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Modelling overflow using mixed integer programming in short- term hydropower scheduling

Per Aaslid, SINTEF ER

Hydropower scheduling conference

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Contributors

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- Dag Haugland, UiB – Professor, Main supervisor
- Tarjei Lid Riise, Eviny Fornybar AS – Co-supervisor



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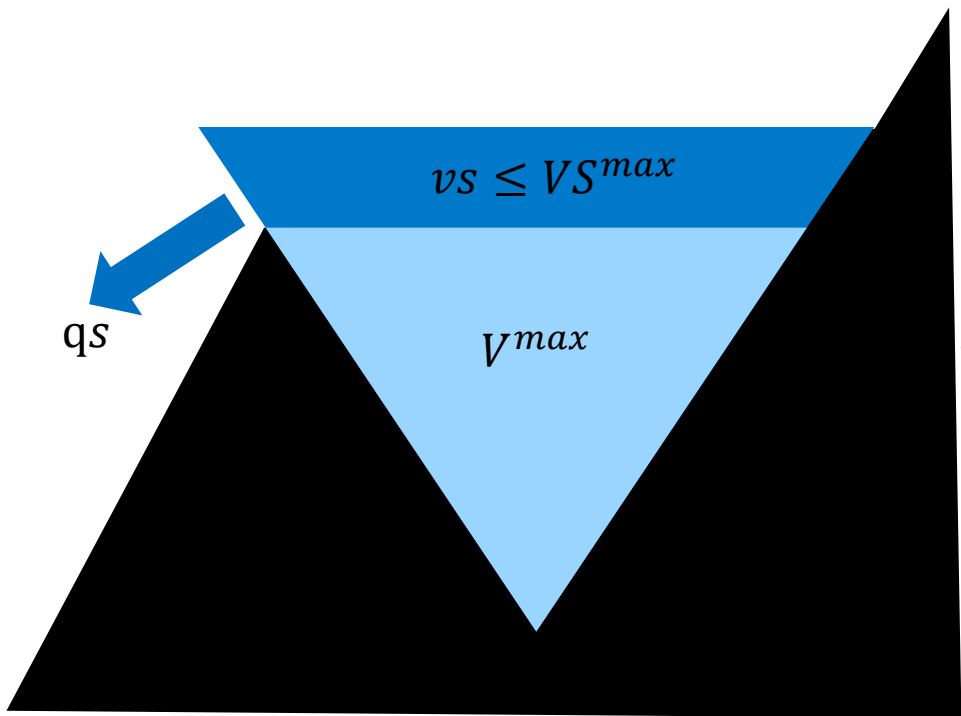
Outline

- Overflow modelling: LP vs MILP
- Challenges: non-physical overflow vs computation time
- Solutions
- Results



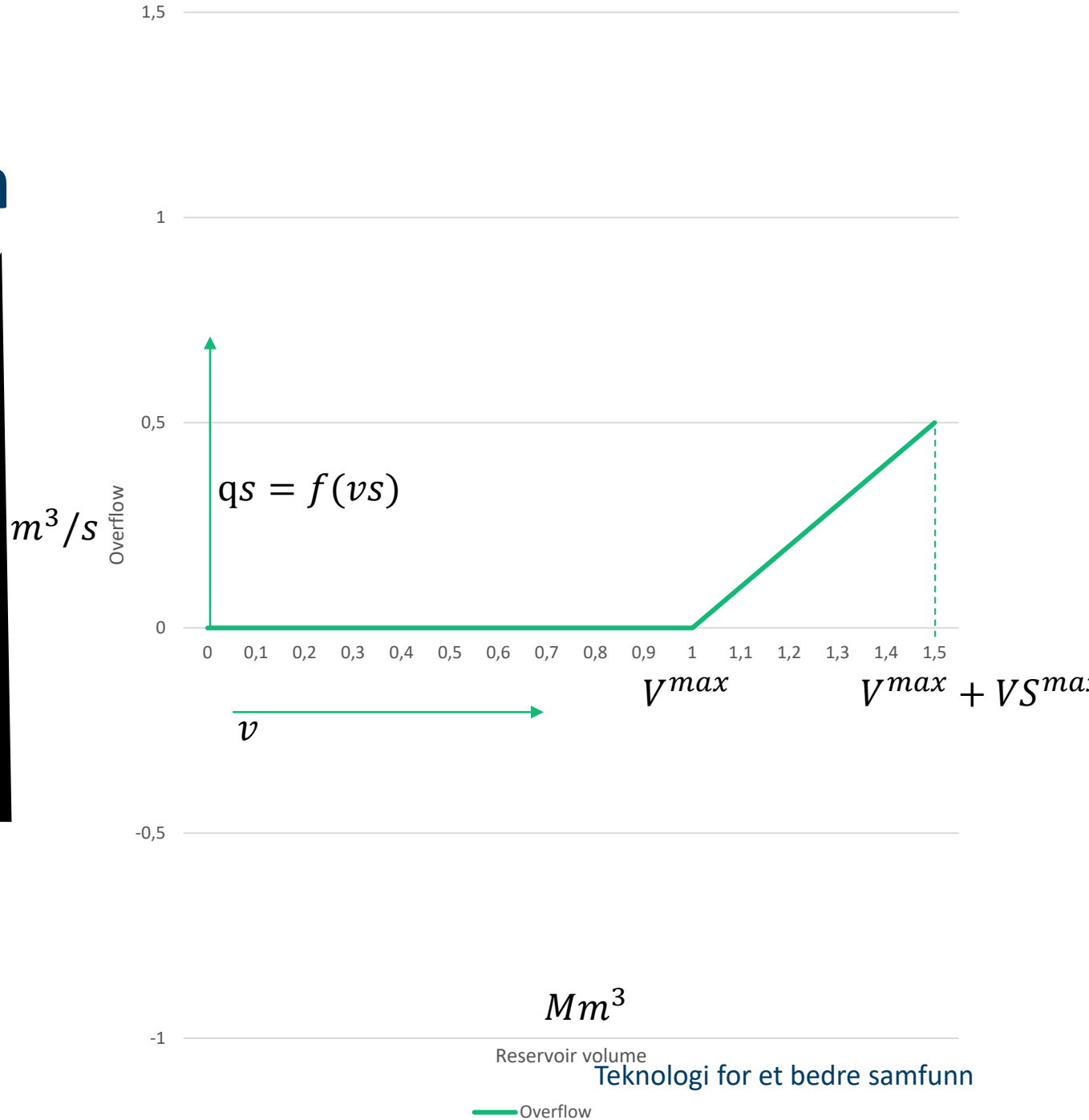
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Overflow function



