

# Floating Wind Turbines

Paul D. Sclavounos

Professor of Mechanical Engineering and Naval Architecture  
Department of Mechanical Engineering  
Massachusetts Institute of Technology

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# Floating Wind Turbines

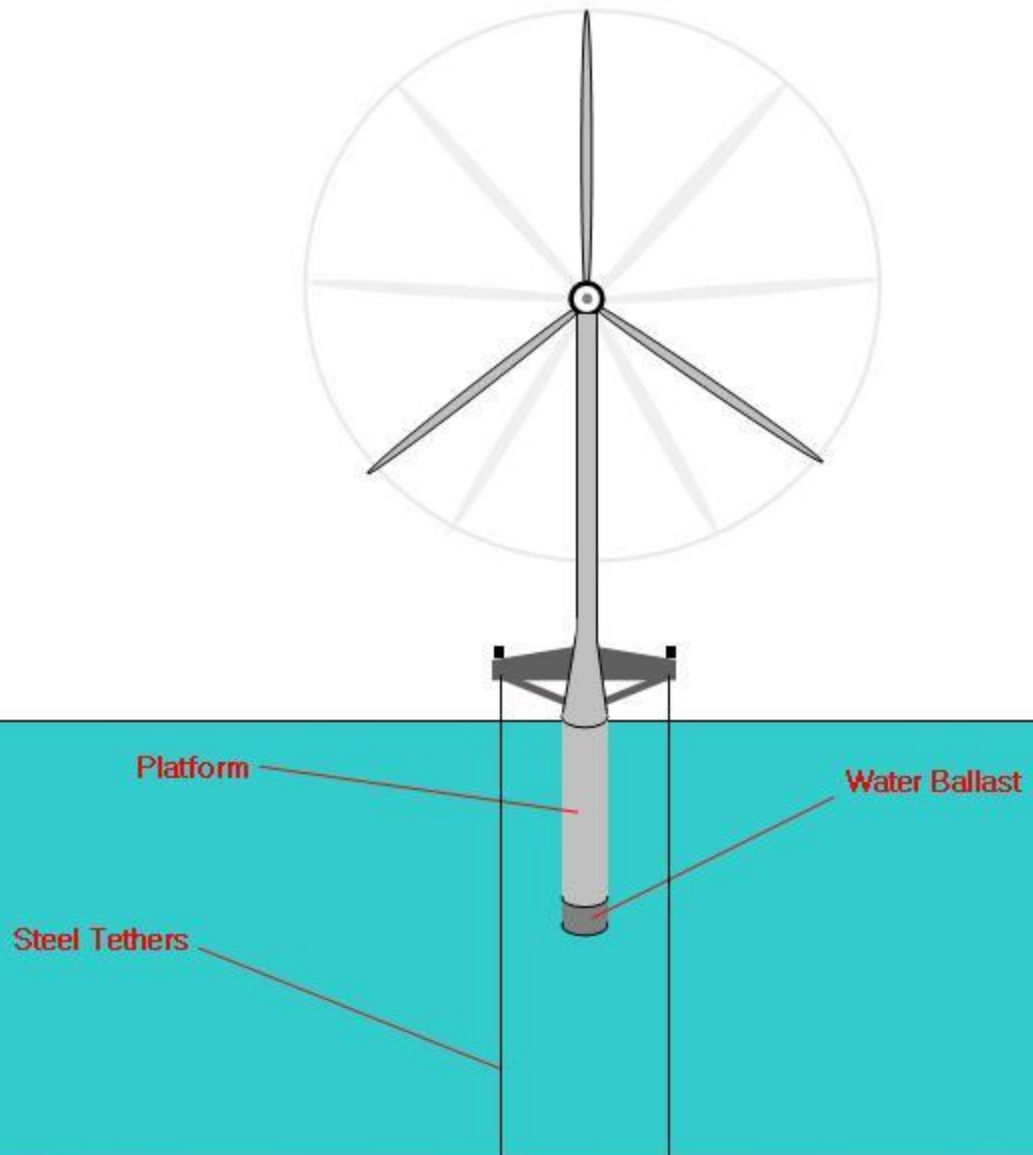
- Vast Offshore Sites Available for Wind Resource Development
- Offshore Siting Mitigates Visual, Noise and Flicker Impact
- Coastal Assembly – Low Cost Float-out Operation
- Floater Cost Lower than Turbine Cost per Marginal MW
- Fault Tolerant Efficient Operation using Turbine Controls
- Larger Turbines on Fewer Floaters – Low O&M Costs per MW

