

# COMBINING MONTHLY INFLOW AND WIND UNCERTAINTIES IN THE OPERATION PLANNING OF HYDRO-DOMINATED SYSTEMS

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# INTRODUCTION

## RENEWABLES IN BRAZIL

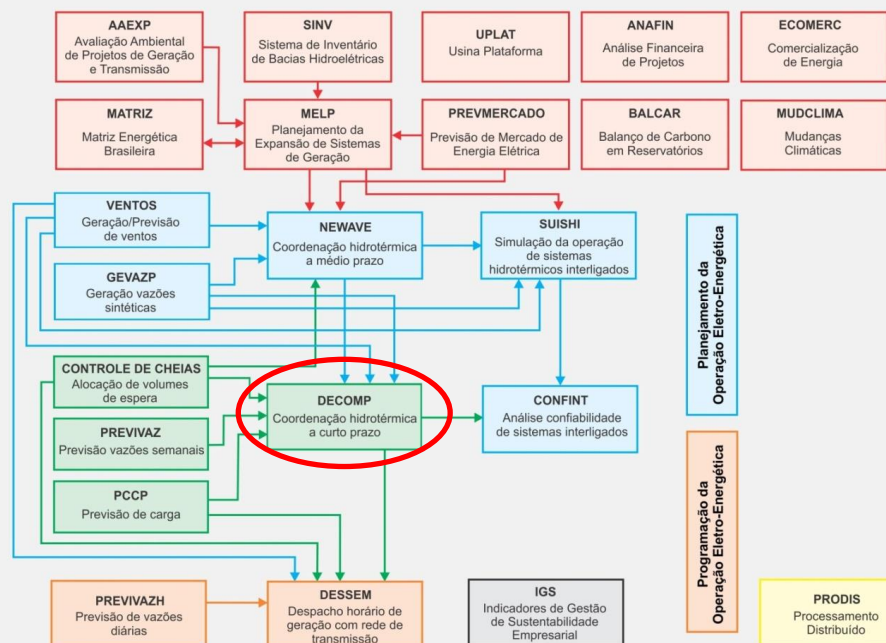
The Brazilian electricity matrix has a high share of renewable sources, mainly with a preponderance of hydroelectric technology

In last decade wind power grew 13 times, reaching 19 GW of installed capacity (10% share); it is also estimated that in the period 2020-2029 its share will increase 2.5 times and reach 40 GW (17.3%)

**Electrical system expansion and operation planning requires even more sophisticated models and tools to deal with the intermittent behavior and uncertainties associated with renewable technologies**

In the case of Brazil, this problem is divided into expansion planning (long term), operation planning (medium and short term), and operation programming, being solved through a chain of computational models

Cadeia de Modelos para o Planejamento da Expansão da Geração e da Operação Energética

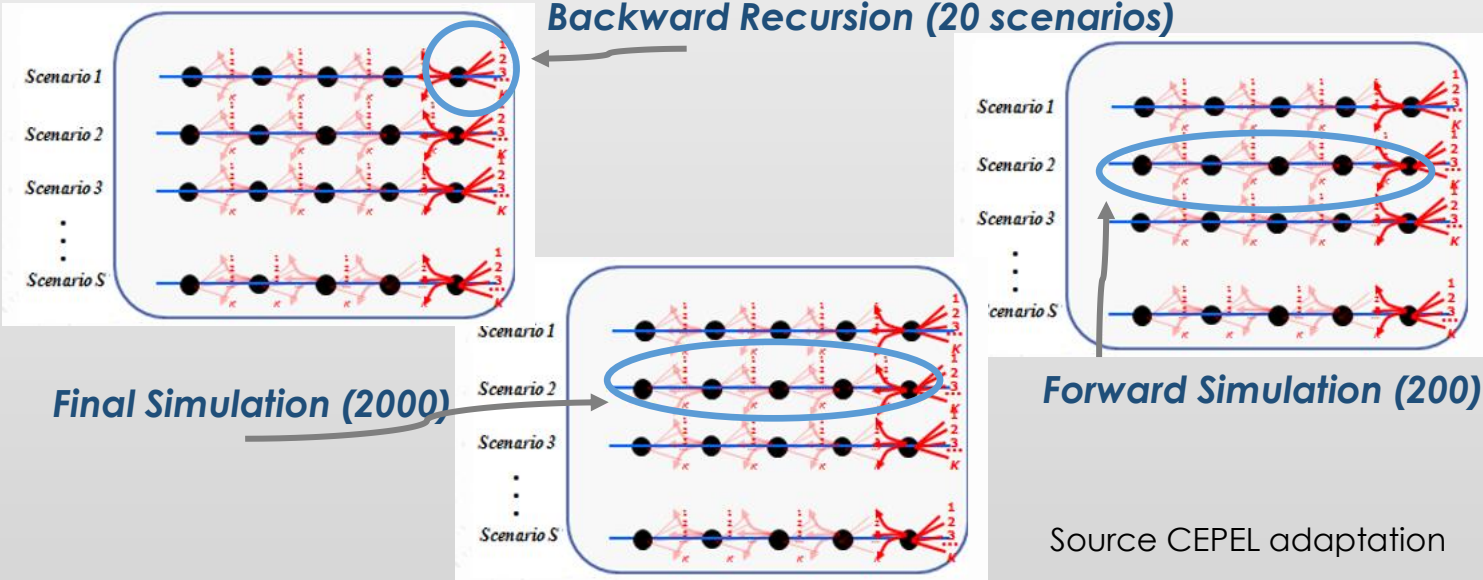
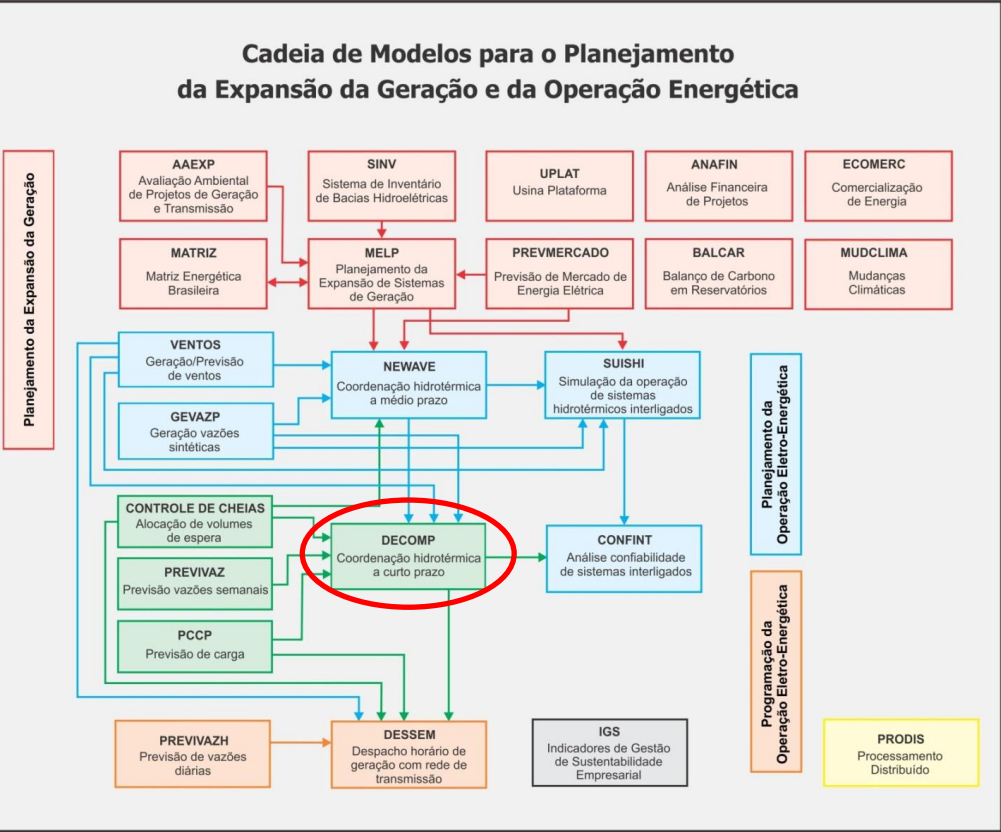
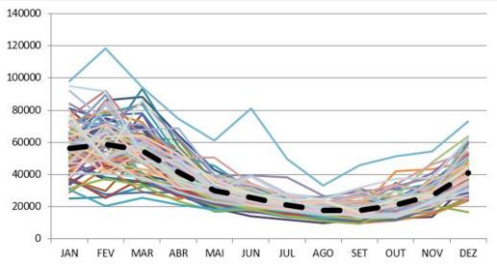