$$vs = \max(0, v - V^{max})$$

Non-convex





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Mathematical formulation

$$v_S \geq 0$$

$$v_S \geq v - V^{max}$$

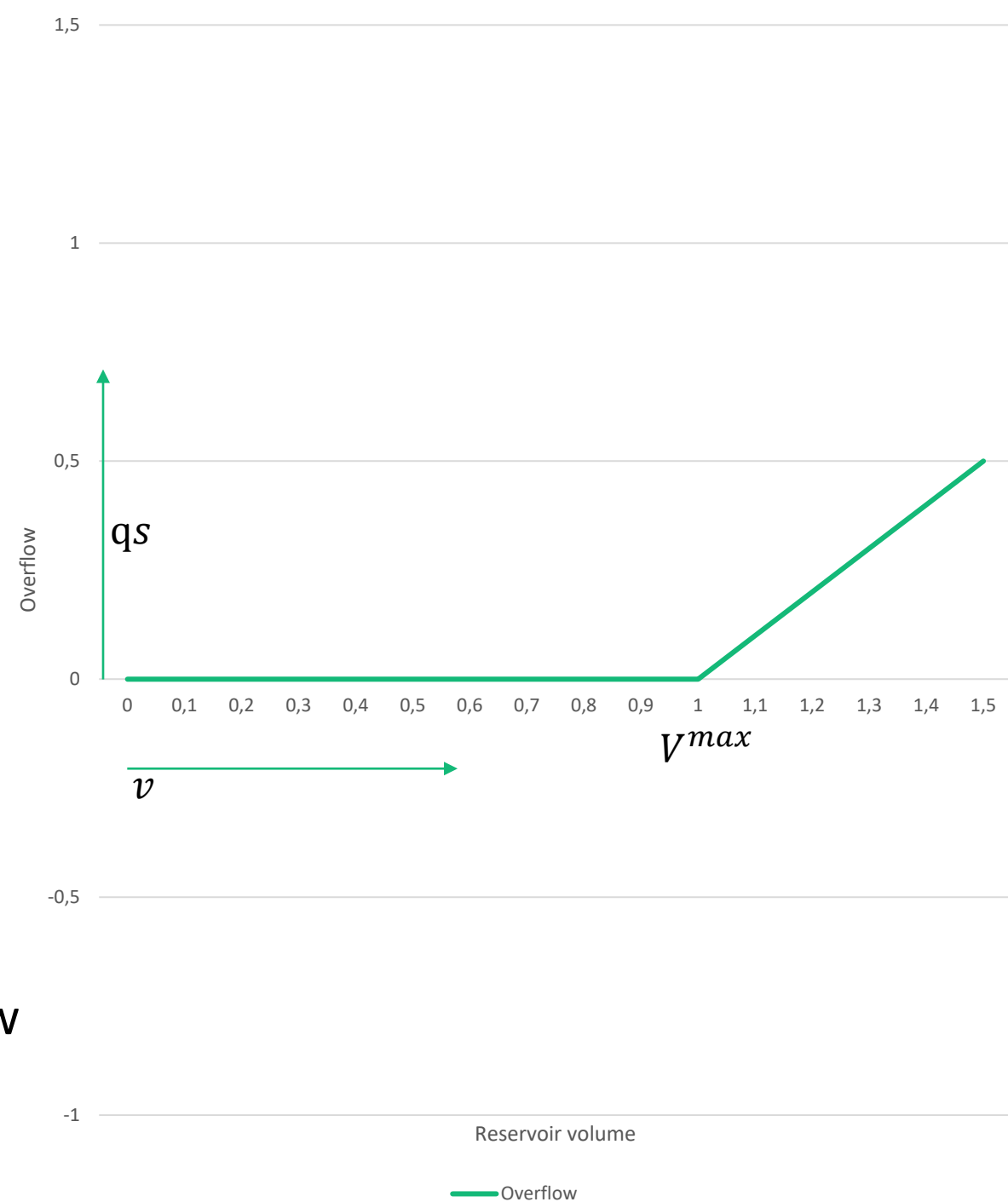
$$v_S \leq v - V^{max} \cdot \delta$$

$$v_S \leq M \cdot \delta$$

$$q_S = c \cdot v_S$$

$\delta = 0$ – no overflow

$\delta = 1$ – overflow





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Zero bound

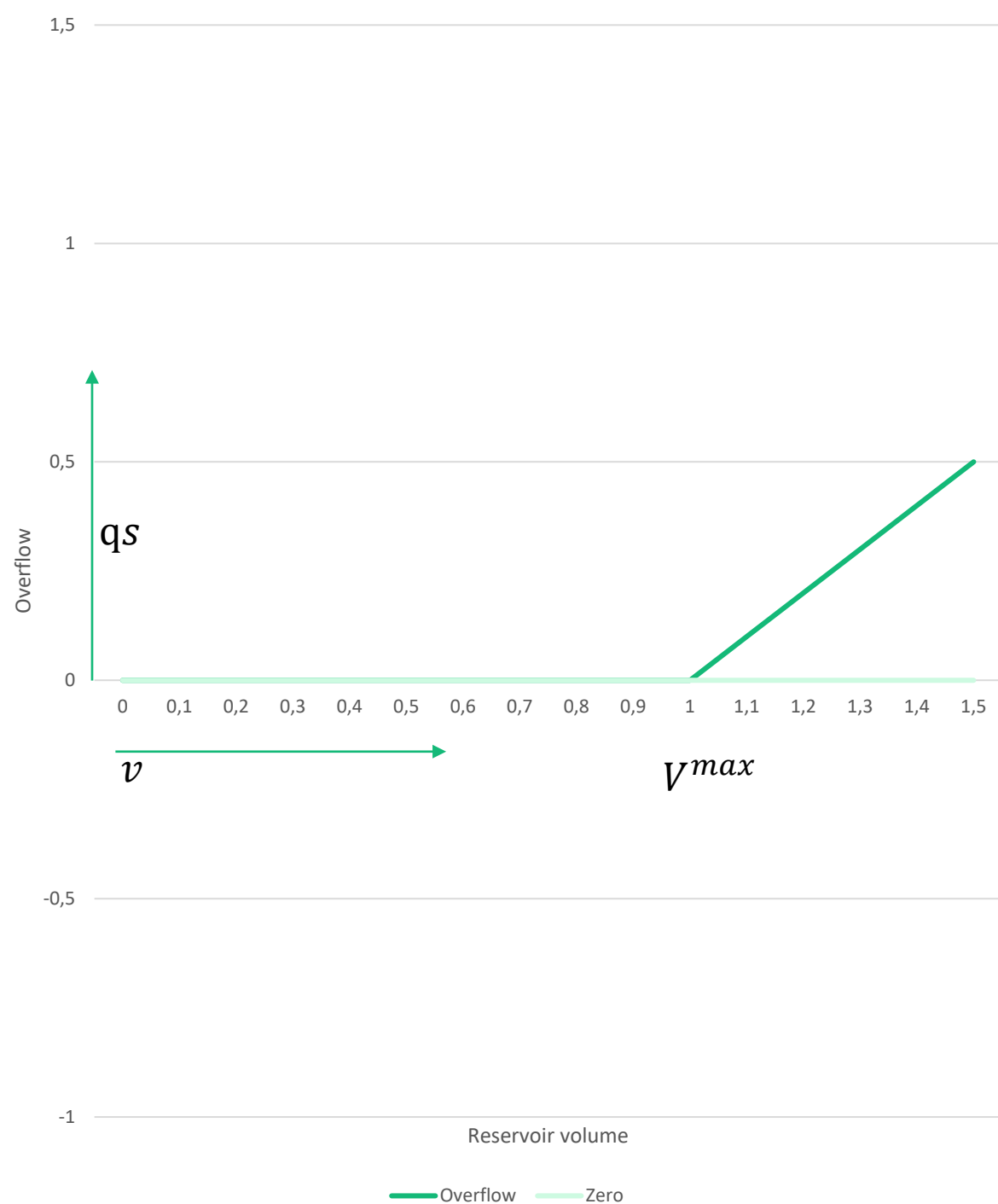
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Upper and lower bounds