# Floating Wind Turbine Prototypes



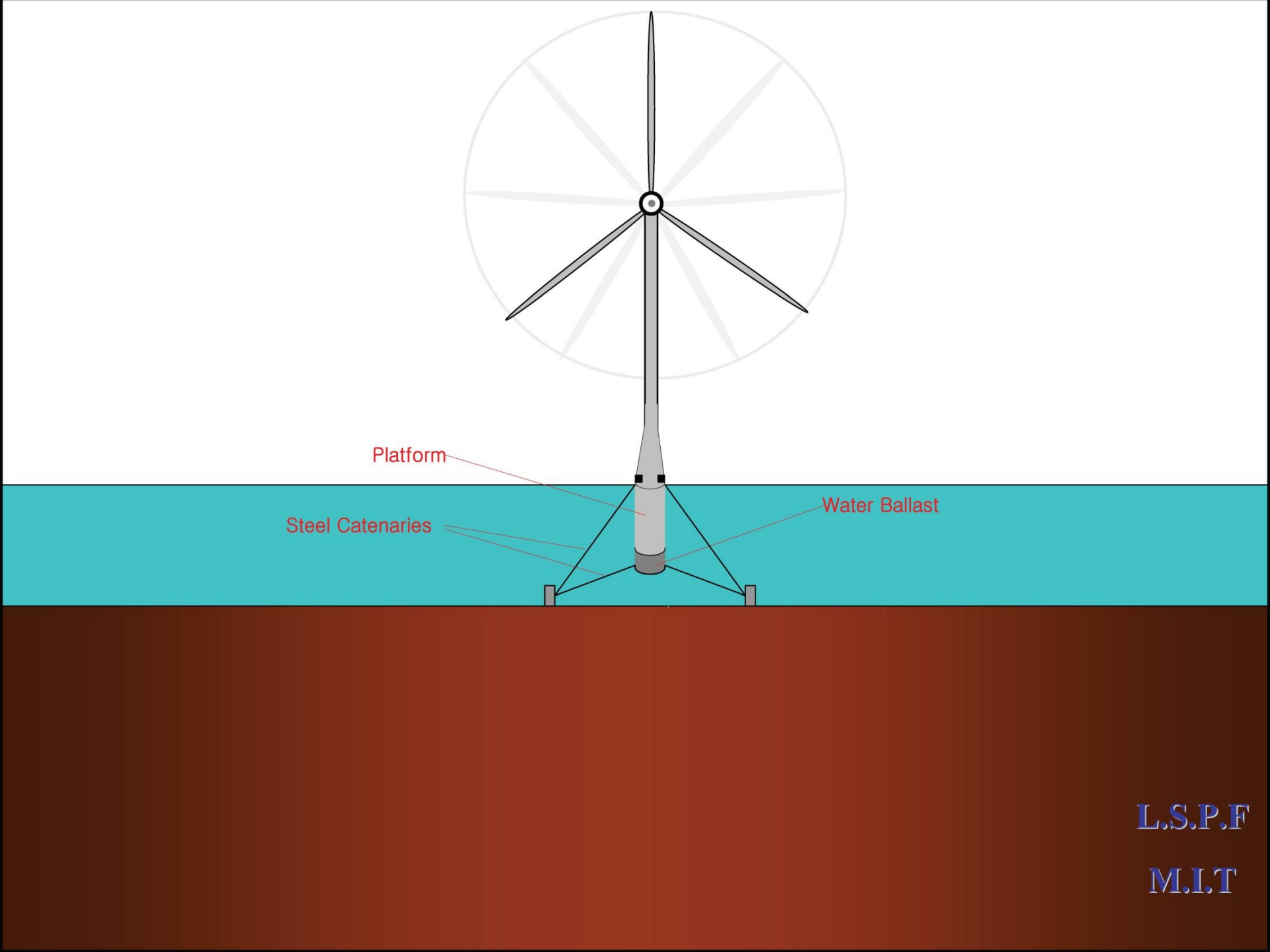
# Hydrodynamics

- Frequency Domain Preliminary Design Analysis
- State-Space Formulation of Free Surface Hydrodynamics
- Generalized Morison Equation with Memory Effects
- Fluid Impulse Theory for Nonlinear Loads
- Ringing Loads
- Efficient Computation – Nonlinear Statistics



