

# Joint modelling of wind and hydro inflow for power system scheduling

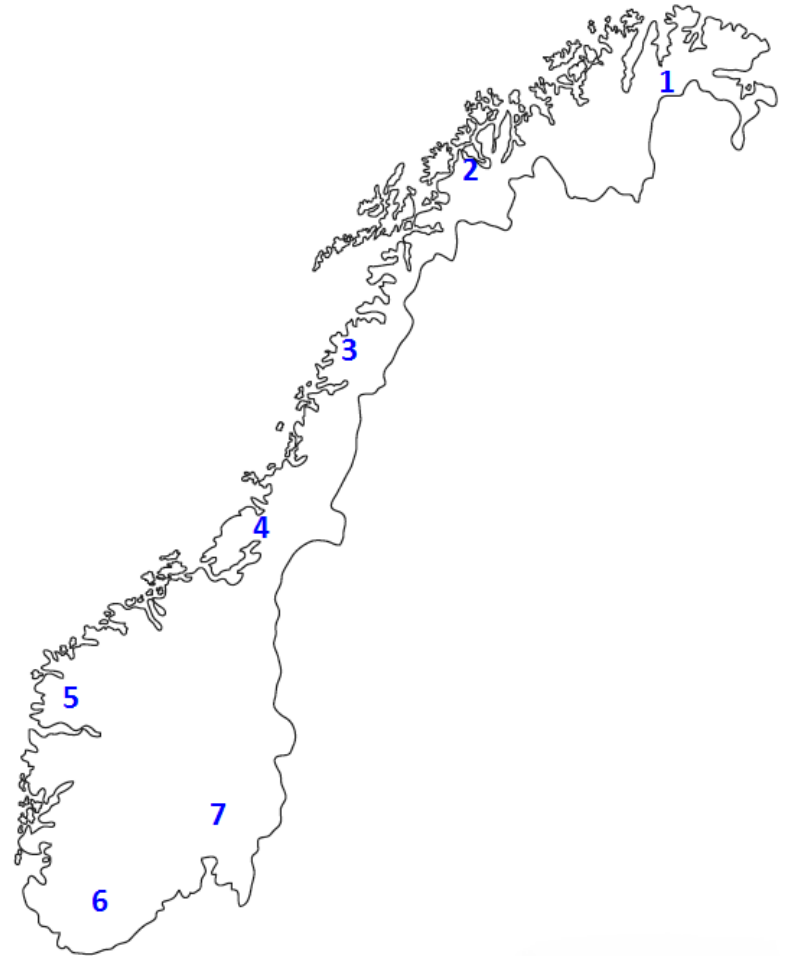
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# Background

- Introduction of wind in hydro-dominated systems
- Regions with limited transfer capacity
- Coordinate long-term hydro scheduling with wind
- Account for uncertainty in wind

# Data

- Reanalysis wind data
- Observed inflow data (NVE)
- Daily and weekly average series