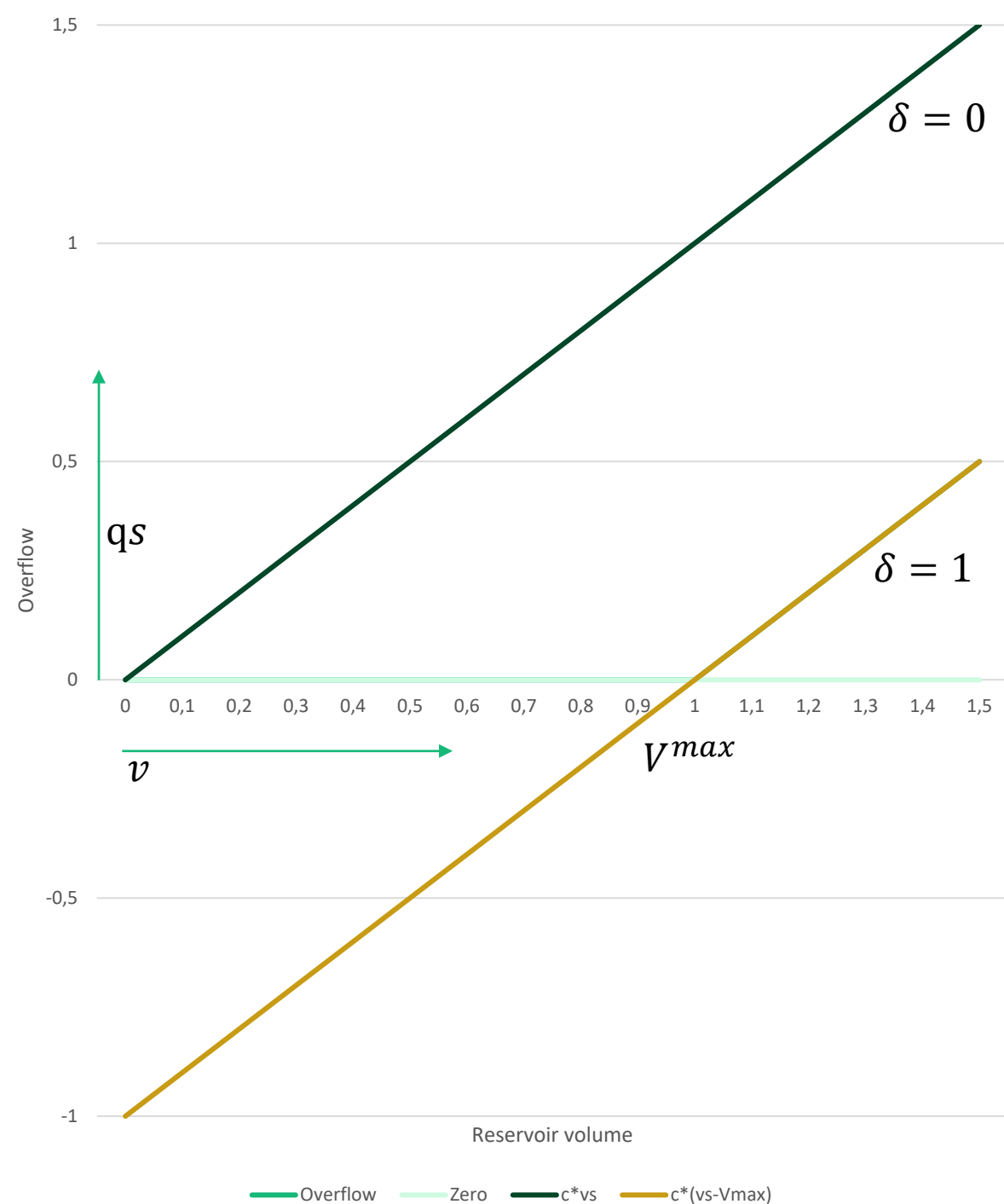
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Big M

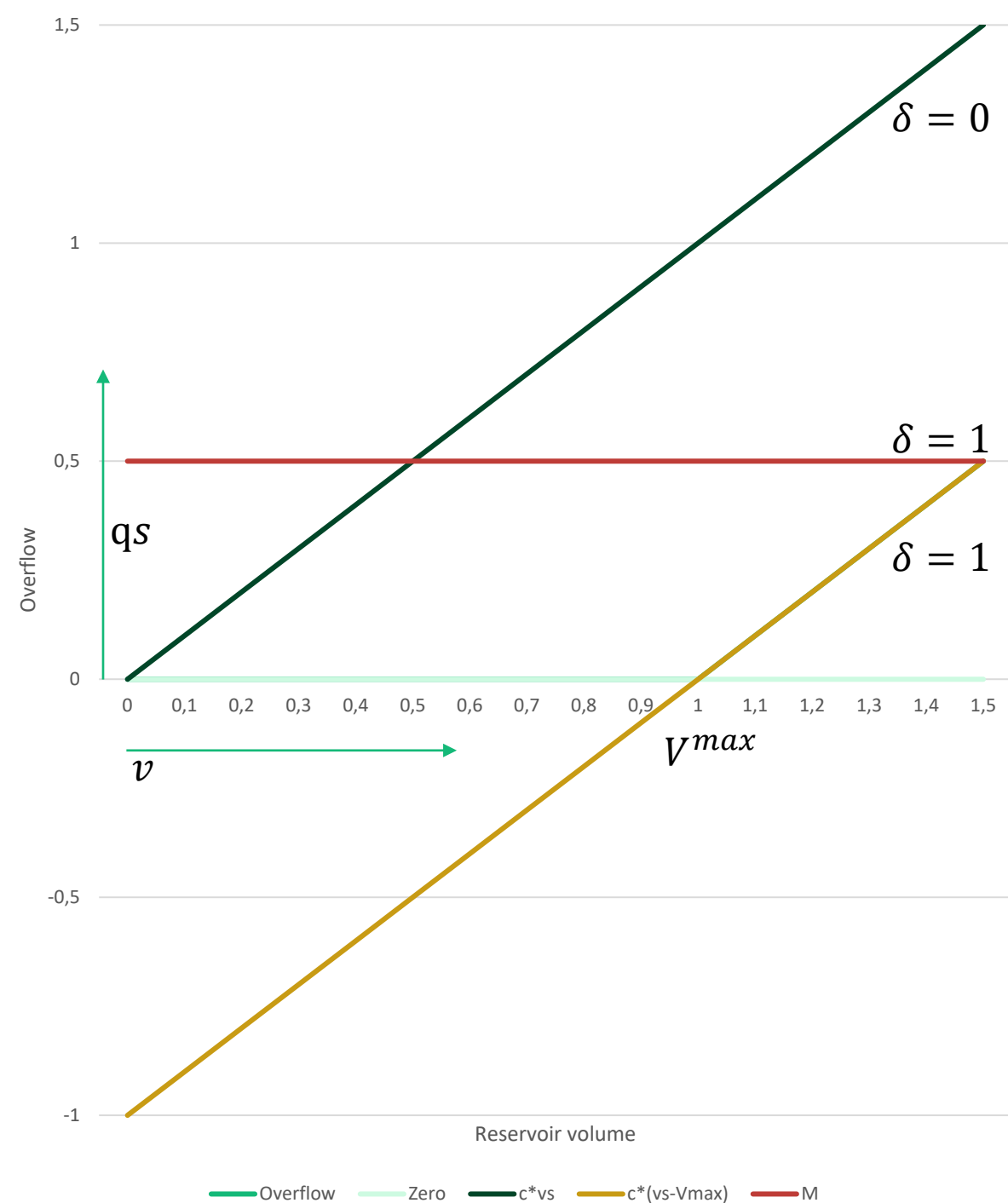
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Binary delta