L.S.P.F

MIT



Platform

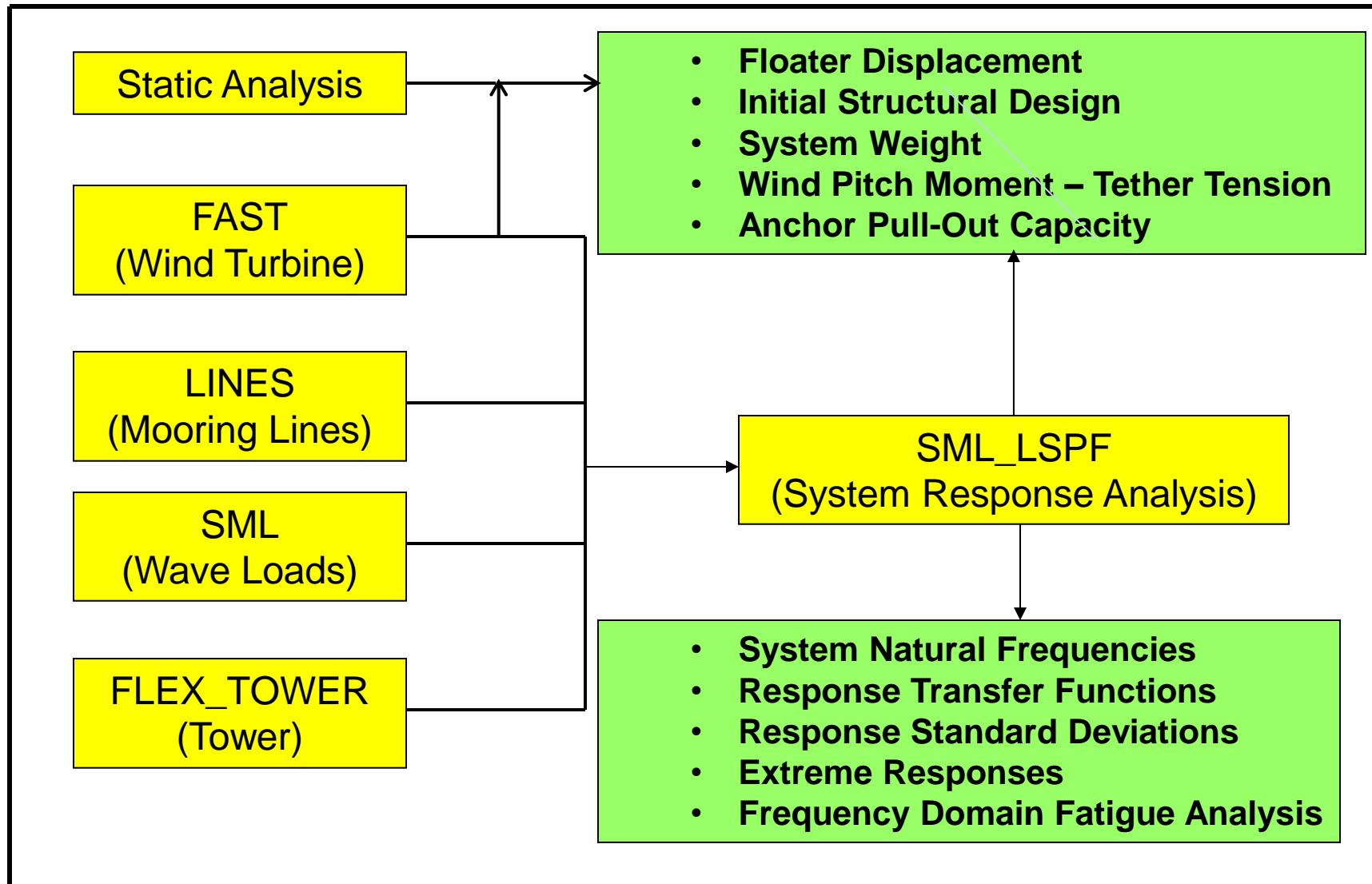
Steel Catenaries

Water Ballast

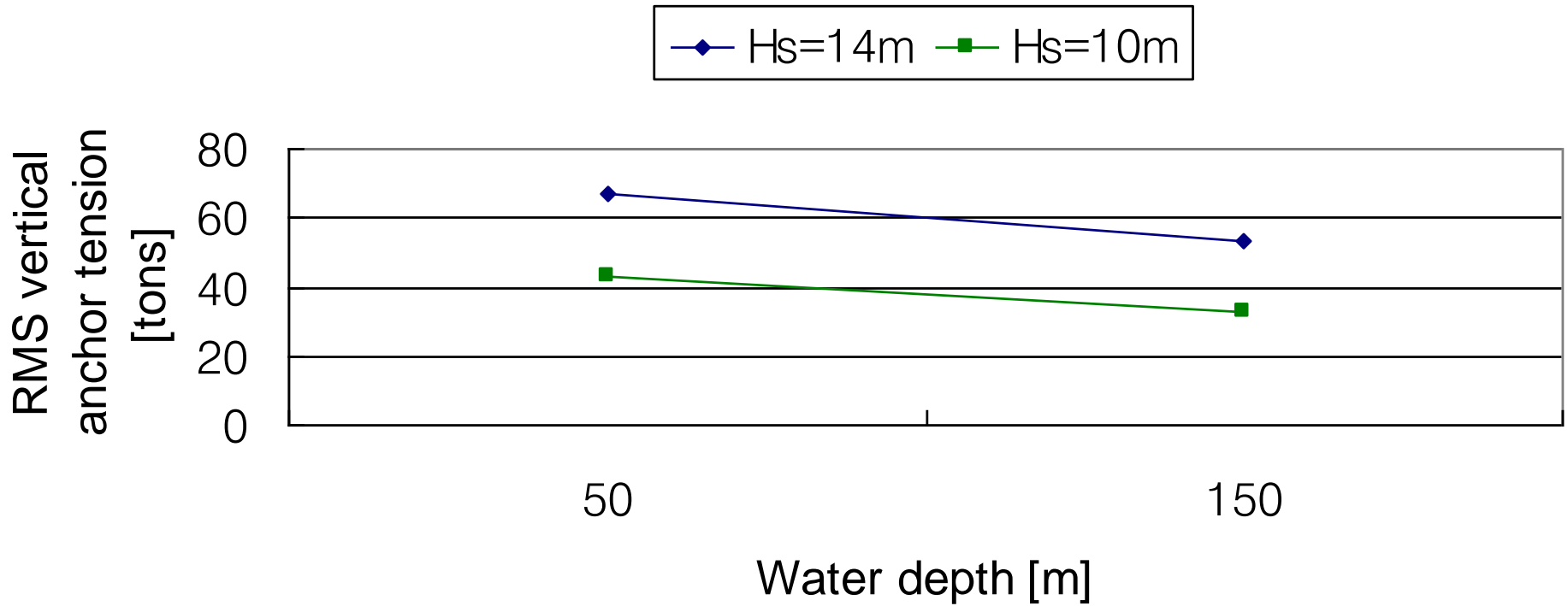
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M.I.T

# Dynamic Analysis of Floating Wind Turbines



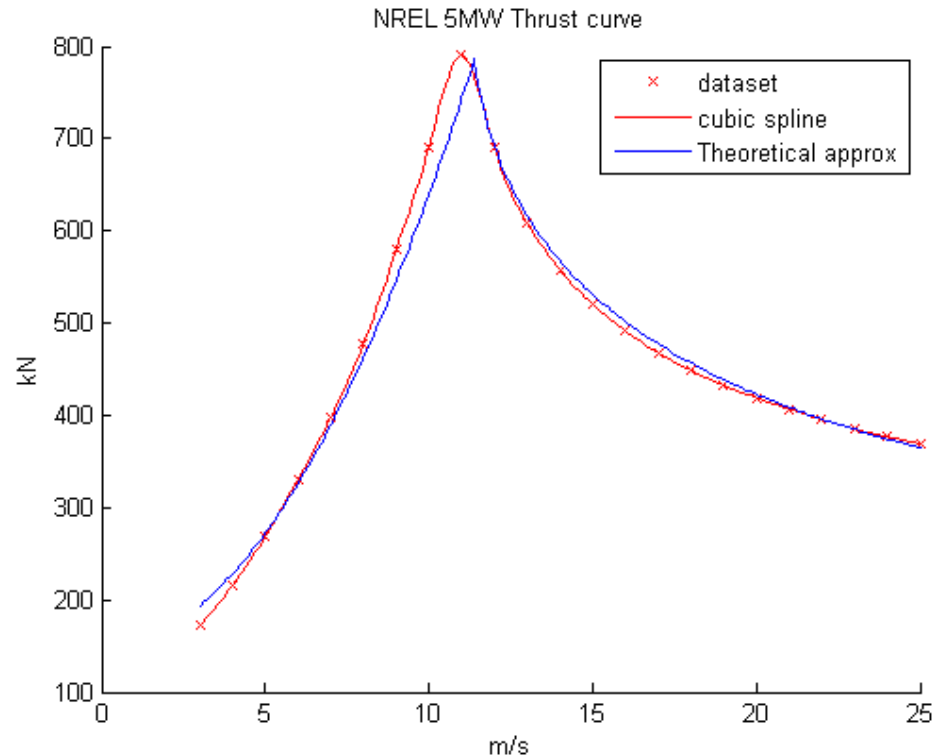
# RMS Vertical Anchor Tension at Windward Side