# INTRODUCTION

## RENEWABLES IN BRAZIL

One of the key models is *NEWAVE*, based on the Stochastic Dual Dynamic Programming – SDDP, which since 1998 has been used in official studies and real decision making regarding the Brazilian Interconnected Power System



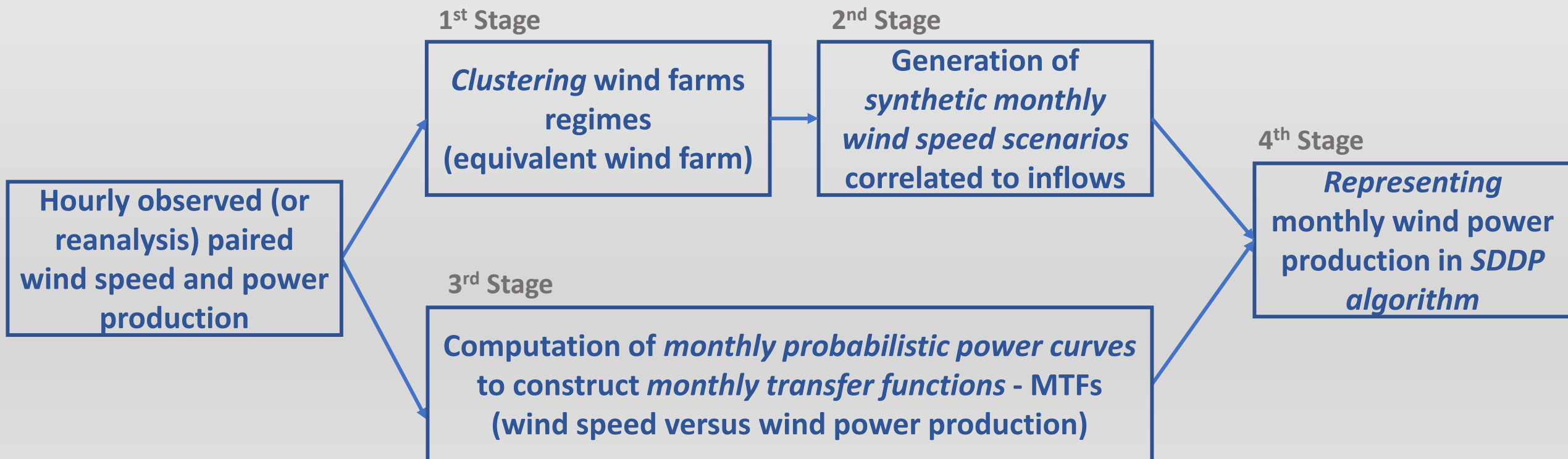
Source CEPEL adaptation

Currently, in accordance with the guidelines of the Electricity Regulatory Agency, the representation of wind power in the NEWAVE model is carried out in a simplified manner, based on the monthly average of the last five years of net generation of each wind farm (WF)

# COMBINING MONTHLY INFLOW AND WIND UNCERTAINTIES IN THE OPERATION PLANNING OF HYDRO-DOMINATED SYSTEMS

## OBJECTIVE

To describe an approach to be used by the Brazilian power industry to represent the uncertainties of monthly wind power in the SDDP algorithm applied in the long-term operation planning model, keeping the large-scale stochastic problem still computationally viable



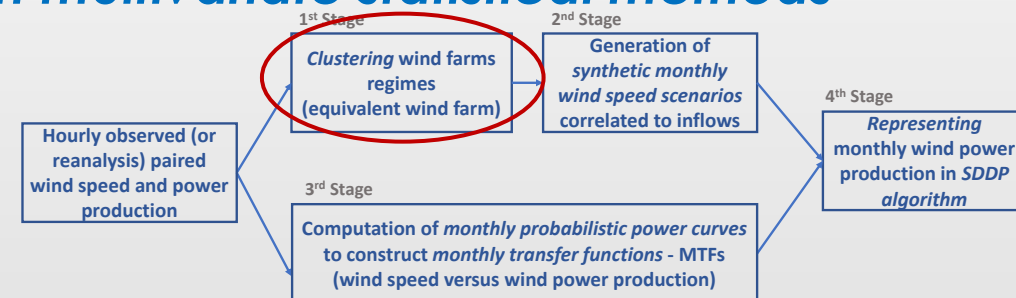
Schematic diagram of the proposed approach



# PROPOSED METHODOLOGY

## 1<sup>st</sup> STAGE - Statistical clustering of wind regimes based on multivariate statistical methods

- The Exploratory Factor Analysis technique is applied to the data matrix in which each column holds the time series wind speeds (**hourly or monthly**) in a wind farm.