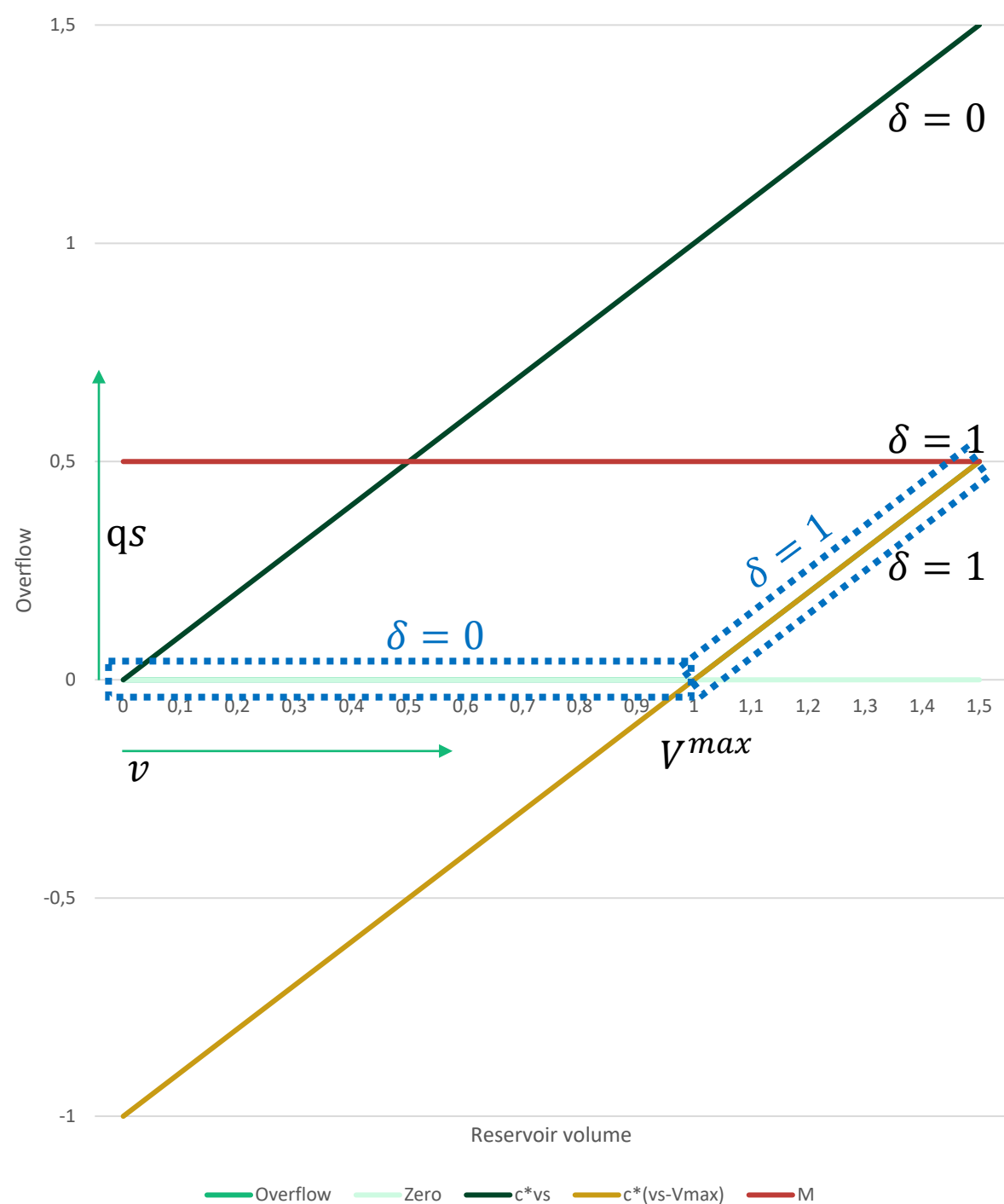
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Continuous delta

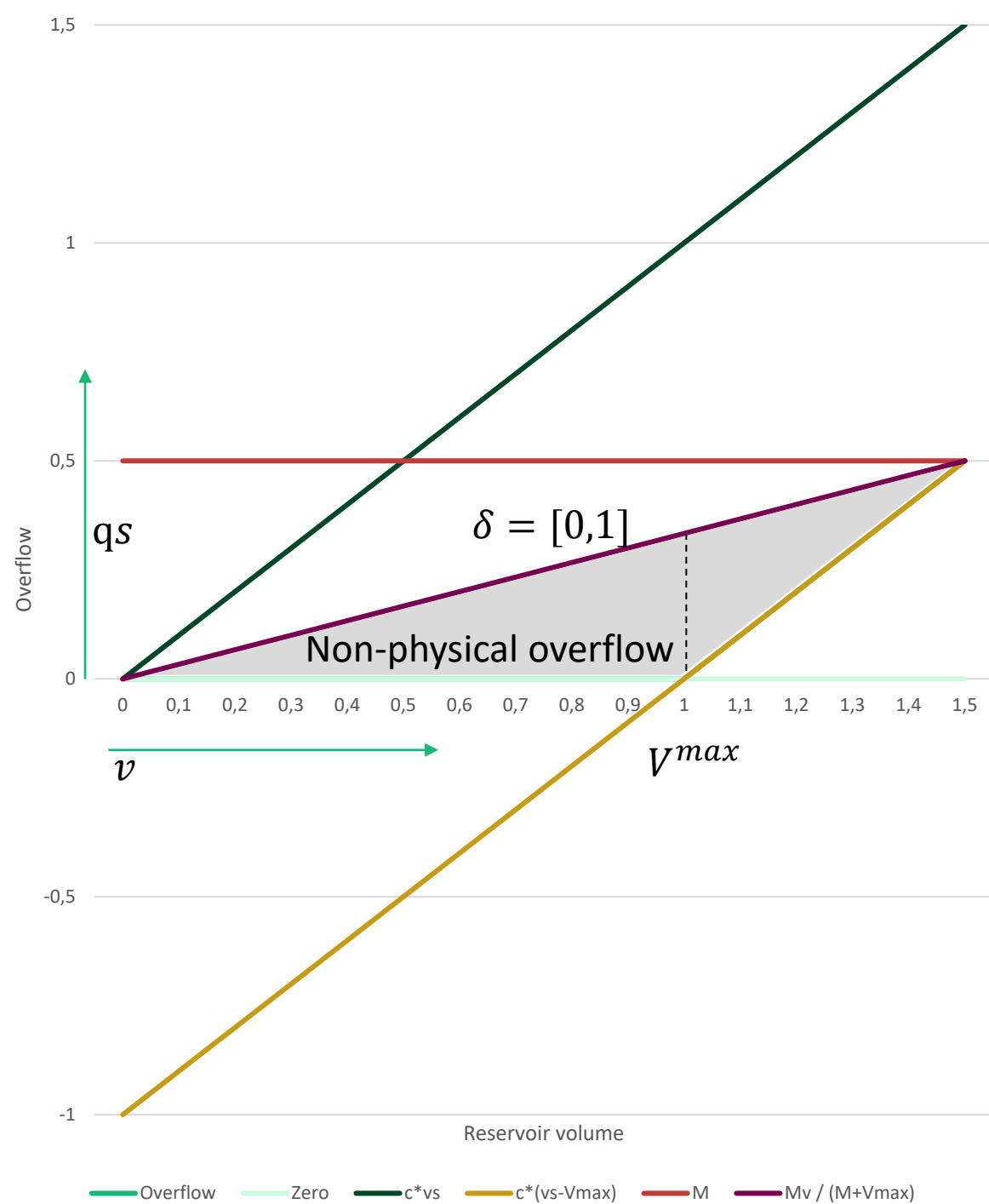
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$$v_S \geq v - V^{max}$$

