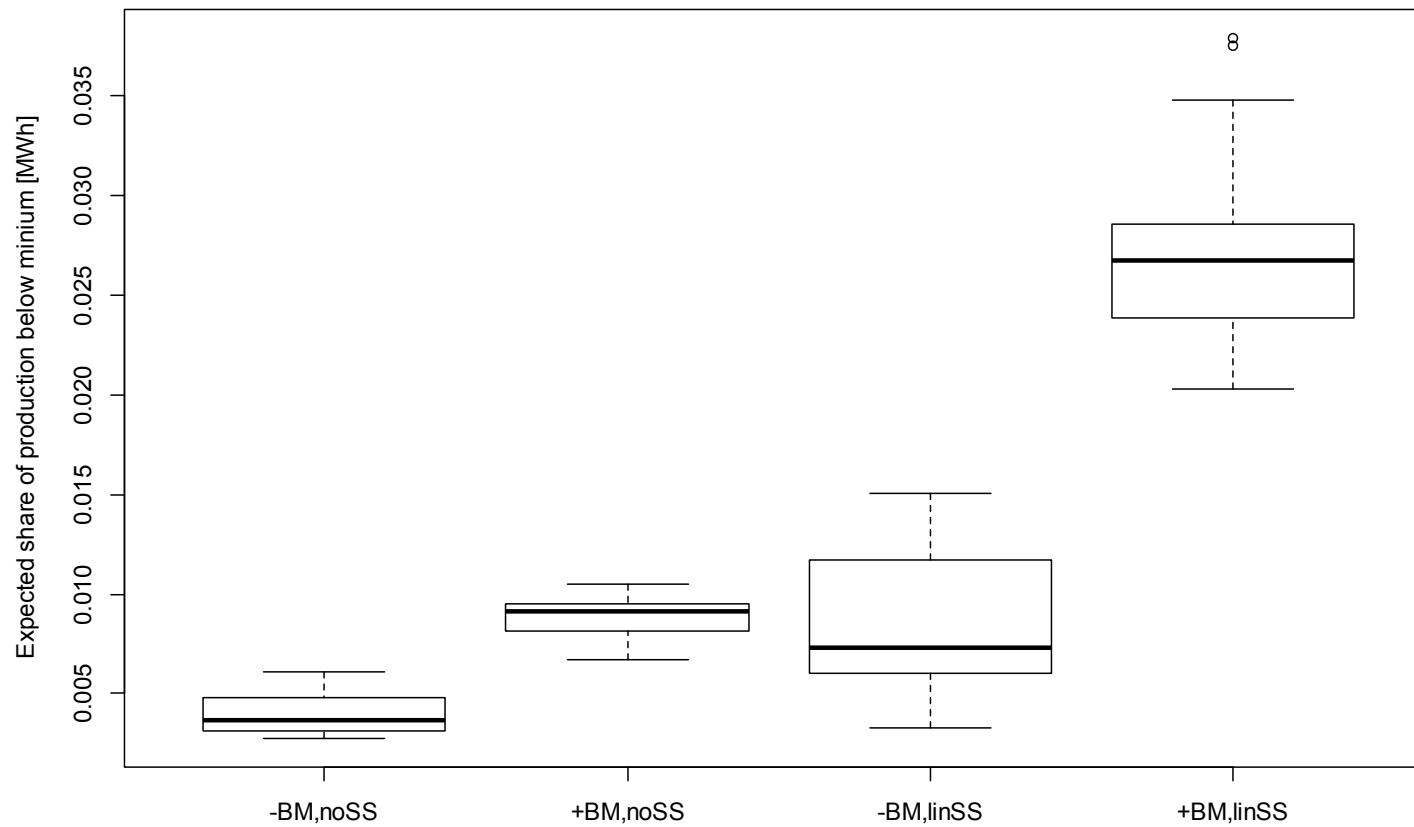
Generator 6



## Observations:

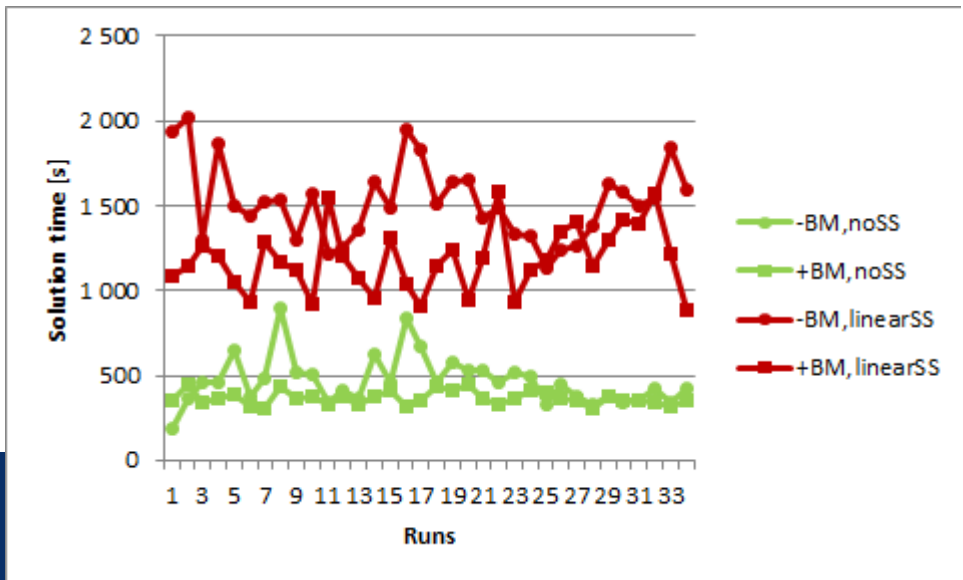
- More non-spinning with BM
- More non-spinning with 0/1
- More fractional spinning variables with BM
  - 19% vs 29%

# Operation below minimum production



# Solution times

- Standard solver (CPLEX) without any tuning or algorithmic efforts
- 204 instances
  - 9 instances removed due to failure (out of memory)
  - Most 0/1 time limited [24 h]
- Binary start/stop slow and memory consuming
  - Even harder with BM
- LinearSS 3-4 times slower than noSS



## Conclusion and further work

- Preliminary "conclusions"
  - Linear ok for valuation, but worse with BM
    - Objective function value good
    - Solution time ok
    - Operating decisions not ok for scheduling
  - BM currently limited value
- Further work
  - Sensitivity to start cost
  - Different seasons

Thank you!





## References

- Warland, G., Huuse, E. S., "Including thermal unit start-up costs in a long-term hydro-thermal scheduling model", 16<sup>th</sup> PSCC, Glasgow, Scotland, July 14-18, 2008