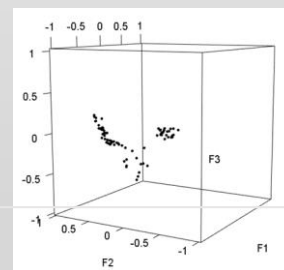
WIND SPEED

Exploratory  
Factor Analysis

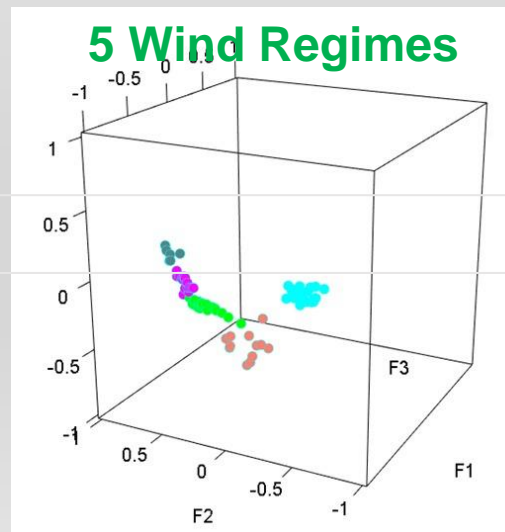
Clustering  
Analysis K-Means

Thus, the wind speed in each wind farm is expressed by the weighted sum of latent F-factors (**representing wind regimes**) plus a residual term  $\varepsilon$ , reducing the dimensionality of the data

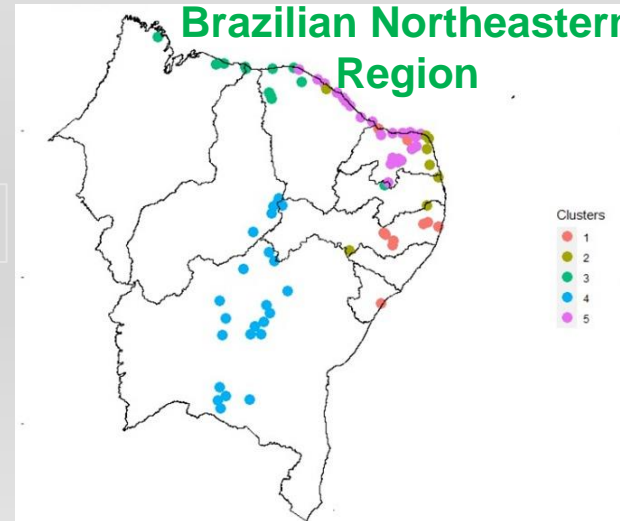
3 Latent F-factors



5 Wind Regimes



Brazilian Northeastern  
Region



- the identification of groups of wind farms with correlated wind regimes can be performed by means of statistical clustering analysis of, e.g., the K-Means or Ward algorithm

# PROPOSED METHODOLOGY

## 2nd STAGE - Integrated model for generating synthetic wind speed and inflow scenarios

### Inflows

Periodic autoregressive model of order p - PAR(p)

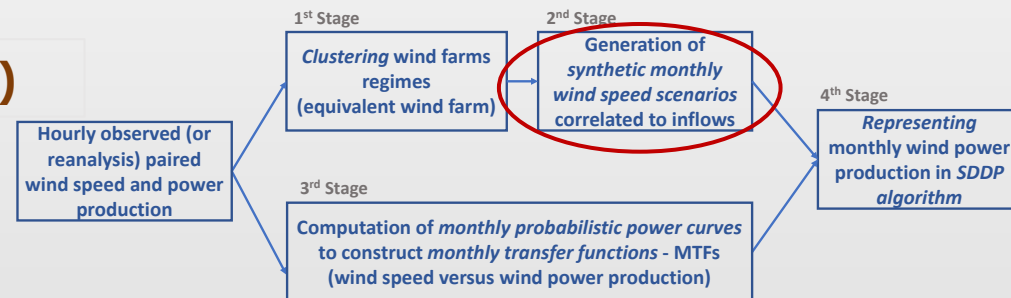
$$\left( \frac{ENA_{t,i} - \mu_{m,i}}{\sigma_{m,i}} \right) = \sum_{j=1}^{p_{m,i}} \phi_{t,j,i} \left( \frac{ENA_{t-j,i} - \mu_{m-j,i}}{\sigma_{m-j,i}} \right) + a_{t,i}$$

### Wind Speeds

$$\left( \frac{W_{t,j} - \mu_{m,j}^v}{\sigma_{m,j}^v} \right) = \text{regression component} + a_{t,j}$$

Positive skewed random noises  $(0, \sigma_a^2(m))$

Positive and negative skewed random noises  $(0, \sigma_a^2(m))$



•  $\mu_m^w$



Monthly wind records in several WFs of Brazil don't present monthly serial correlation

•  $\vartheta^m$

$$\left( \frac{W_{t-1} - \mu_{m-1}^w}{\sigma_{m-1}^w} \right)$$

For ones that present monthly serial correlation

•  $\varphi^m$

$$\left( \frac{ENA_t - \mu_m}{\sigma_m} \right)$$

Monthly wind records in several WFs of Brazil present monthly dependence with inflows to HPPs

Correlation between  $W_t$  and  $W_{t-1}$

Correlation between  $W_t$  and  $Z_t$

# PROPOSED METHODOLOGY

## 2nd STAGE - Integrated model for generating synthetic wind speed and inflow scenarios

### Inflows

Periodic autoregressive model of order p - PAR(p)

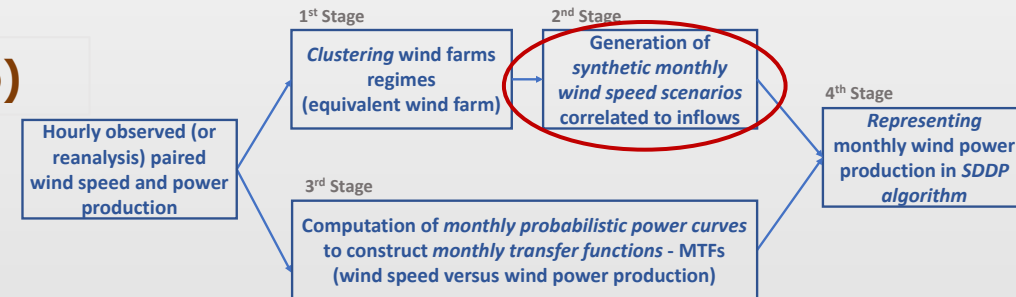
$$\left( \frac{ENA_{t,i} - \mu_{m,i}}{\sigma_{m,i}} \right) = \sum_{j=1}^{p_{m,i}} \phi_{t,j,i} \left( \frac{ENA_{t-j,i} - \mu_{m-j,i}}{\sigma_{m-j,i}} \right) + a_{t,i}$$

### Wind Speeds

$$\left( \frac{W_{t,j} - \mu_{m,j}^v}{\sigma_{m,j}^v} \right) = \text{regression component} + a_{t,j}$$