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$$v_S \leq M \cdot \delta$$

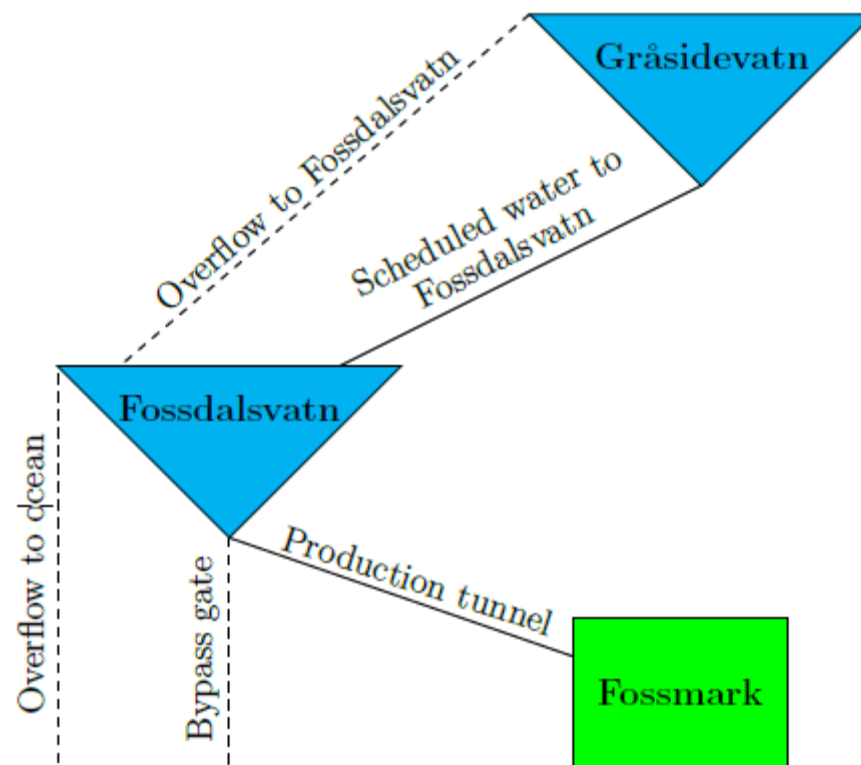
$$q_S = c \cdot v_S$$



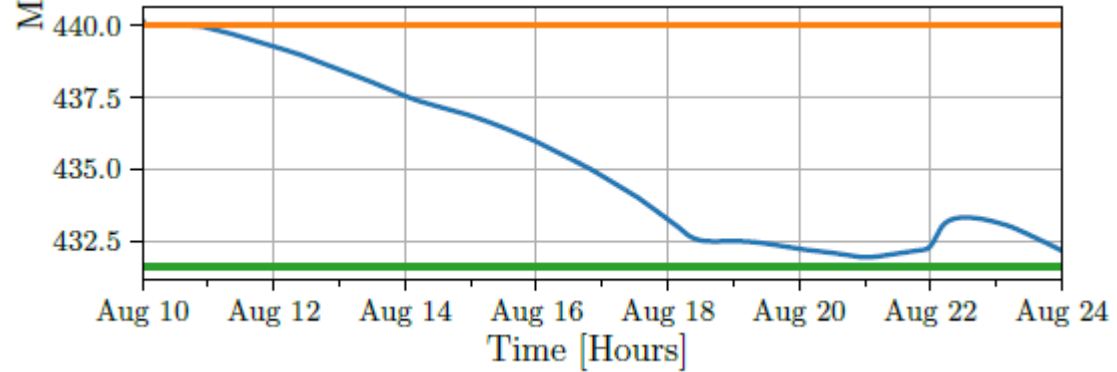
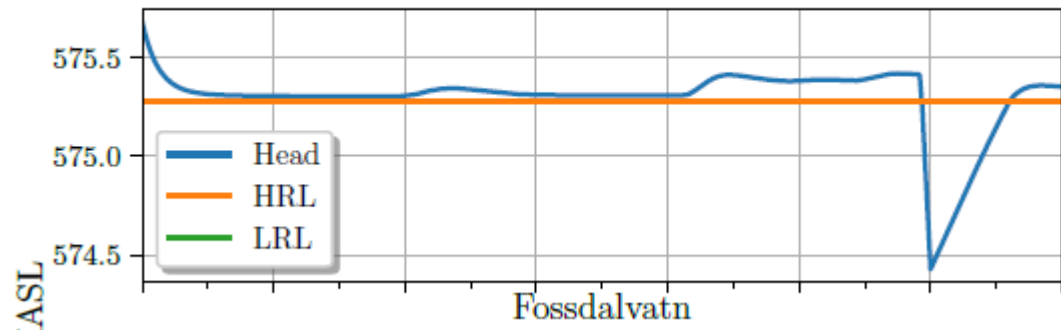
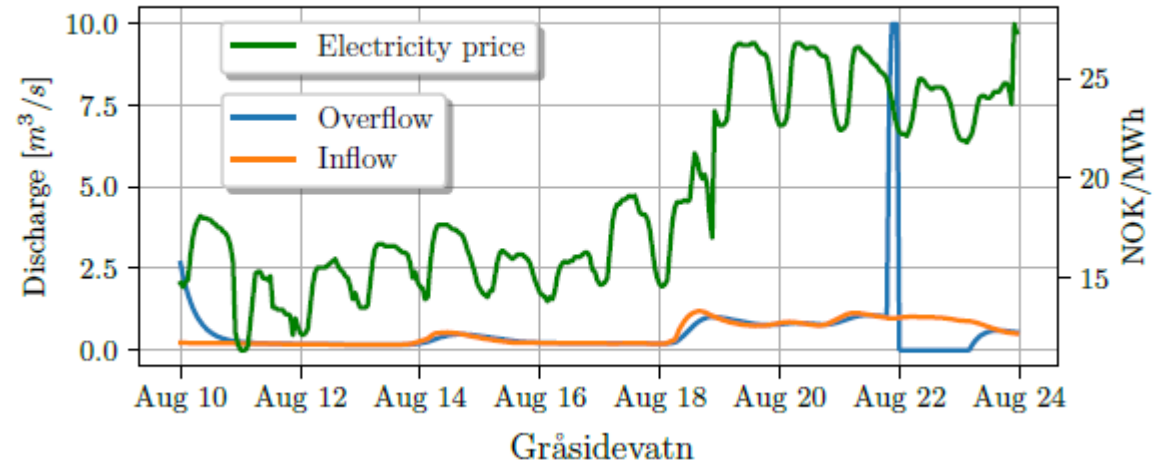