3 MW TLP Floating Wind Turbine



# Wind Turbine and Floater Damping



$$B_{TURBINE}(U) = \frac{dT}{dU}; \quad B_{BUOY} = \frac{1}{2} \rho C_d S \sqrt{\frac{8}{\pi}} \sigma_v; \quad \text{Damping Ratio}=0.23 \text{ at } U=10 \text{ m/s; } H_s=6\text{m}$$

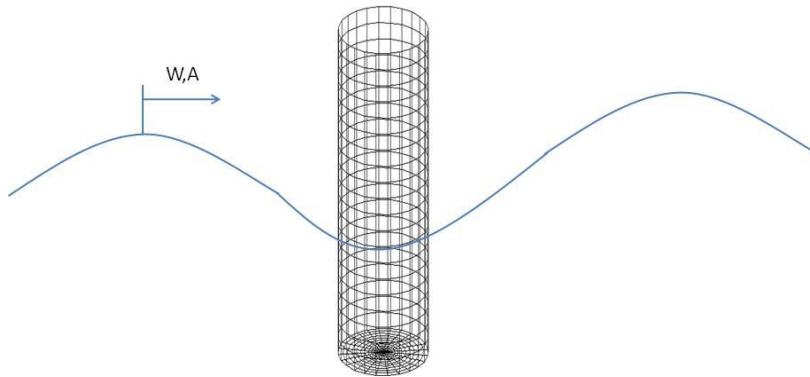
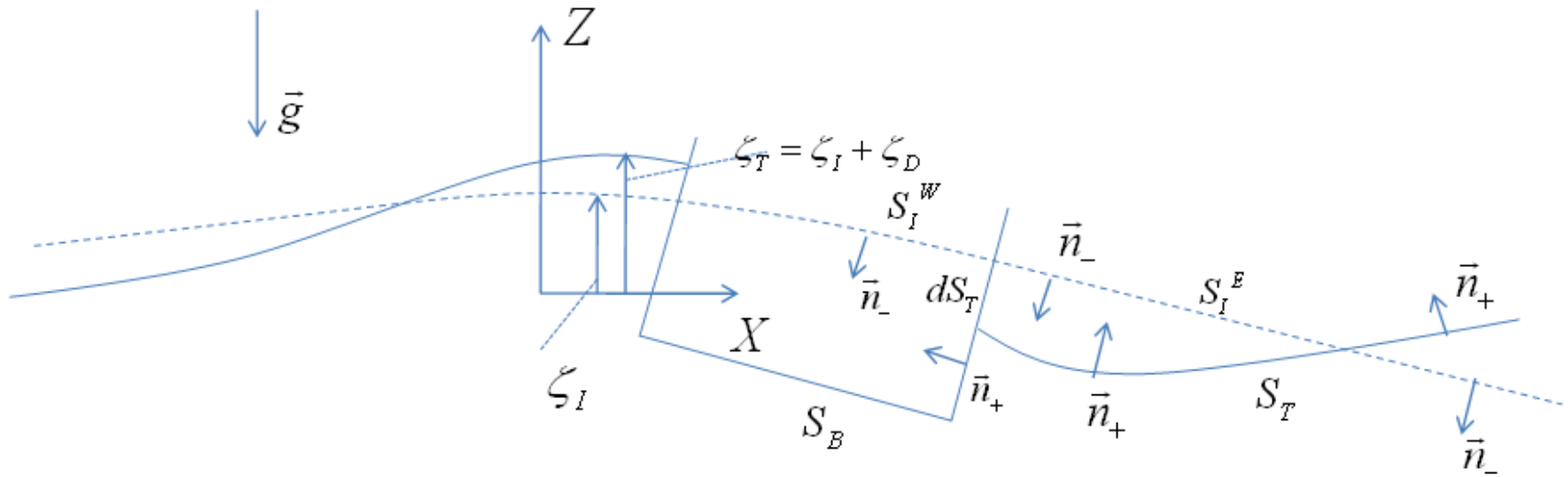
$$\text{Damping Ratio}=0.15 \text{ at } U=15 \text{ m/s; } H_s=6\text{m}$$

Nielsen et. al. (OMAE, 2006), Jonkman (Wind Energy, 2008)