Positive skewed random noises ( $0, \sigma_a^2(m)$ )

Positive and negative skewed random noises ( $0, \sigma_a^2(m)$ )



- 100 thousand of uncorrelated  $N(0,1)$  random noises  $a_t$  are generated for the HPPs and EWFs
- K-Means method is applied to reduce the cardinality of the original sample

## To generate correlated monthly inflows and wind speeds

- The random noises (HPP and WF) are transformed in spatially correlated noises by applying the correlation matrix

Inflows x inflows; wind speeds x wind speeds; inflows x wind speeds

# PROPOSED METHODOLOGY

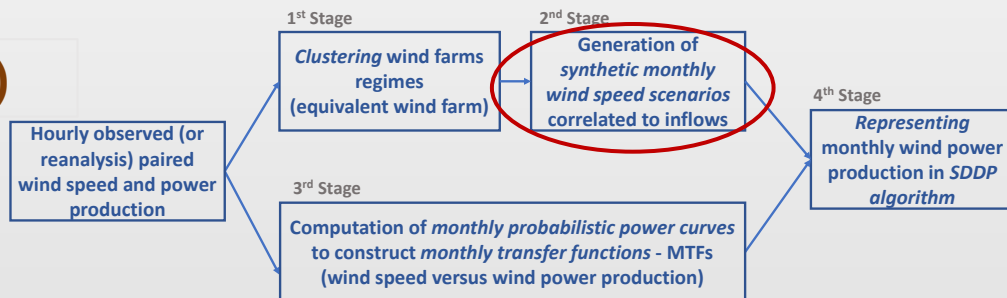
## 2nd STAGE - Integrated model for generating synthetic wind speed and inflow scenarios

### Inflows

Periodic autoregressive model of order p - PAR(p)

$$\left( \frac{ENA_{t,i} - \mu_{m,i}}{\sigma_{m,i}} \right) = \sum_{j=1}^{p_{m,i}} \phi_{t,j,i} \left( \frac{ENA_{t-j,i} - \mu_{m-j,i}}{\sigma_{m-j,i}} \right) + a_{t,i}$$

A 3-parameter Lognormal distribution is fitted to the spatially correlated residuals to better reproduce the observed positive skewness

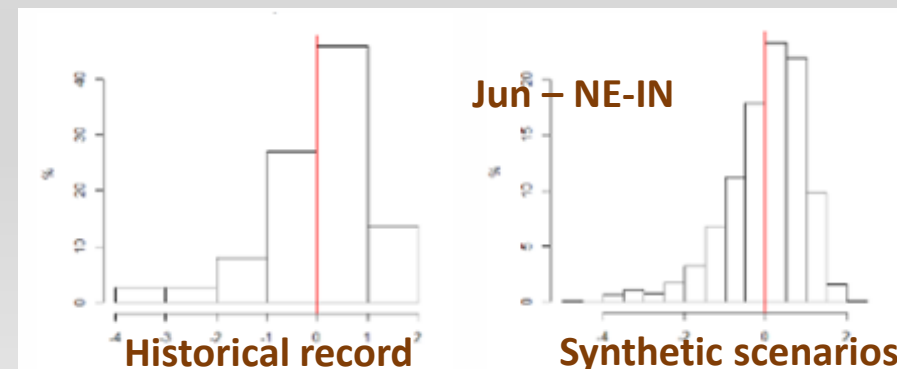
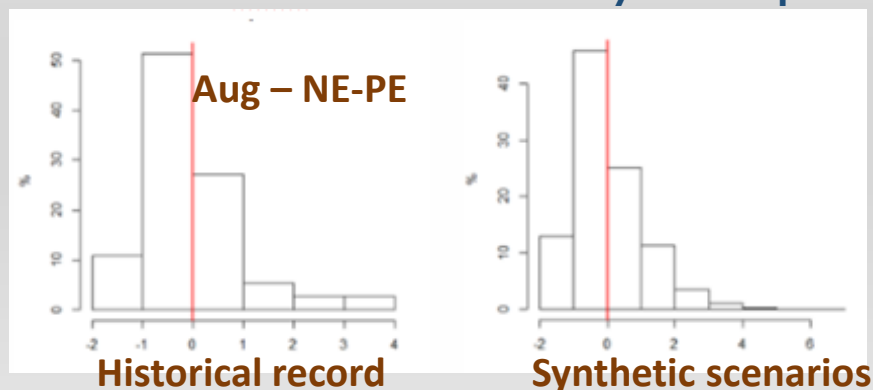


### Wind Speeds

$$\left( \frac{W_{t,j} - \mu_{m,j}^v}{\sigma_{m,j}^v} \right) = \text{regression component} + a_{t,j}$$

The monthly wind speed residuals can present positive as well as negative skewness

a 3-parameter Weibull distribution is then used  
a special purpose algorithm was developed