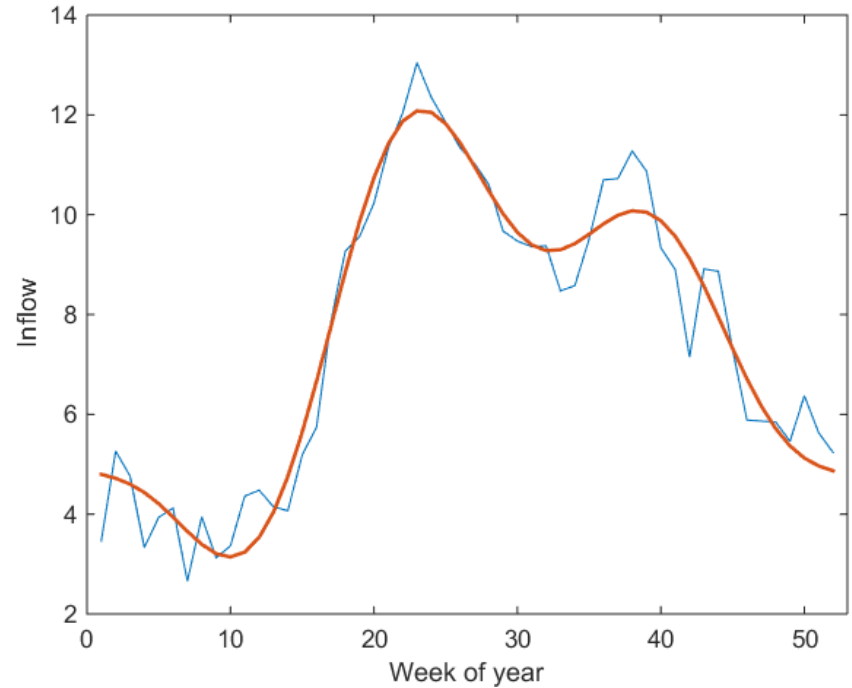
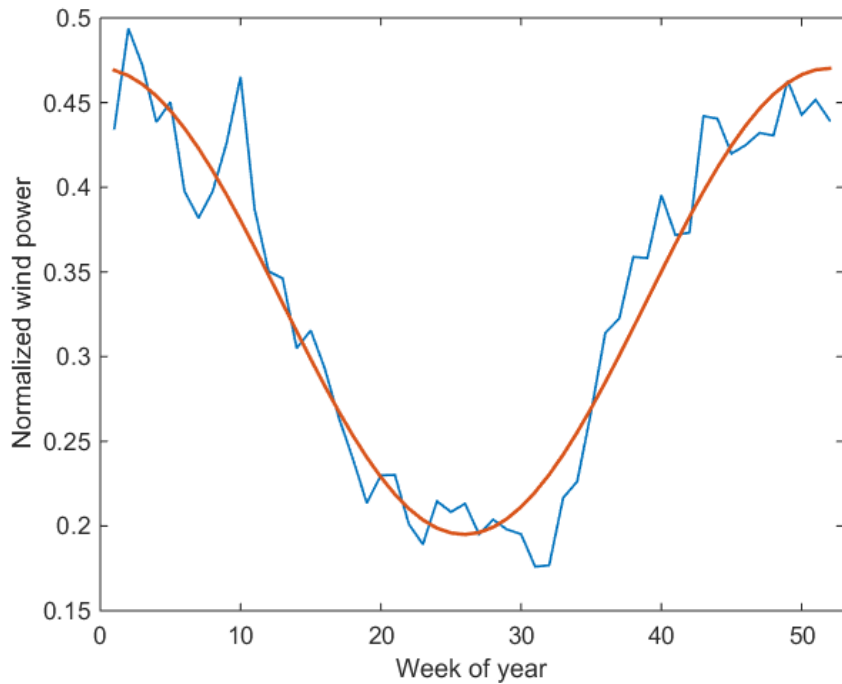
# Data characteristics