# Wave Energy Extraction Potential – NREL 5MW

NREL – 5 MW – TLP platform					
<i>Buoy characteristics</i>					
		Draft	30 m	Draft	15 m
		Radius	4.75 m	Radius	6.72 m
Depth	Conditions	Additional Power (+% of turbine power at that wind speed)			
50 m	Sig. Wave H. [m]	6	10	6	10
	Mean Period [s]	11.6	13.6	11.6	13.6
	Wind 6 m/s	+3.13%	+8.94%	+4.92%	+13.5%
	Wind 8 m/s	+2.47%	+6.73%	+3.89%	+10.2%
	Wind 10 m/s	+2.29%	+5.59%	+3.58%	+8.33%
100 m	Sig. Wave H. [m]	6	10	6	10
	Mean Period [s]	11.6	13.6	11.6	13.6
	Wind 6 m/s	+2.3%	+6.46%	+3.55%	+9.5%
	Wind 8 m/s	+1.74%	+4.83%	+2.69%	+7.11%
	Wind 10 m/s	+1.51%	+4.06%	+2.34%	+5.98%

# Nonlinear Time Domain Loads



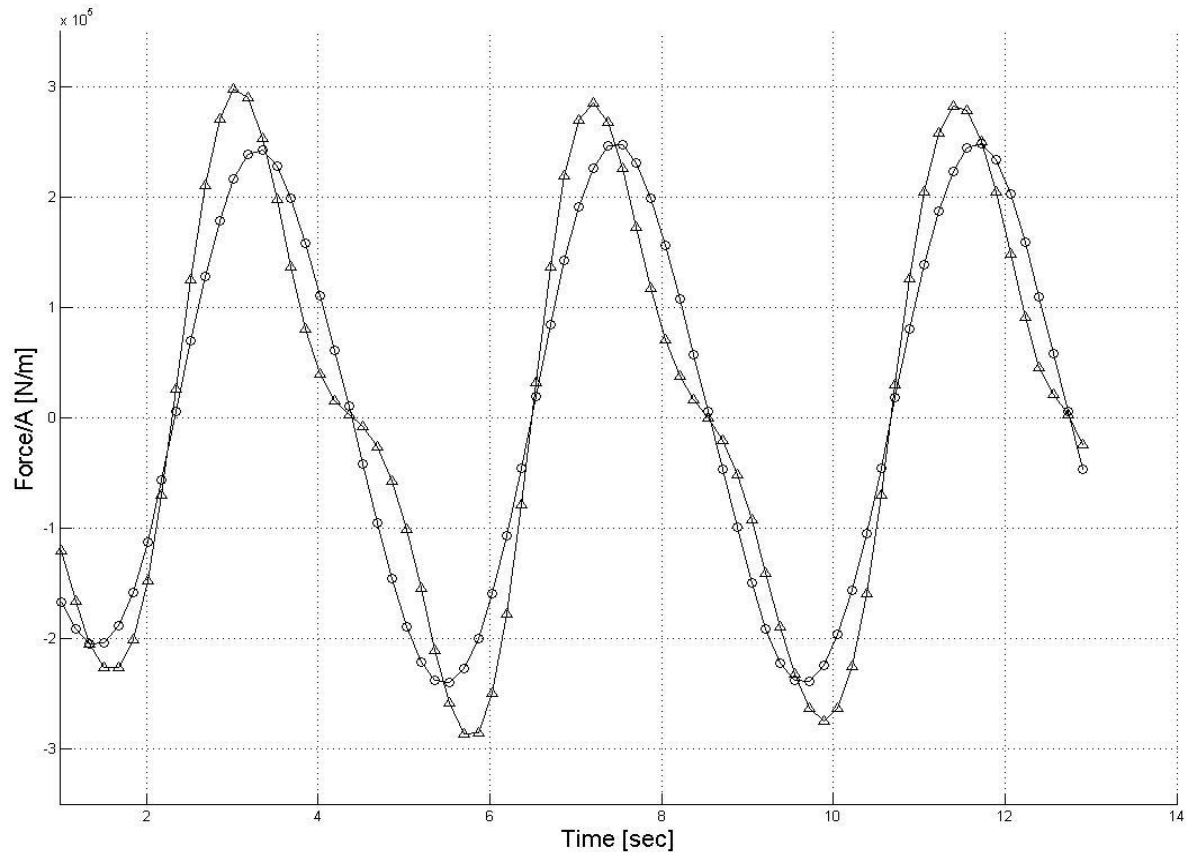
Cylinder Diameter:  $d$   
 Wave Amplitude:  $A$   
 Wavenumber:  $k$

# Nonlinear Fluid Impulse Hydrodynamic Force

$$\vec{F}(t) = \vec{F}_1(t) + \vec{F}_2(t)$$

$$\vec{F}_1(t) = \underbrace{-\rho g \int_{S_B^W(t)+S_I^W(t)} Z \vec{n} ds}_{\text{Buoyancy force}} - \underbrace{\rho \frac{d}{dt} \int_{S_B^W(t)+S_I^W(t)} \varphi_I \vec{n} ds}_{\text{Froude-Krylov Impulse Force}} - \underbrace{\rho \frac{d}{dt} \int_{S_B^W(t)} \varphi_D \vec{n} ds}_{\text{Radiation and Diffraction Body Impulse Force}}$$

$$\vec{F}_2(t) = \left. \begin{aligned} &-\rho \frac{d}{dt} \int_{S_I^E(t)} \varphi_D \vec{n} ds - \rho g \vec{k} \int_{S_I^E(t)} \zeta_D ds \\ &-\rho \frac{d}{dt} \iiint_{v(t)} (\nabla \varphi_I + \nabla \varphi_D) \text{sgn}(\zeta_D) dv \end{aligned} \right\} \begin{aligned} &\text{Radiation and Diffraction} \\ &\text{Free Surface Impulse Force} \\ &\text{Slow Drift, Springing and} \\ &\text{Ringing Loads} \end{aligned}$$



Nonlinear Surge exciting force in an ambient wave with  $kA=0.4$  and  $kd=0.9$ . Triangles: Bernoulli Force; Circles: Body Impulse Force  $F_1$ .