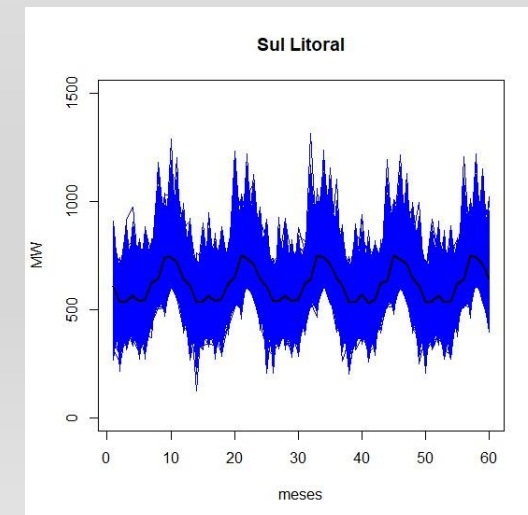
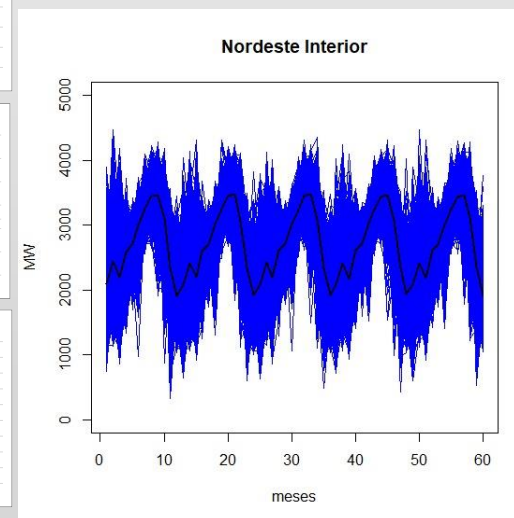
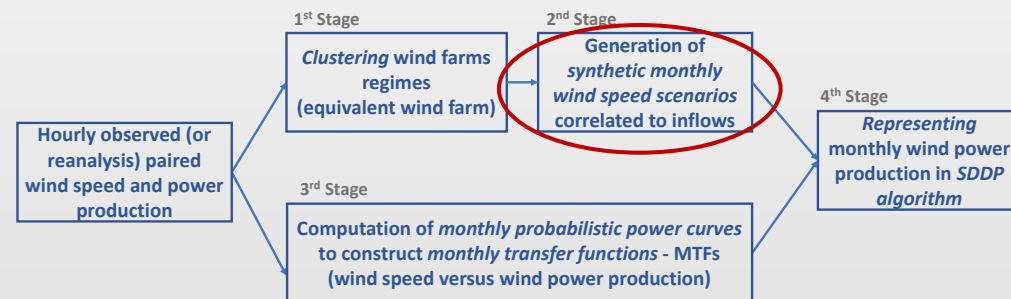
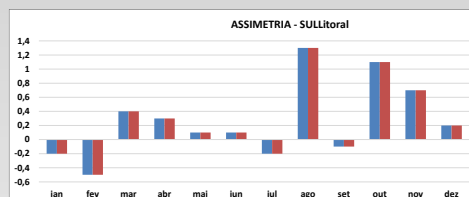
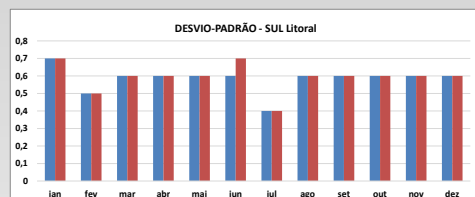
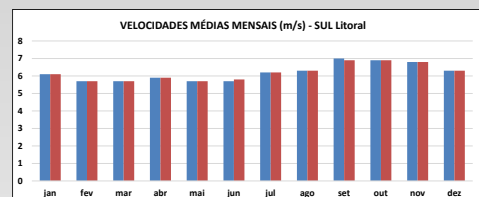
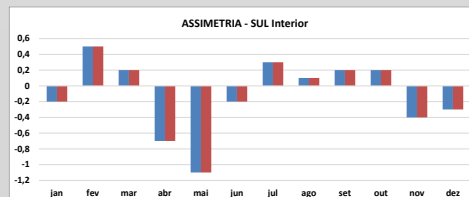
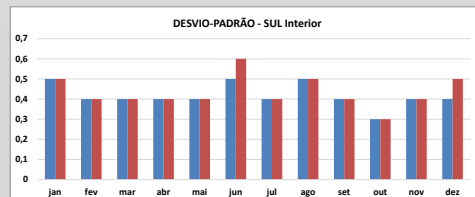
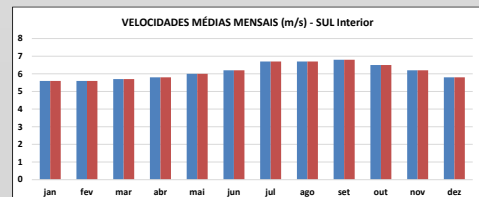
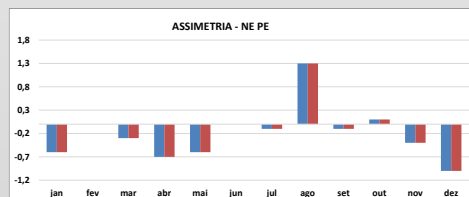
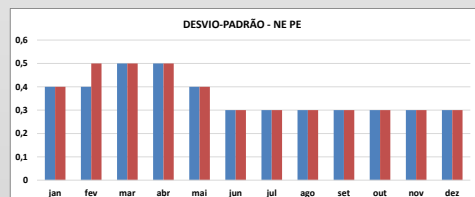
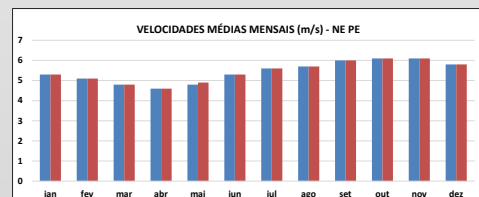
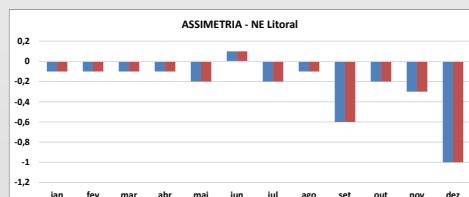
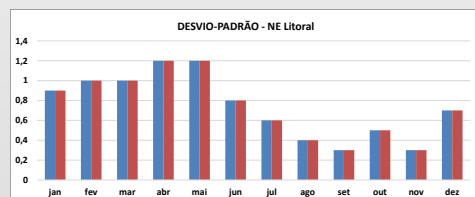
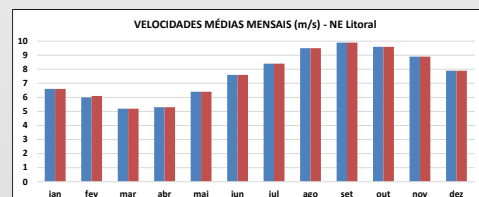
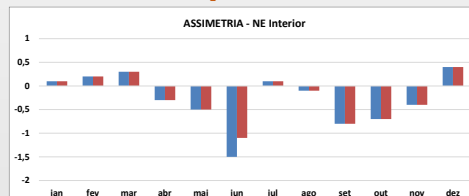
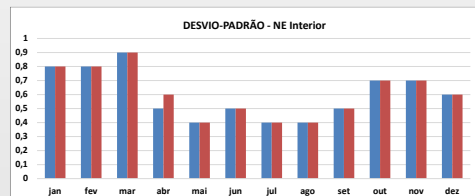
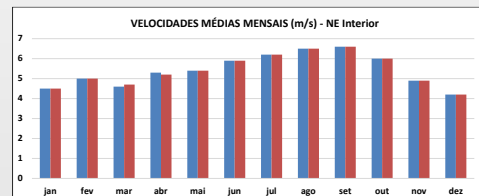
# PROPOSED METHODOLOGY