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Fossdal watercourse



Comparing electricity prices with overflow and inflow at Gråsidevatn





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Binary delta

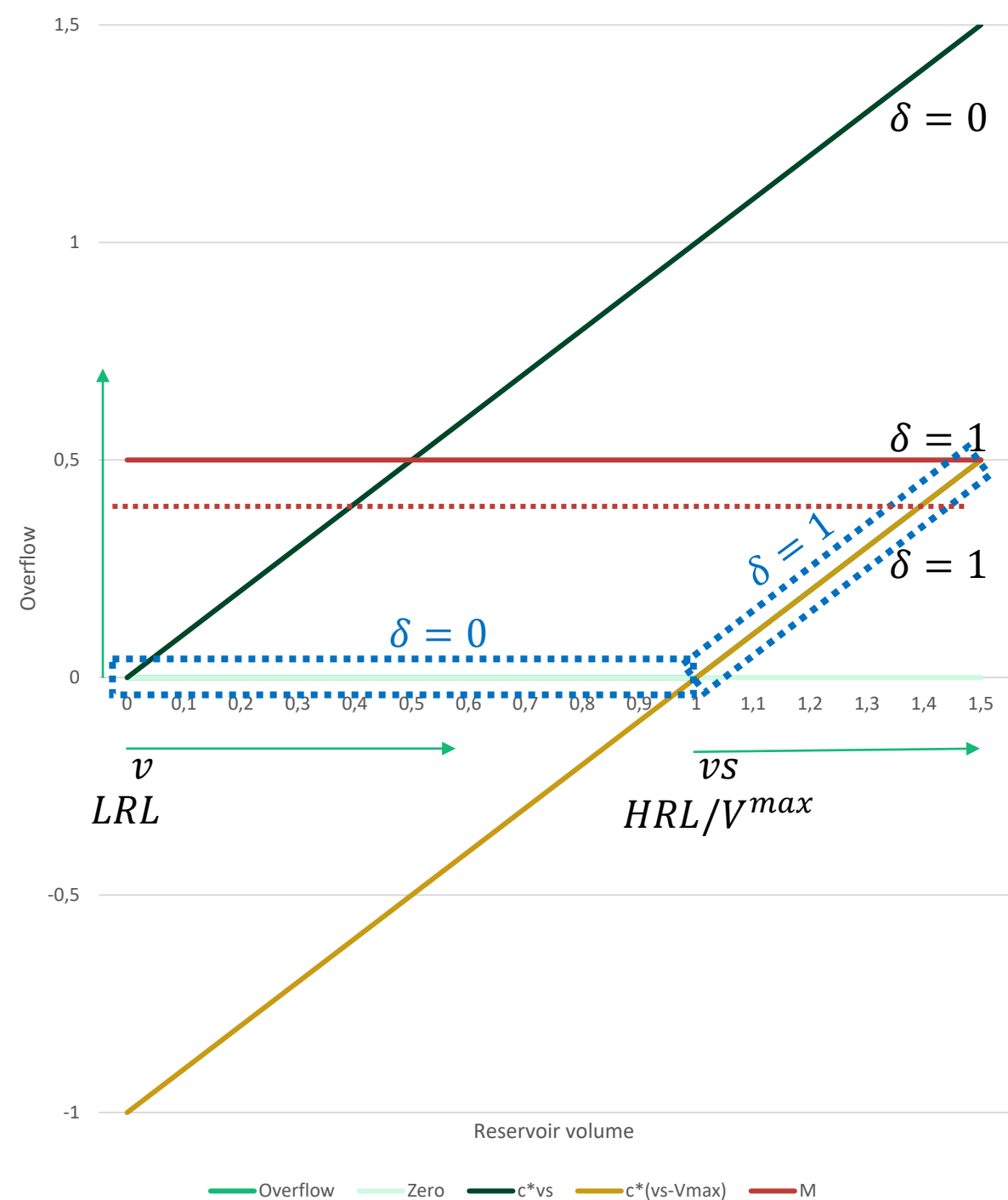
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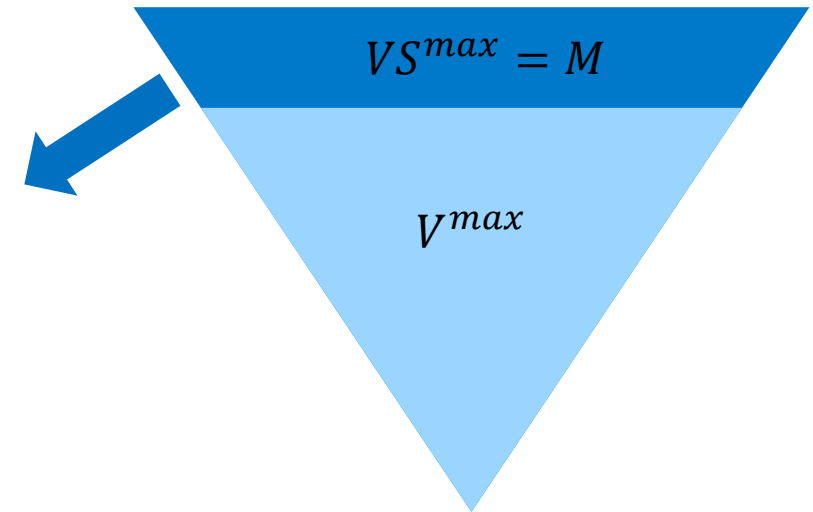




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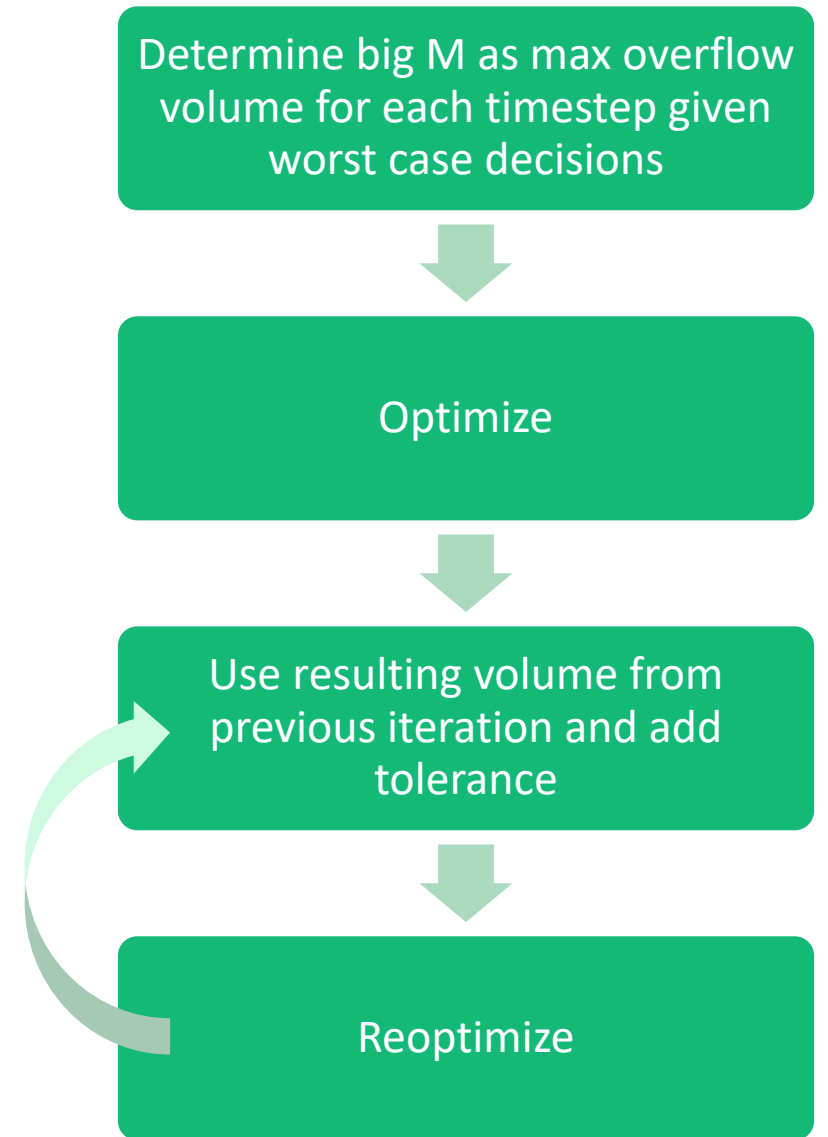
Big M

- The tightest big M is given by the maximum possible overflow volume.
- Can be approximated with known inflow by assuming the worst possible upstream production and gate discharge.
- Can be updated between the SLP iteration.