# Controls

- State-Space Model of Floating Wind Turbine Dynamics
- Unsteady Linear Quadratic Controller – Conjugate Control
- Energy Yield Enhancement by Blade Pitch and Torque Control
- Forecasting of Wave Elevation and Exciting Forces
- Load Mitigation and Damping at Above Rated Wind Speeds
- Energy Yield Increase by LIDAR Forecasting of Wind Speed

# State-Space Model of Floater and Wind Turbine Dynamics

- Surge Equation of Motion in the Time-Domain:

$$[M + A_\infty] \ddot{\xi}(t) + \int_0^t K(t-\tau) \cdot \dot{\xi}(\tau) d\tau + B_V \dot{\xi} + C\xi(t) = X(t) + F_T(t, \vec{u})$$

$$K(s) = \frac{p_r s^r + p_{r-1} s^{r-1} + \dots + p_0}{s^n + q_{n-1} s^{n-1} + \dots + q_0}$$

- Equation of Motion of Rotor and Generator:

$$I \frac{d\Omega}{dt} = T_{Aero}(t, \vec{u}) - \eta T_{Gen}(\Omega); \quad \eta = \Omega_{Gen} / \Omega; \quad I = I_{Rotor} + \eta^2 I_{Gen}$$

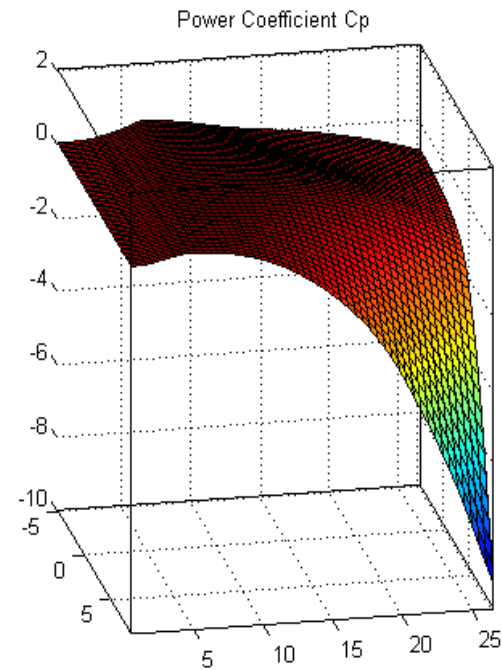
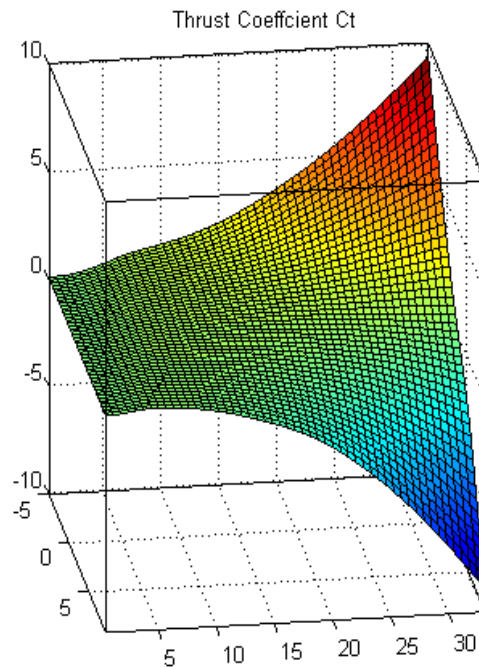
- State-Space Model of System:

$$\dot{\vec{x}} = [A] \vec{x} + \vec{X} + [B_W] \vec{u}$$

# Aerodynamic Model

$$T_{Aero} = \frac{P}{\Omega} = \frac{1}{2} \rho_A S_R C_P (\lambda, \theta) \cdot \frac{(V_\infty - \dot{\xi})^3}{\Omega};$$

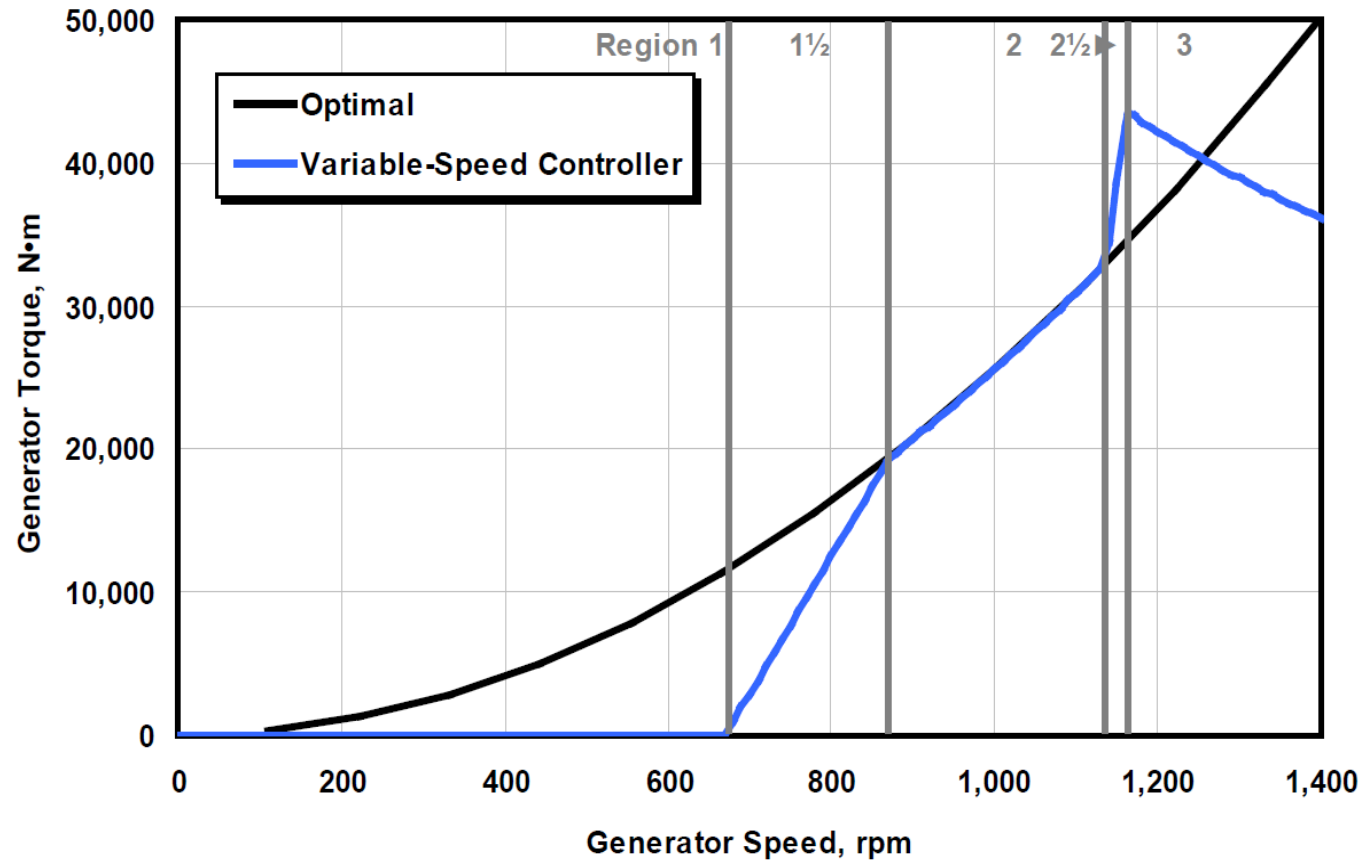
$$F_T = \frac{1}{2} \rho_A S_R C_T (\lambda, \theta) \cdot (V_\infty - \dot{\xi})^2$$