## 2nd STAGE - Integrated model for generating synthetic wind speed and inflow scenarios

### Monthly Average

### Monthly Standard Deviation

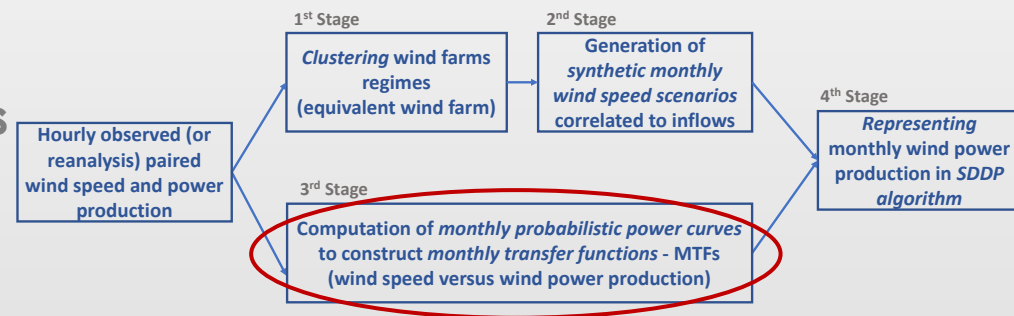
### Monthly Skewness



# PROPOSED METHODOLOGY

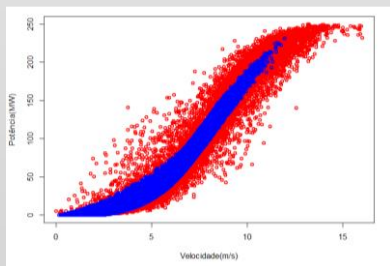
## 3rd STAGE - Construction of Monthly Transfer Functions (MTFs) between wind speed and wind power production

MTFs - mathematical functions, that relate the monthly averages of wind speed with the monthly averages of energy production in each equivalent wind farm

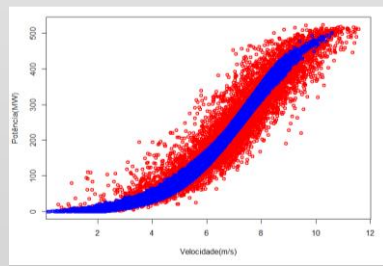


From paired data of wind speed and wind power:

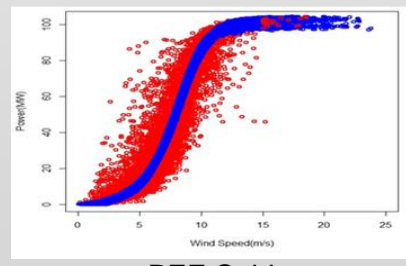
### Probabilistic Power Curves – Hourly



PEE NE-I



PEE NE-PE

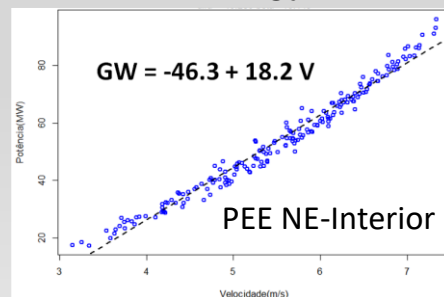


PEE Sul-L

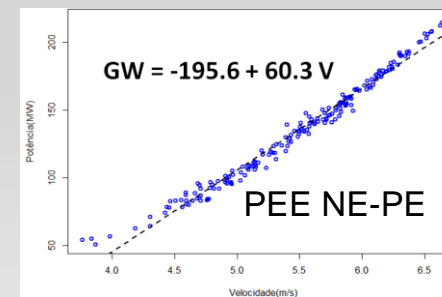
MTFs are obtained through *linear regression models* - simple or piecewise - adjusted to the monthly probabilistic power curves of each (equivalent) wind farm

### Probabilistic Power Curves – Monthly

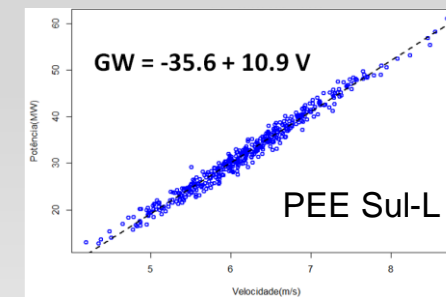
High correlations (above 98,5%)



PEE NE-Interior



PEE NE-PE



PEE Sul-L

# PROPOSED METHODOLOGY

## 4th STAGE - Representing monthly wind production in the SDDP algorithm

### Objective Function

$$z_t = \min \sum_{m=1}^{NSBM} \left( \sum_{c=1}^{NPMC} \left( \sum_{j=1}^{NUT_m} cterm_{t,m,j} \cdot GT_{t,m,j,c} \right) + \sum_{idef=1}^{NPDF} CDEF_{t,idef} \cdot DEF_{t,m,idef,c} \right) + \sum_{v=1}^{nviol \in NSBM, NREE} c_{t,v} \cdot viol_{t,m,k,c} + \frac{1}{1+\beta} \cdot \alpha_{t+1}$$

### Load supply equation in subsystem $m$ in the load level $c$ and period $t$

$$\sum_{k \in NREE_m} (GH_{t,c,k} + fpeng_{t,c} GFIO_{t,c,k}) + \sum_{j \in NUT_m} GT_{t,c,j} + \sum_{j=1, j \neq m}^{NSBM} (INT_{t,c}(j, k) - INT_{t,c}(k, i)) + DEF_{t,c,m} - EXC_{t,c,m} + \sum_{u=1}^{NPEE_m} GW_{t,u,c} = merc_{t,m,c} - \left( submot_{t,m} + pqusi_{t,m} + \sum_{j \in NUT_m} gtmin_{t,m,j} \right) \cdot fpeng_{t,c}$$

### Controllable energy balance equation in REE $k$ and period $t$

$$EA_{t+1,k} = FDIN_{t,k} EA_{t,k} + FC_{t,k} EC_{t,k} - GH_{t,c,k} - EVT_{t,k} - EVP_{t,k} - EDVC_{t,k}$$

### Wind power production through the MTFs in WF/EFW $u$ (simple linear regression) in WF/EFW $u$ and period $t$

$$\sum_{c=1}^{NPMC} GW_{t,u,c} \leq b_{t,u}^W + a_{t,u}^W V_{t,u}$$

### Set of multivariate linear constraints (Benders cut) representing the cost-to-go function

$$\alpha_{t+1} - \sum_{k \in NREE} \bar{\pi}_{EA_{1,t+1,k}} EA_{t+1,k} + \sum_{j=1}^p \bar{\pi}_{EAF_{1,j,t+1,k}} EAF_{t-j+1,k} \geq \bar{\delta}_{1,t+1}$$

Hourly observed (or reanalysis) paired wind speed and power production

1<sup>st</sup> Stage

Clustering wind farms regimes (equivalent wind farm)