Big M heuristics for SLP (successive linear programming)

- Starting volume
- Inflow
- Overflow description
- Plant and gate discharge



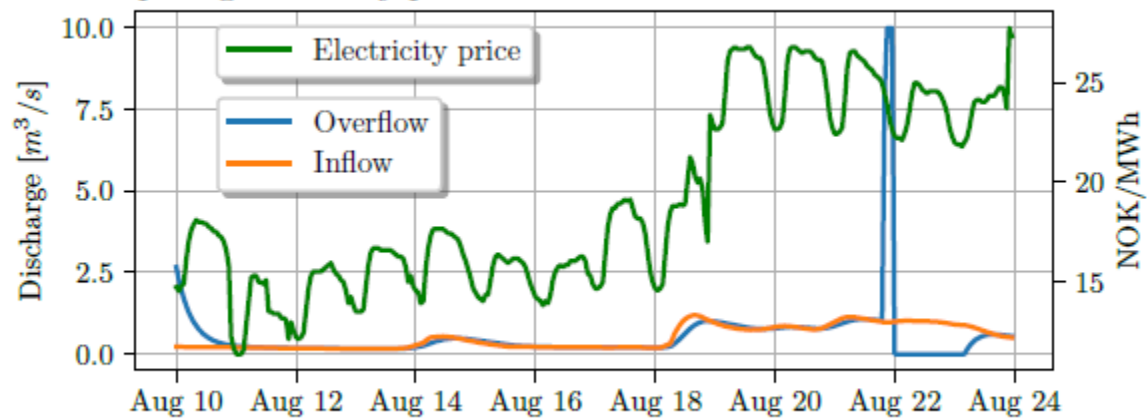


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SHOP

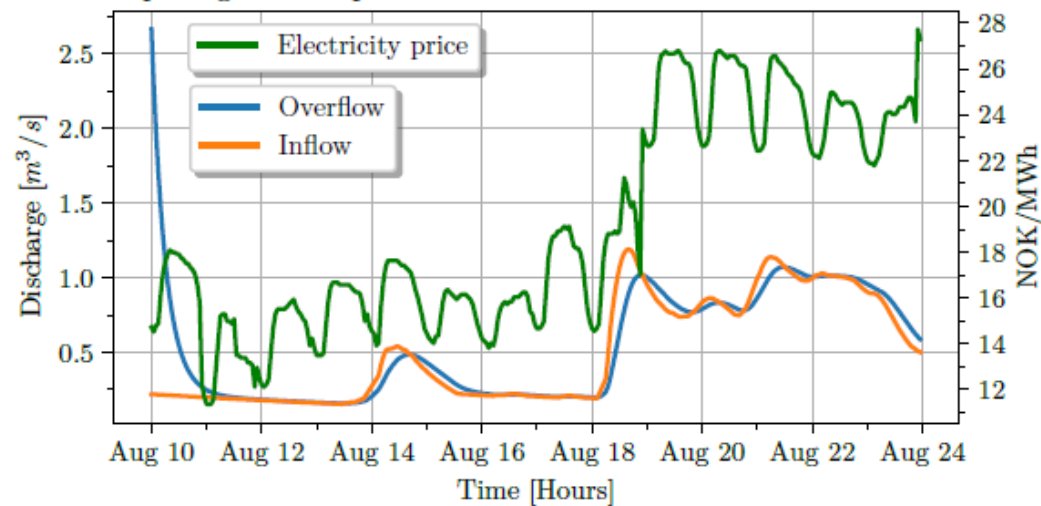
- SHOP is a short-term hydro scheduling model developed by SINTEF.
- Uses successive linear programming.
- In operational use by most of the major hydro power producers in the Nordic countries.

Comparing electricity prices with overflow and inflow at Gråsidevatn

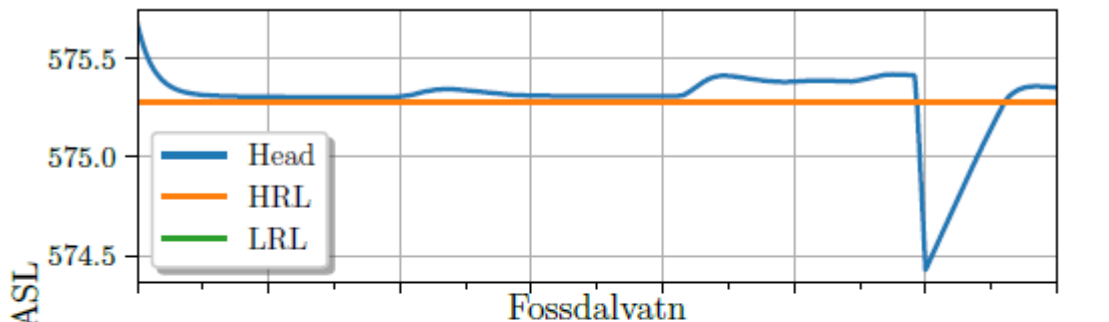


Gråsidevatn

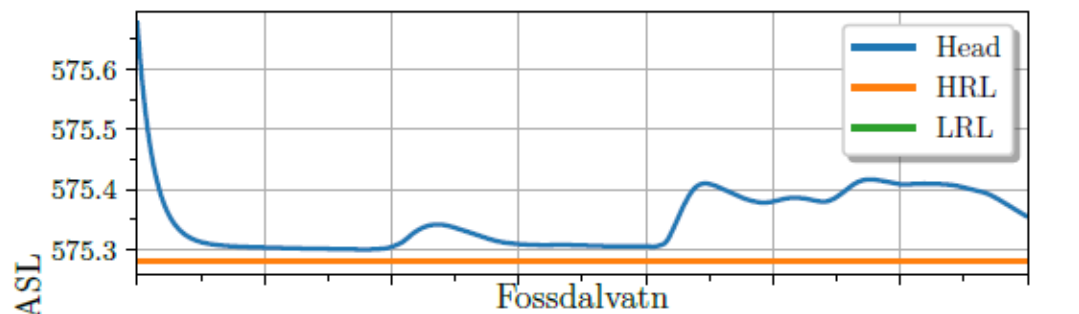
Comparing market price with overflow and inflow at Gråsidevatn