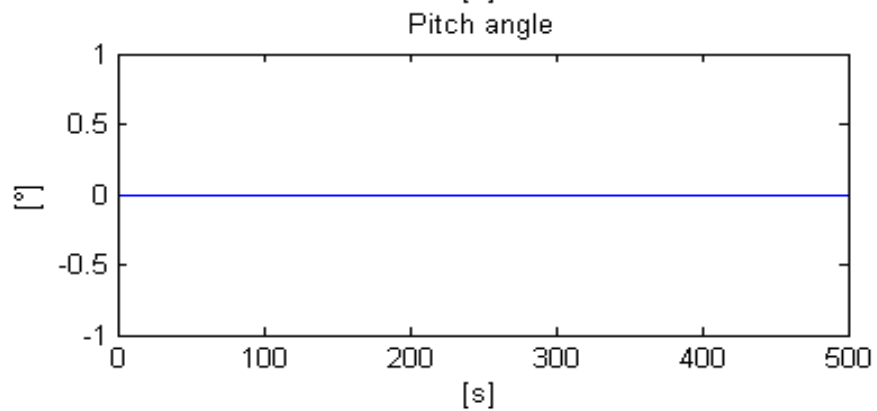
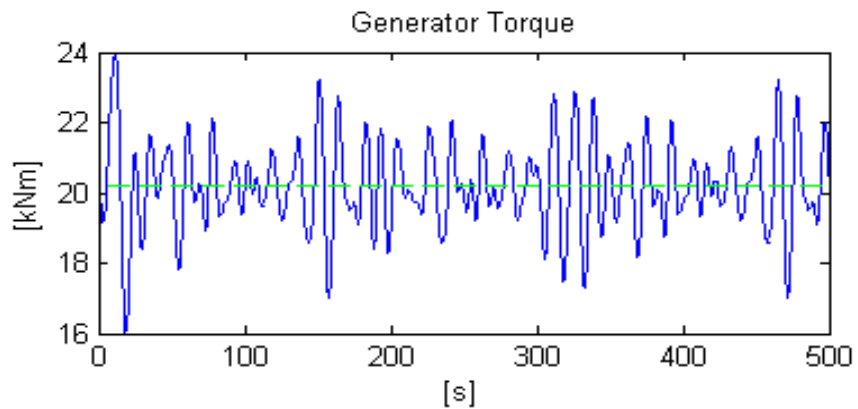


$C_t$  and  $C_p$  Surfaces of NREL 5 MW Turbine

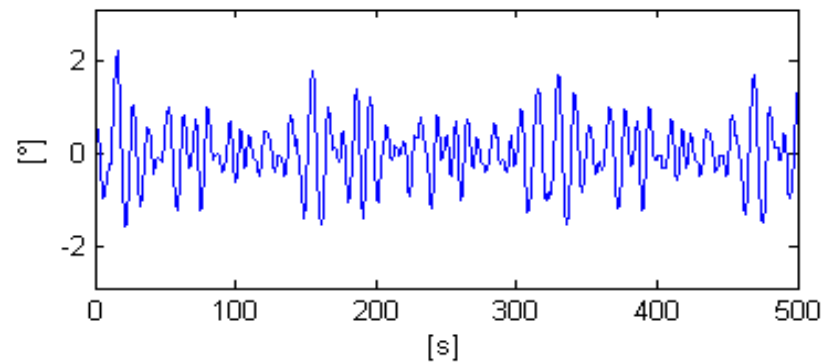
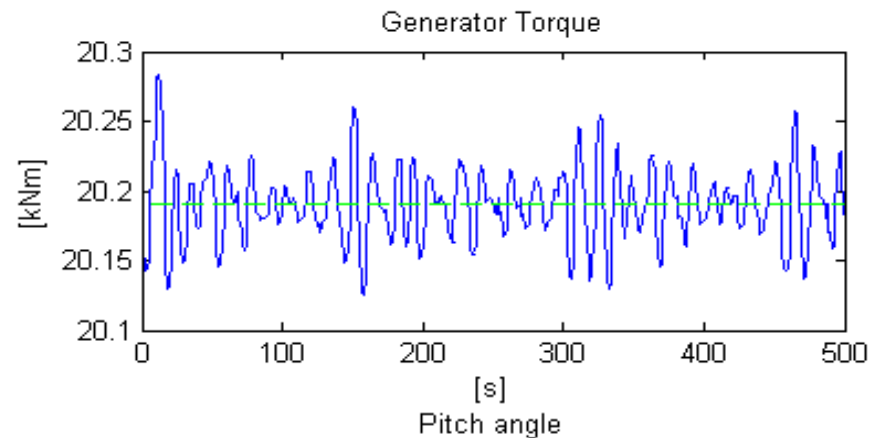