2<sup>nd</sup> Stage

Generation of synthetic monthly wind speed scenarios correlated to inflows

4<sup>th</sup> Stage

Representing monthly wind power production in SDDP algorithm

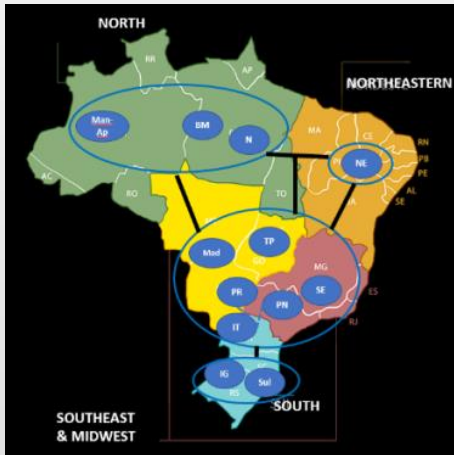
3<sup>rd</sup> Stage

Computation of monthly probabilistic power curves to construct monthly transfer functions - MTFs (wind speed versus wind power production)

The wind production is represented in the SDDP dispatch problem as an available generation source with null operating cost

The MTFs are used with the synthetic monthly wind speed scenarios to obtain the wind power production. The Benders cuts of SDDP algorithm must incorporate a new term related to the dependence of the wind speed with the inflows, depending on the adopted *regression component*

# COMPARING THE OPERATION POLICIES



## 1<sup>st</sup> Case - Without uncertainty

**Average monthly wind power** of the Northeast and South subsystems were determined by applying the MTFs of the 5 EWFs to their respective historical monthly wind speeds and then obtaining the monthly averages of the resulting values

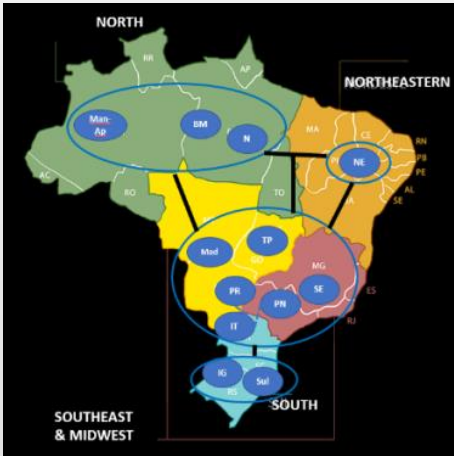
**Generation of non-dispatched plants in NEWAVE to emulate the approved current procedures**

## 2<sup>nd</sup> Case - With uncertainty

**Wind power uncertainty** was modeled through the generation of synthetic sequences of monthly average wind speeds in the EWFs for the *backward* and *forward* passes of the SDDP algorithm and also for the final simulation

Then they are transformed into synthetic sequences of wind power through the MTFs, which are also explicitly used in each operation dispatch problems

# COMPARING THE OPERATION POLICIES



System performance indices are obtained with a simulation of the system operation with 2,000 synthetic wind and inflow scenarios

Expected Total Operation Cost, Annual Deficit Risk, Annual EENS

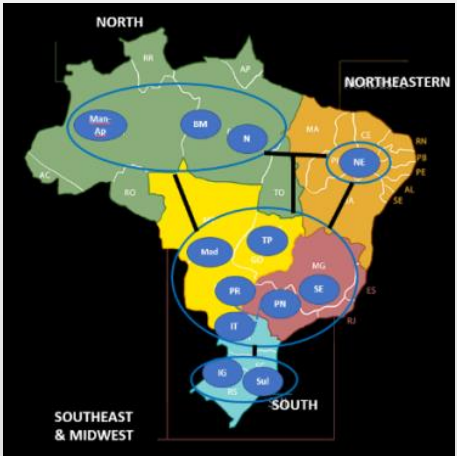
YEAR	SOUTHEAST		SOUTH		NORTHEAST		NORTH	
	RISK	EENS	RISK	EENS	RISK	EENS	RISK	EENS
	%	MWMONTH	%	MWMONTH	%	MWMONTH	%	MWMONTH
Without_Uncertainty_Case								
Expected Total Operation Cost = 25,790.54								
2021	0,2	1,4	0,1	0,2	0,0	0,0	0,0	0,0
2022	0,1	0,4	0,1	0,3	0,0	0,0	0,0	0,0

Reduction in the expected total operation cost of 2.16% (560 M R\$)

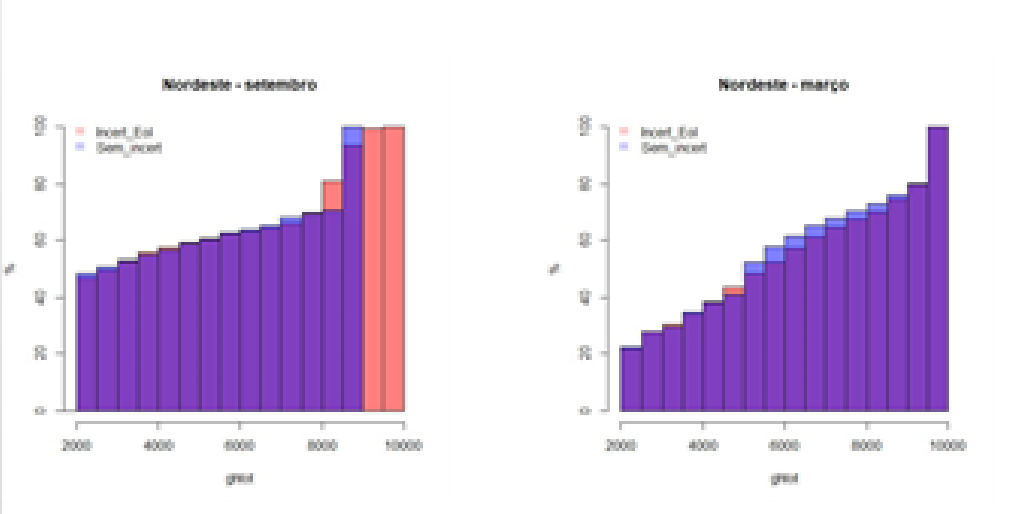
YEAR	SOUTHEAST		SOUTH		NORTHEAST		NORTH	
	RISK	EENS	RISK	EENS	RISK	EENS	RISK	EENS
	%	MWMONTH	%	MWMONTH	%	MWMONTH	%	MWMONTH
Uncertainty_Wind Case								
Expected Total Operation Cost = 25,234.37								
2021	0,3	0,5	0,1	0,2	0,0	0,0	0,0	0,0
2022	0,0	0,0	0,1	0,1	0,0	0,0	0,0	0,0