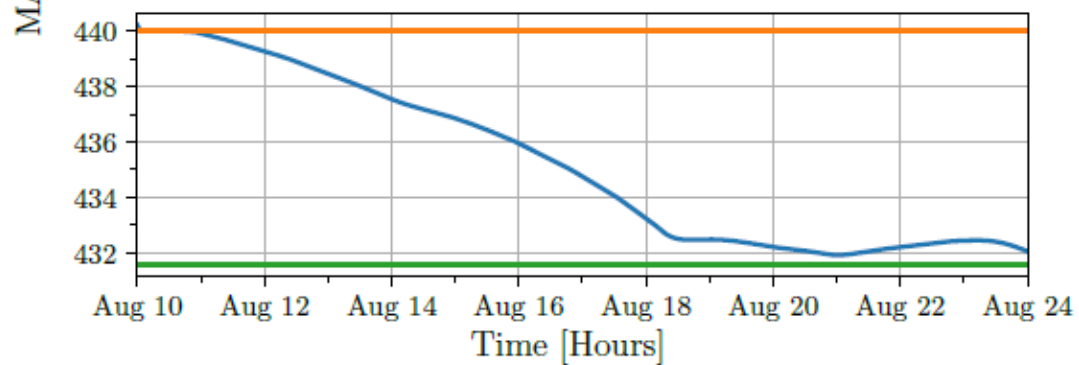
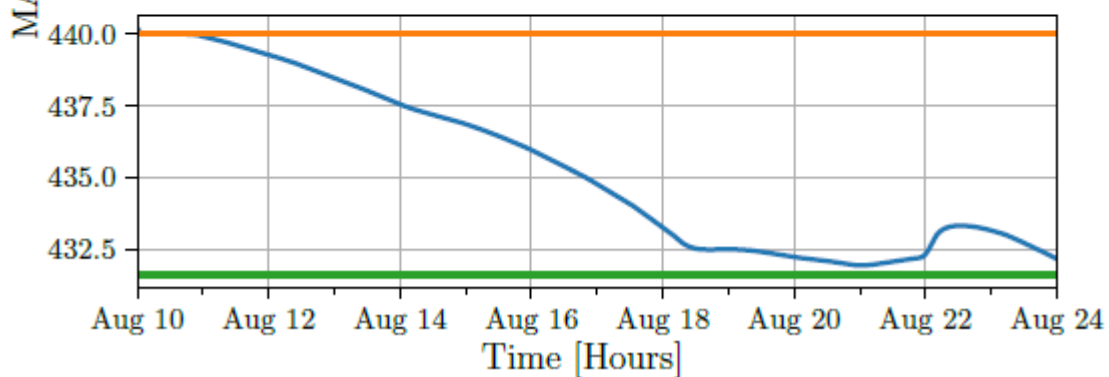
Gråsidevatn



Fossdalvatn



Fossdalvatn

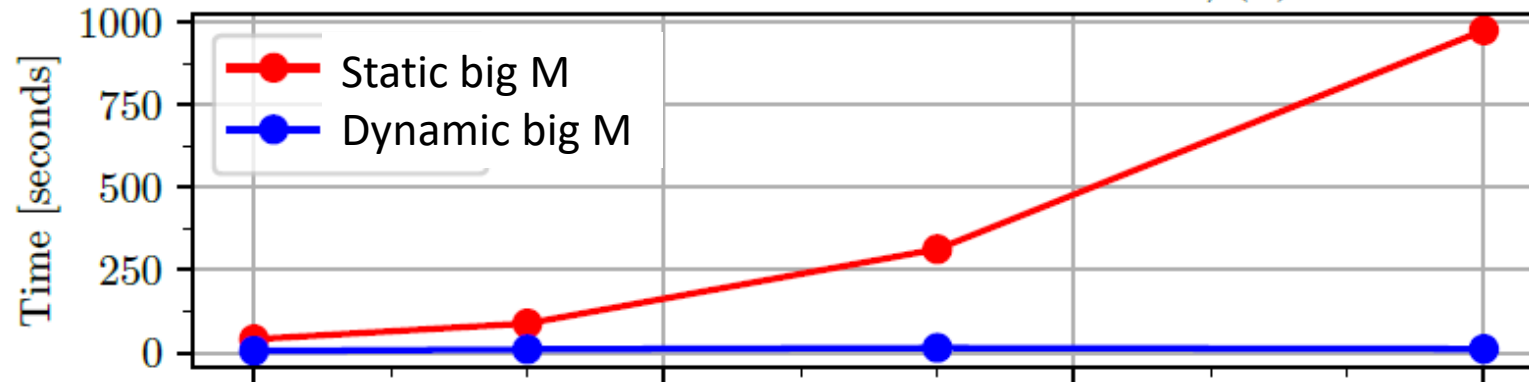




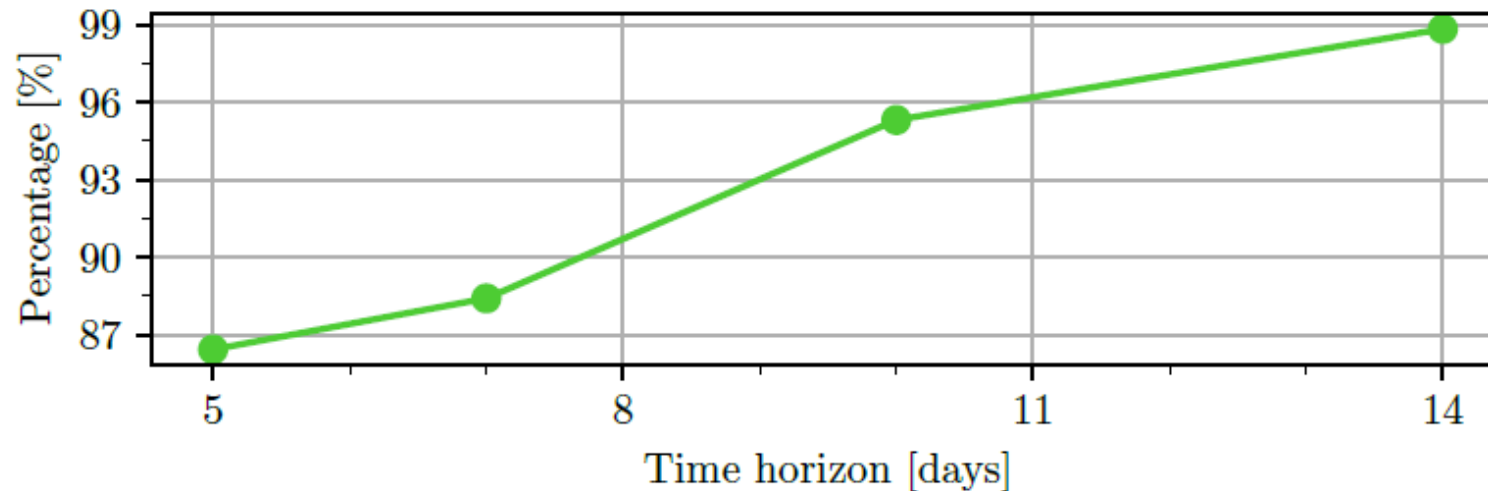
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Comparison of static and dynamic big M

Solution time in CPLEX - comparing $\sigma_{r,t}(g)$ to ζ_r



Percentage reduction of the solution time





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Optimizing big M?

Maximize flood volume

~~Minimize costs~~

Subject to physical and market
constraints



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Further work

- Investigate feasible directions towards tight feasible big M values.
- Test method for more complex systems and improve heuristics if necessary.
- Test other reasons for non-physical overflow.



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Teknologi for et bedre samfunn