# NREL Torque Controller

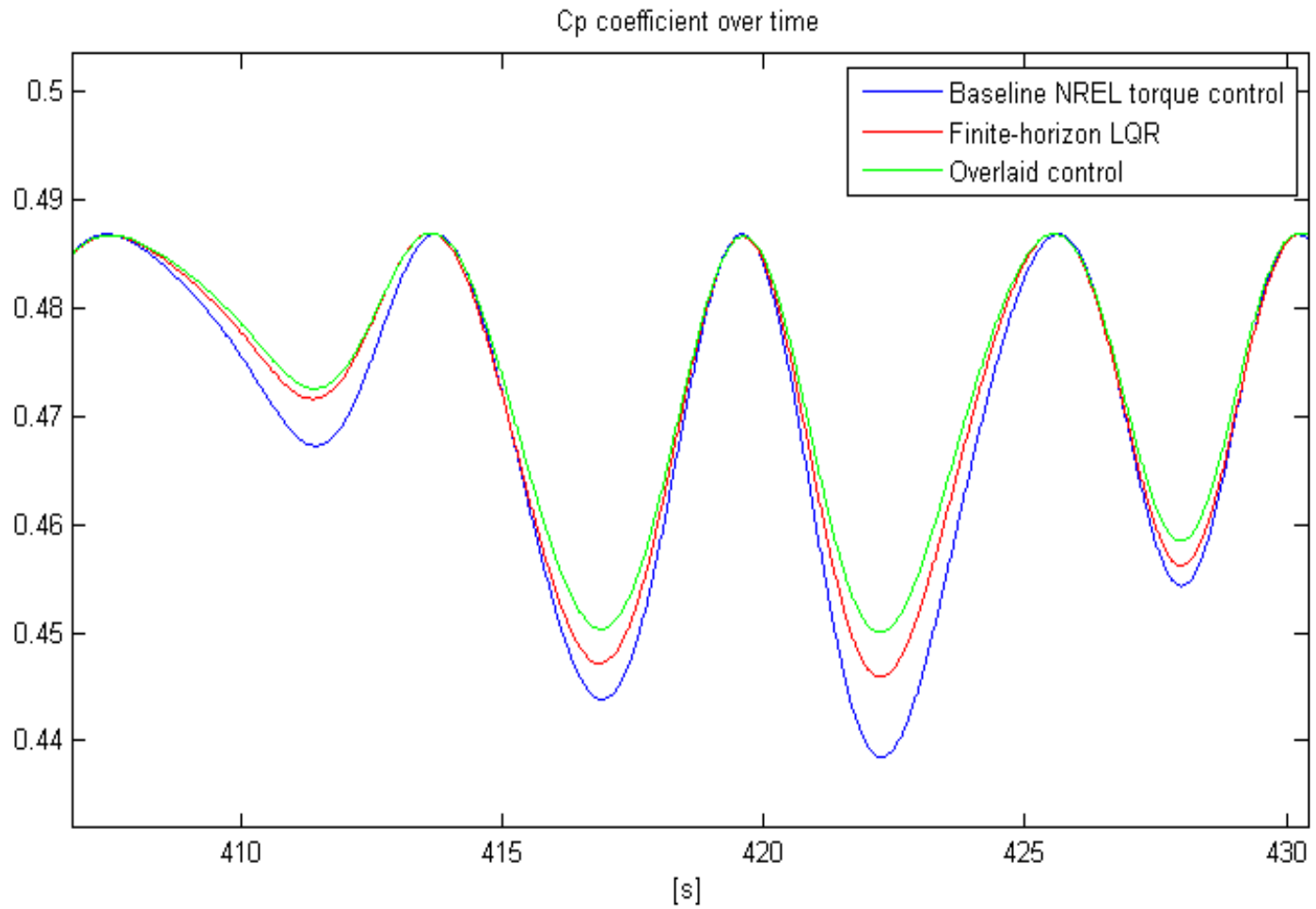




NREL torque controller



Finite-horizon LQR control



Power Coefficient comparison

# Comparison of Target to Conjugate Control Energy Yield Increase

$H_s$	6 m			10 m		
$V_\infty$	6 m/s	8 m/s	10 m/s	6 m/s	8 m/s	10 m/s
<b>Target</b>	+2.3%	+1.74%	+1.51%	+6.46%	+4.83%	+4.06%
<b>Unsteady LQR</b>	+2.952%	+1.595%	+1.261%	+8.306%	+4.889%	+3.927%

# Conclusions

- Nonlinear Loads for Bottom Mounted and Floating Turbines
- Unsteady Conjugate Control of Floating Wind Turbines
- Wind Farm Energy Yield Optimization
- Energy Yield Enhancement via LIDAR Wind Speed Forecasts
- Load Mitigation of Floating Wind Turbines
- Optimal Control of Wave Energy Converters