- Seasonality – wind and inflow

**Non-stationary**

- Serial correlation
- Inter-dependence

# Seasonality



Sample weekly mean (blue) and estimated seasonal mean (red) for region 5

# Joint model wind and inflow

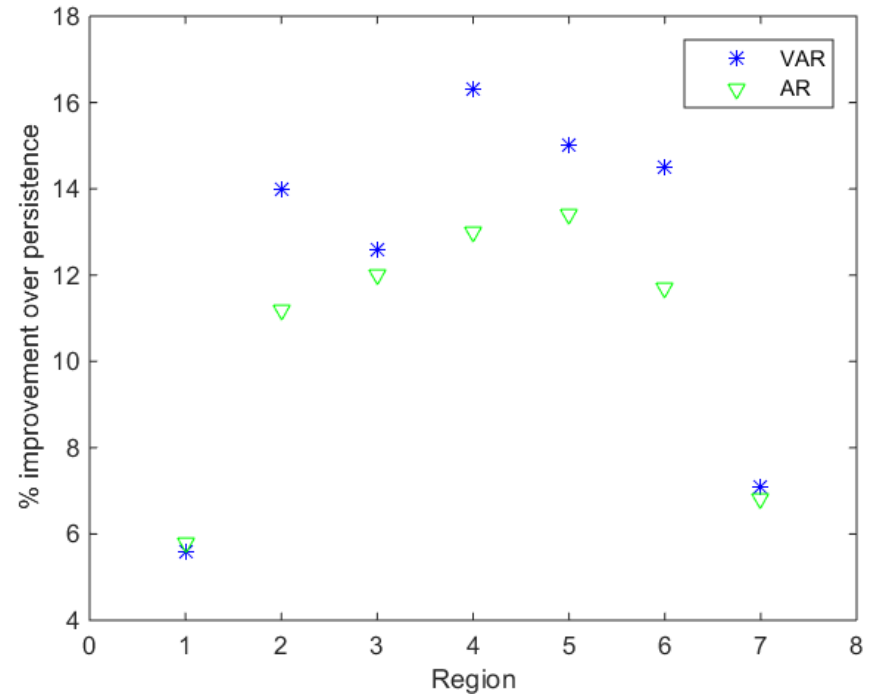
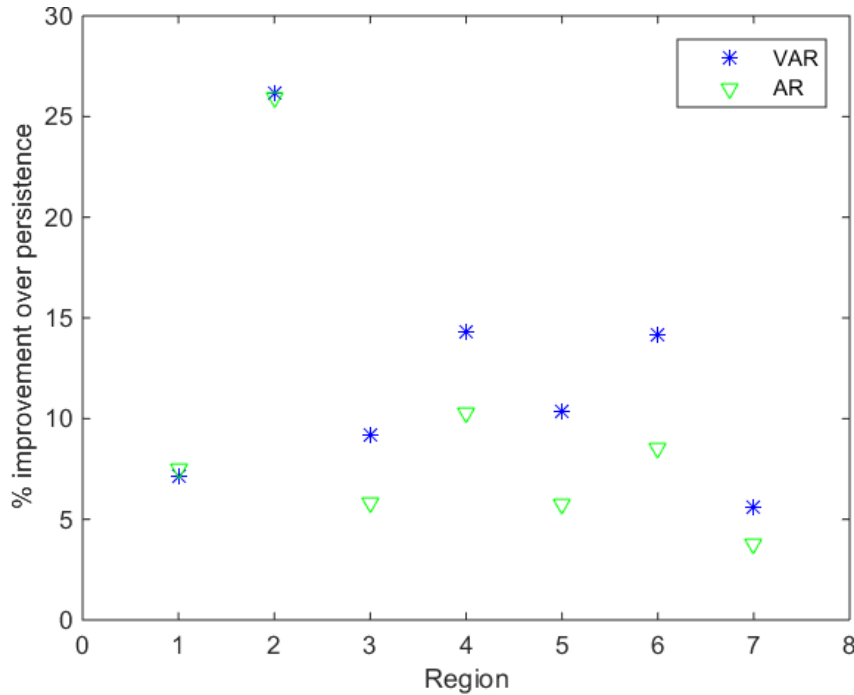
- Deseasonalize individually
  - harmonic regression
- Series now assumed stationary
- Lagged and contemporaneous dependencies
  - vector autoregressive model of order  $p$   
( $\text{VAR}(p)$ )

# Modelling results

VAR(1), region 5. Parameter estimates and corresponding standard error

Data	$\varphi_{11}$	SE	$\varphi_{12}$	SE	$\varphi_{21}$	SE	$\varphi_{22}$	SE
Region 1	0.144	0.019	-0.015	0.019	0.008	0.014	0.696	0.014
Region 2	0.175	0.020	0.030	0.020	0.157	0.016	0.550	0.016
Region 3	0.199	0.020	0.026	0.019	0.074	0.020	0.409	0.019
Region 4	0.229	0.021	-0.010	0.020	0.169	0.020	0.280	0.020
Region 5	0.213	0.020	0.052	0.020	0.095	0.019	0.363	0.019
Region 6	0.185	0.021	0.050	0.021	0.140	0.019	0.414	0.019
Region 7	0.240	0.019	0.021	0.017	0.032	0.017	0.612	0.015

# Forecasting performance



Percentage improvement over persistence forecast in terms of mean Euclidean error for daily (left) and weekly (right) series



# Concluding remarks

- Joint modelling of wind and inflow can improve forecasting performance
- Can improved *quality* be translated into improved *value*?
- TODO: Investigate impact of stochastic wind-inflow representation in SDDP-based scheduling models

Thank you