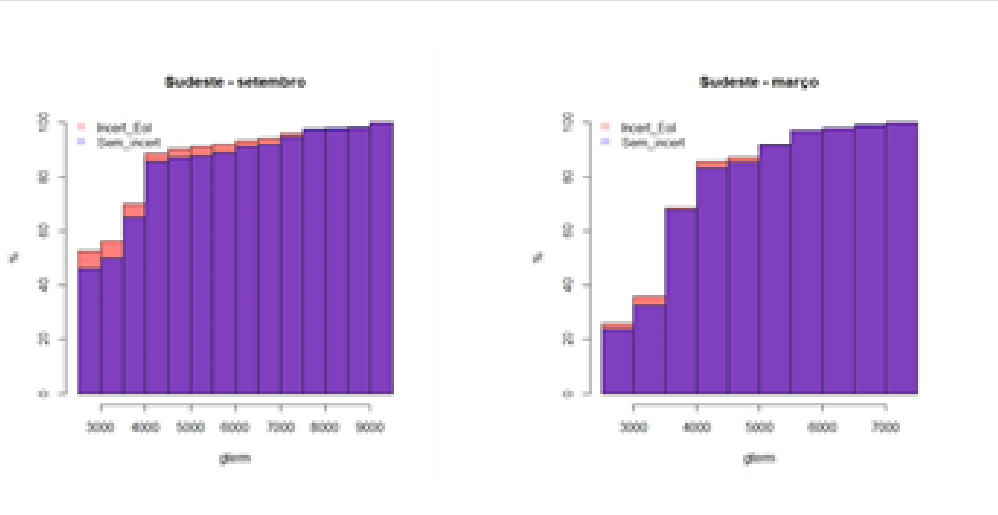
# COMPARING THE OPERATION POLICIES



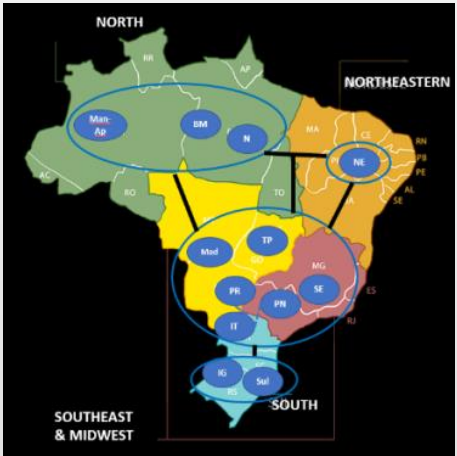
## Monthly Hydro Generation



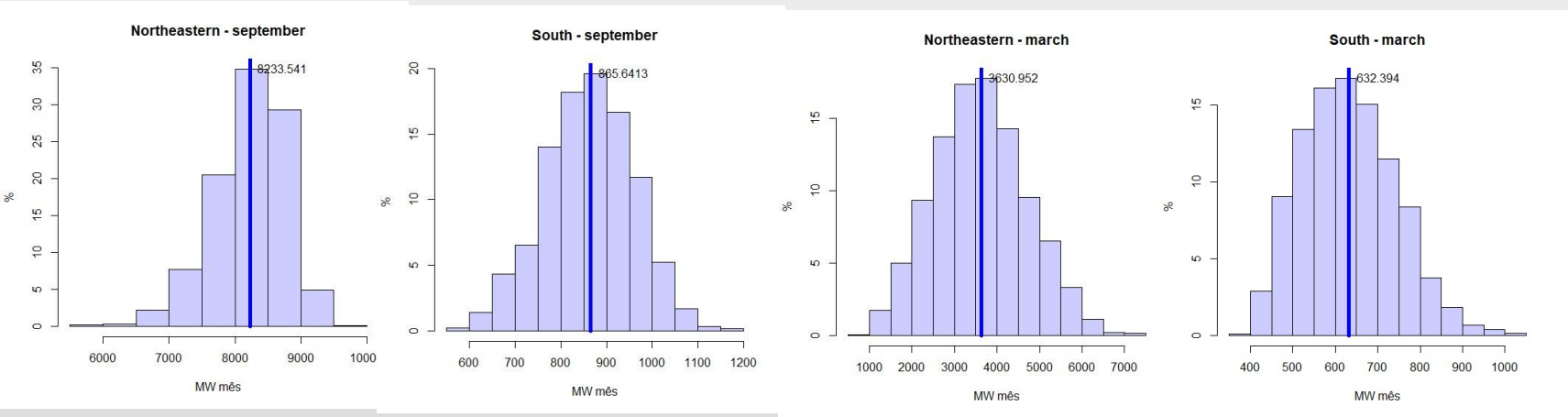
## Monthly Thermal Generation



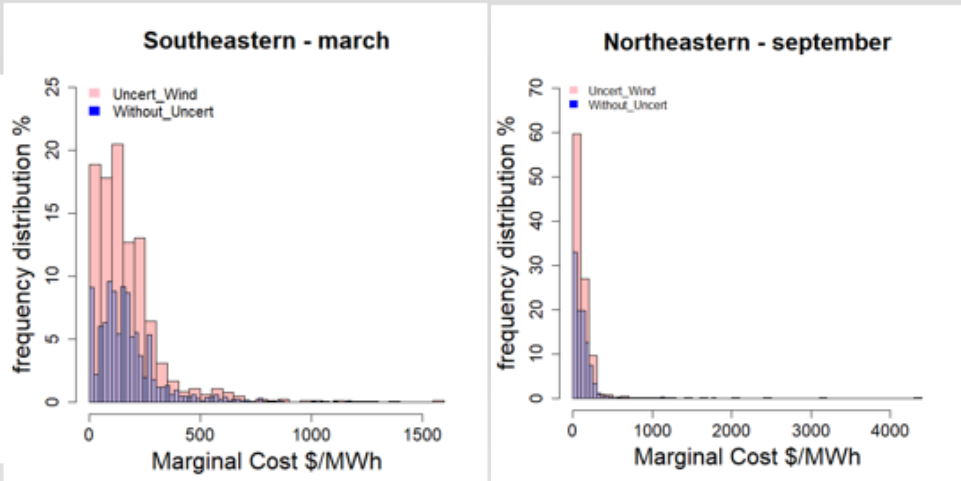
# COMPARING THE OPERATION POLICIES



## Frequency distribution of the synthetic wind power production



## Operation Marginal Cost - March



# CONCLUSIONS

**Currently**, in accordance with the guidelines of the Electricity Regulatory Agency, the representation of wind power in the **NEWAVE** model is carried out in a simplified manner

The objective of this work was to describe an approach to be used by the Brazilian power industry to represent the uncertainties of monthly wind power in the operation dispatch problem, solved by SDDP algorithm

- (i) statistical **clustering of wind regimes** and definition of EWFs;
- (ii) an **integrated model** for the **generation of monthly multivariate synthetic sequences of inflows** and **winds**, considering the correlations between wind speeds, between inflows and between wind speeds and inflows;
- (iii) evaluation of **monthly transfer functions** (MTFs) between wind speed and power production
- (iv) representing **monthly wind power** through MTFs, to be used in the **SDDP algorithm**.



**Thank you!**

The effectiveness of the proposed approach was illustrated with a real configuration of the Brazilian interconnected system